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## Commentary: The concept of 'Mendelian randomization'

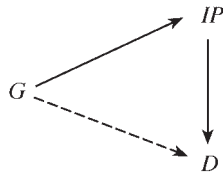
Duncan C Thomas and David V Conti

This issue of the *International Journal of Epidemiology* reprints a seminal letter to the editor by Martijn Katan,<sup>1</sup> which appears to be the first description of the concept of 'Mendelian randomization.' In discussing the controversy over whether the association between low serum cholesterol and cancer is causal or might simply reflect an effect of the disease to lower cholesterol levels ('reverse causation') or confounding by diet or other factors, Katan proposed a test of causality by studying instead

the relationship between cancer and a genetic determinant of serum cholesterol, the apolipoprotein A (*APOE*) gene. His rationale was that since alleles are allocated essentially at random, such an association would not be subject to either confounding or reverse causation. Thus, if a causal relationship between *APOE* and serum cholesterol were clearly established, then an association between *APOE* and cancer would provide indirect evidence for the causality of the association between serum cholesterol and cancer. Although Katan did not use the term 'Mendelian randomization', the concept has been attributed to him and subsequently developed by a number of other authors.<sup>2–6</sup> In particular, Davey Smith and Ebrahim<sup>2</sup>

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have shown how the magnitude of the estimated effects of a gene ( $G$ ) on an intermediate phenotype ( $IP$ ) and on disease ( $D$ ) can be combined to yield an estimate of the causal effect of the intermediate phenotype on disease, as illustrated in the following figure:



(where the dotted arrow from  $G$  to  $D$  represents the indirect association assumed to be mediated entirely through  $IP$ ).

### Use of instrumental variables in epidemiology

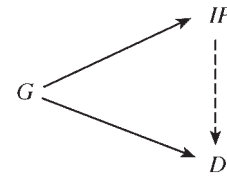
It may seem perverse to try to study the causality of a relationship between  $IP$  and  $D$  through the relationship of each with  $G$ , but there is merit in the idea. While its application to molecular epidemiology is novel, the idea is more than 70 years old, apparently first introduced into the econometrics literature by Wright<sup>7</sup> and later adopted into the statistical measurement error and causal inference literature under the rubric of ‘instrumental variables’.<sup>8–10</sup> The basic idea is that if a causal pathway is correctly specified as in the above Figure (including certain additional assumptions discussed in the Appendix), then the causal effect of  $IP$  on  $D$  can be estimated by the ratio of the coefficients for the regression of  $D$  on  $G$  and of  $IP$  on  $G$ . (An exactly analogous argument applies in randomized controlled trials, where  $G$  would represent ‘intent to treat’ and  $IP$  the treatment actually received: although the  $IP$ – $D$  association could be biased various ways, the  $G$ – $D$  association is guaranteed by randomization to be unbiased and can be used to recover an unbiased estimate of the  $IP$ – $D$  relationship. Similarly, in Berkson error models for measurement error,<sup>11–13</sup>  $G$  might represent an ‘applied exposure’ for a group, such as ambient air pollution, and  $IP$  the unobserved true personal exposure; again, the  $IP$ – $D$  association can be estimated by observation of the  $G$ – $D$  association, although here there is no claim that the  $G$ – $D$  association would be unbiased unless exposure were applied experimentally.) In any of these settings, the precision of this estimate depends strongly upon how well  $G$  predicts  $IP$ . Thompson *et al.*<sup>14</sup> have shown that, even if the causal pathway is correctly specified, the statistical uncertainties in the estimates of the  $G$ – $IP$  and  $G$ – $D$  associations can combine to yield extremely uncertain estimates of the  $IP$ – $D$  relationship.

### Complications

#### Direct effect of $G$ on $D$ not mediated through $IP$

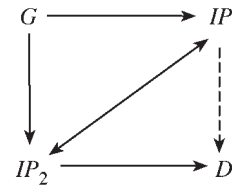
One difficulty is that  $G$  could also have a direct effect on  $D$ . A minor change in the figure shown above shows how it can be used to represent confounding, by turning the  $G$ – $D$  arrow into a solid one representing a direct (causal) connection and turning the  $IP$ – $D$  arrow into a dashed one representing a non-causal

connection induced by confounding by  $G$ :



This would be a case of a ‘false-positive’ inference—an incorrect conclusion that there is a causal connection between  $IP$  and  $D$  when in fact none exists. Of course, negative confounding could also lead to a false-negative conclusion—that there was no association between  $IP$  and  $D$  when there really is one.

One way such a situation could come about is when a single gene has pleiotropic effects. Suppose, for argument sake, that the true causal picture were as follows:



where the solid arrows indicate causal connections and the dashed arrow indicates a non-causal association induced by the other associations.

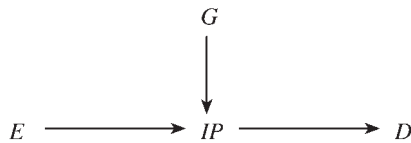
For example, Davey Smith and Ebrahim<sup>2</sup> provide an interesting discussion of the role of folate, homocysteine, and the methylenetetrahydrofolate reductase (*MTHFR*) gene in the aetiology of coronary heart disease (CHD) and neural tube defects (NTD). This is a very complex pathway, involving several feedback loops. For CHD, we agree with their assessment that the similarity of the direct estimate of the association between homocysteine and CHD and the indirect estimate based on the associations of each with *MTHFR* supports a causal interpretation. For NTD, on the other hand, they find a similar concordance of the estimates, but a causal interpretation seems less appropriate. We think it more likely that the second picture applies here, where  $IP_1$  might represent homocysteine and  $IP_2$  folate availability.<sup>6,15,16</sup> Nevertheless, whether homocysteine or serum folate is the proximal cause of NTD, an intervention to increase dietary folate could be an effective preventive measure.

Although  $G$  may be the ultimate determinant of  $IP$ , many other factors can induce expression of  $G$ , so that associations between  $IP$  and  $D$  could better reflect that proximal causal relationship than the more distant  $G$ – $D$  association. Davey Smith and Ibrahim discuss the complications posed by the phenomenon of ‘canalization,’ the buffering of effects of genetic or environmental influences to maintain homeostatic equilibrium, via such mechanisms as alternative metabolic pathways, possibly regulated by different genes. On the other hand,  $G$  remains constant over time and is generally measured with a high degree of accuracy, whereas  $IP$  varies throughout the aetiologically relevant period and a measurement at a single point in time may subject to a large amount of

measurement error (or even bias in the case of reverse causation). These are well-known advantages of the instrumental variables approach, which apply equally to Mendelian randomization.

### Gene—environment interactions

The diagrams we have considered so far do not include any external environmental factors or gene—environment ( $G \times E$ ) interactions. Such a model might be represented schematically as follows:



where  $E$  represents exposure (e.g. dietary folate) and the two arrows converging on  $IP$  could represent independent main effects or a  $G \times E$  interaction (different genetic sensitivities to  $E$  or induction of the expression of  $G$  by  $E$ ). In many, but not all, circumstances, it may be reasonable to assume that  $G$  and  $E$  are independently distributed in the population at risk, i.e. the gene does not predispose one to become exposed. (Obvious counterexamples might be a gene for addictive behaviour, where  $E$  is the substance to which the gene makes one addicted, or where a non-causal association between  $G$  and  $E$  is induced by some confounding factor such as population stratification by ethnicity or use of oral contraceptives being influenced by family history of breast or ovarian cancer.) However, if  $G$  and  $E$  are independently distributed in the source population and each makes independent (additive) contributions to  $IP$ , then  $E$  can be ignored in a linear model and the marginal  $G$ – $D$  and  $G$ – $IP$  associations can still be used to estimate the effect of  $IP$  on  $D$ . This may not apply in non-linear models, however (Appendix). Furthermore, if the two factors are associated or have interactive effects, this distortion could be quite severe and could lead to either false-positive or false-negative inferences. This picture can become even more complicated when the architecture of competing pathways evolves over time in response to developmental influences or exposures via adaptive mechanisms (canalization).<sup>2</sup>

Even in linear models, it seems a stretch to conclude that:

the association of genotype with NTD risk ... demonstrates that an environmental intervention may benefit the whole population, independently of the genotype of individuals receiving the intervention<sup>2</sup>

—at least without good observational evidence about the association of exposure and disease *within* genotype. One would also want to see evidence that changes in exposure actually lead to changes in disease risk, particularly in complex systems where there are multiple points at which different genetic and environmental perturbations may lead to various phenotypic outcomes.<sup>6</sup>

Clayton and McKeigue<sup>3</sup> have argued that:

Despite current enthusiasm for study of gene—environment interactions, the closely related issue of how to define and interpret interaction between environmental factors remains

unresolved after two decades of debate. ... We suggest that epidemiologists should focus instead on use of genetic associations to test hypotheses about causal pathways amenable to intervention. ... In this example [*NAT* and heterocyclic amines in cooked meat], as with the *MTHFR* gene, there is a possible biological interaction between genotype and dietary intake, but testing for statistical interactions between genotype and dietary intake would not contribute much to our understanding of these biological interactions or to our ability to exploit them in disease prevention. ... The prospects for epidemiology in the post-genome era depend on understanding how to use genetic associations to test hypotheses about causal pathways, rather than on modeling the joint effects of genotype and environment.

Part of their argument relies on the observation that power to test main effects will often be much better than for interactions, although there are exceptions.<sup>17</sup> Hence the opportunity to exploit Mendelian randomization to assess causality is a great advantage of tests of pure genetic main effects. Indeed, the track record of replication of reports of  $G \times E$  interactions seems to be even more dismal than for main effects of gene associations,<sup>18–20</sup> perhaps in large part because such studies are frequently underpowered, involve some data dredging, and are subject to publication bias. We generally agree with their conclusion that:

A case-control study of the relation between the TT genotype [of *MTHFR*] and risk of neural tube defect *can be interpreted as equivalent to a randomized trial* of the effect on disease risk of alteration of the availability of folate<sup>3</sup> [emphasis added].

### Gene—gene interactions

The same picture might apply if one were to replace  $E$  by another gene, say  $H$ . It is quite conceivable that a second causal variant may exist within the same candidate gene region and be in linkage disequilibrium with  $G$ . The lack of independence between  $H$  and  $G$  may lead to substantial bias in the estimation of the  $G$ – $D$  association.<sup>6</sup> Furthermore, by the same line of argument as above for non-linear models, if  $IP$  were determined by two genes (either independently or in some interactive manner), but one only assessed  $G$ , then the association between  $IP$  and  $D$  estimated from the associations of each with  $G$  would also be biased. In particular, a false-negative conclusion could be reached if  $H$  were really the more relevant determinant of  $IP$  and failure to account for it led to a null result for the  $G$ – $D$  association. As with  $G \times E$ , failure to account for  $G \times G$  interactions could also lead to either false-positive or false-negative inferences.

### Population stratification

A reservation about the broad conclusion Mendelian randomization is equivalent to a randomized trial is that  $G$ – $D$  associations from case-control studies are susceptible to distortion by population stratification.<sup>6</sup> Not only substantial genetic differences in populations, but more subtle clustering of genetically similar individuals within the population, can bias a test of the  $G$ – $D$  association.<sup>21</sup> Although some have argued that population stratification may not be a serious concern, at least in Caucasian populations of European descent,<sup>22,23</sup> this problem can be overcome by appropriate design or analysis. The low power of Mendelian randomization compared with direct tests of association implies that very large sample sizes will be required.

Unfortunately, the problem of inflation of Type I Error rates by population stratification will only increase with increasing sample size, as smaller and smaller biases will become significant.

To fully exploit the power of Mendelian randomization, one should consider using the case-parent-triad design that is based on the random transmission of alleles from parents to offspring and is therefore robust to population stratification.<sup>24,25</sup> Similar properties are shared by other family-based association tests (FBAT), such as a sib case-control design and those that exploit both parents and siblings or even extended pedigrees.<sup>26–29</sup>

### Conclusions

We conclude that the validity of the Mendelian randomization approach to evaluating the causality of an association between *IP* and *D* depends upon the correct specification of the causal model. If *G* has multiple effects, at least one of which has a causal effect on *D* through some pathway not involving *IP*, or if the association between *G* and *D* is confounded by population stratification or other genes it is in linkage disequilibrium with, then the estimated association between *IP* and *D* will be distorted. The method will be most efficient when the connection between *G* and *IP* is strong, as noted by Davey Smith and Ibrahim<sup>2</sup> in comparing the usefulness of the beta-fibrinogen and haptoglobin polymorphisms as predictors of plasma fibrinogen and vitamin C respectively.

Biological pathways are extremely complex, so a simple triangulation picture will almost certainly be wrong in most situations. However, our understanding of these pathways will doubtless continue to improve (and hence the pictures will get more and more complicated), but on the other hand, prospects for overcoming confounding and reverse causation in traditional observational studies of the *IP*–*D* association are very limited. In the long run, the concept of Mendelian randomization may prove to be a valuable way for epidemiology to move ‘beyond its limits’. Thus, the conditions for its validity deserve careful consideration.

### Appendix

#### Validity and efficiency of the ‘instrumental variables’ approach

Suppose we wish to estimate the slope of a regression of *D* on *IP* and we have available a surrogate variable *G* for *IP*—that is, *G* is a determinant of *IP* but is conditionally independent of *D* given *IP*. We begin by assuming all the relationships are linear, before turning our attention to the additional complications that arise in non-linear models. Thus, we assume

$$\begin{aligned} E(D|IP) &= \beta_0 + \beta_1 IP, & \text{var}(D|IP) &= \sigma^2 \\ E(IP|G) &= \alpha_0 + \alpha_1 G, & \text{var}(IP|G) &= \tau^2 \end{aligned}$$

Then,

$$E(D|G) = \gamma_0 + \gamma_1 G, \quad \text{var}(D|G) = \omega^2$$

where  $\gamma_0 = \beta_0 + \beta_1 \alpha_0$ ,  $\gamma_1 = \beta_1 \alpha_1$ , and  $\omega^2 = \sigma^2 + \beta_1^2 \tau^2$ . Thus, if one had unbiased estimators of  $\gamma_1$  and  $\alpha_1$ , then  $\gamma_1/\alpha_1$  becomes an unbiased estimator of  $\beta_1$  but its variance is complex (see ref. 14 for a derivation), and can be infinite in the event that the

variance of  $\alpha_1$  is large in relation to its true value. Note also that the parameter of interest,  $\beta_1$ , is involved in  $\text{var}(D|G)$  and thus ignoring this information will lead to a less than fully efficient estimator. In particular, if  $\text{var}(IP|G)$  were not constant, then an appropriately weighted estimator of  $\gamma$  would be required. In any event, the variance of a ratio can be quite unstable, depending strongly upon  $\tau^2$ . Thus, if *G* were not a good predictor of *IP*, then  $\text{var}(\gamma_1/\alpha_1)$  will be very large.

The derivation above assumes that the model is correctly specified. In the main body of our article, we describe several ways the model could be misspecified and the implications for bias. For example, suppose *G* has a direct effect on *D*, independent of *IP*, say  $E(D|IP) = \beta_0 + \beta_1 IP + \beta_2 G$ . Then it is easy to see that  $\gamma_1/\alpha_1$  estimates  $\beta_1 + \beta_2/\alpha_1$ , and thus will yield a biased estimate of the causal effect of *IP* on *D*. Alternatively, suppose there is another factor that influences *IP*, say *H*, which could be another gene or some environmental factor. Suppose first that *H* has no direct effect on *D* other than through its influence on *IP*, and *G* and *H* are independent and contribute additively to *IP*, that is,  $E(IP|G, H) = \alpha_0 + \alpha_1 G + \alpha_2 H$ . Then even if *H* is ignored,  $\gamma_1/\alpha_1$  still estimates  $\beta_1$ , although its variance will be increased. However, if *G* and *H* are associated in the population or if they have an interactive effect on *IP*, then both  $\gamma_1$  and  $\alpha_1$  will be biased, but to the same extent, so their ratio  $\gamma_1/\alpha_1$  turns out to be a consistent estimator of  $\beta_1$  (assuming there is no direct effect of *G* or *H* on *D* except through *IP*). To see this, suppose  $E(H|G) = \eta_0 + \eta_1 G$ . Then if  $E(IP|G, H) = \alpha_0 + \alpha_1 G + \alpha_2 H$ , then  $E(IP|G) = \alpha_0 + \alpha_1 G + \alpha_2 E(H|G) = \alpha_0^* + \alpha_1^* G$ , where  $\alpha_0^* = \alpha_0 + \alpha_2 \eta_0$  and  $\alpha_1^* = \alpha_1 + \alpha_2 \eta_1$ . Likewise, if  $E(D|IP, G, H) = \beta_0 + \beta_1 IP$ , then  $E(D|G) = \beta_0 + \beta_1 E[IP|G, E(H|G)] = \gamma_0^* + \gamma_1^* G$ , where  $\gamma_0^* = \beta_0 + \beta_1(\alpha_0 + \alpha_2 \eta_0)$  and  $\gamma_1^* = \beta_1(\alpha_1 + \alpha_2 \eta_1)$ . Thus  $\gamma_1^*/\alpha_1^* = \beta_1(\alpha_1 + \alpha_2 \eta_1)/(\alpha_1 + \alpha_2 \eta_1) = \beta_1$ . This also applies if *G* and *H* have an interactive effect on *IP* (but no direct effects on *D*), provided the estimates of the *GD* and *GIP* associations derive from the same dataset or studies with the same joint distribution of *G* and *H*.

For dichotomous disease traits, the derivation is somewhat more complex and the conditions for validity are more restrictive. The most tractable situation is when  $IP \sim N(\alpha_0 + \alpha_1 G, \tau^2)$  and  $\ln[\text{Pr}(D = 1|IP)] = \beta_0 + \beta_1 IP$  for a rare disease. Then it is easily shown that  $\ln[\text{Pr}(D = 1|G)] = \gamma_0 + \gamma_1 G$ , where  $\gamma_0 = \beta_0 + \beta_1 \alpha_0 + \beta_1^2 \tau^2/2$  and  $\gamma_1 = \alpha_1 \beta_1$ , so  $\gamma_1/\alpha_1$  is a consistent estimator of  $\beta_1$ , just as in the linear model. For a probit link, the corresponding expression is  $\beta_1 = \gamma_1/\sqrt{(\alpha_1^2 - \gamma_1^2 \tau^2)}$ , without the need for a rare disease assumption, but now the ratio  $\gamma_1/\alpha_1$  is only an approximate estimator of  $\beta_1$ . Closed-form solutions are not available for the logistic model, but qualitatively the behaviour is similar.<sup>14</sup> As before, a direct effect of *G* on *D* will yield a biased estimator.

Unlike the linear model, however, if there is another factor *H* influencing *IP*, then if *G* and *H* are not independent, the estimators  $\gamma_1$  and  $\alpha_1$  are both biased, but these biases may no longer cancel out exactly. Suppose that  $\ln[\text{Pr}(D = 1|IP)] = \beta_0 + \beta_1 IP$  and  $IP \sim N(\alpha_0 + \alpha_1 G + \alpha_2 H, \tau^2)$ . If  $H \sim N(\eta_0 + \eta_1 G, \omega^2)$  and *H* is ignored, then  $IP \sim N(\alpha_0^* + \alpha_1^* G, \tau^2 + \alpha_2^2 \omega^2)$ , where  $\alpha_1^* = \alpha_1 + \alpha_2 \eta_1$ , and  $\ln[\text{Pr}(D = 1|G)] = \gamma_0^* + \gamma_1^* G$ , where  $\gamma_1^* = \beta_1(\alpha_1 + \alpha_2 \eta_1)$ , so in this case  $\gamma_1/\alpha_1$  is indeed a consistent estimator of  $\beta_1$ . But now suppose instead that *H* were dichotomous, with  $\text{Pr}(H = 1|G) = p_G$ . Then  $\gamma_1^* = \beta_1 \alpha_1 + \ln[1 + p_1 \exp(\beta_1 \alpha_2)] - \ln[1 + p_0 \exp(\beta_1 \alpha_2)]$  and  $\alpha_1^* = \alpha_1 +$

$\alpha_2(p_1 - p_0)$ . Thus  $\gamma_1^*/\alpha_1^*$  will not estimate  $\beta_1$  unless  $p_1 = p_0$  or  $\alpha_2 = 0$  or  $\beta_2 = 0$ .

In general, the validity of Mendelian randomization lies in the equivalency of  $\alpha_1\beta_1 = \gamma_1$ . That is, the association between  $GIP$  and  $IPD$  is assumed to be equivalent to the  $GD$  relation. If  $g(D|\cdot)$  gives the functional relation between an exposure and the disease outcome and  $h(IP|G)$  gives the relation between the gene variant and the intermediate phenotype, then for Mendelian randomization estimates to be valid, it must be possible to write  $g(D|G, \gamma_1) = \int g(D|IP, \beta_1) h(IP|G, \alpha_1) dIP$  as  $g(D|G, \alpha_1\beta_1)$ . This holds if  $h(\cdot)$  is conjugate to  $g(\cdot)$ .

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