

# Flexible Models for Secure Systems

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**Sarah Meiklejohn**

# A creation story

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Motivating scenario that founded modern cryptography:

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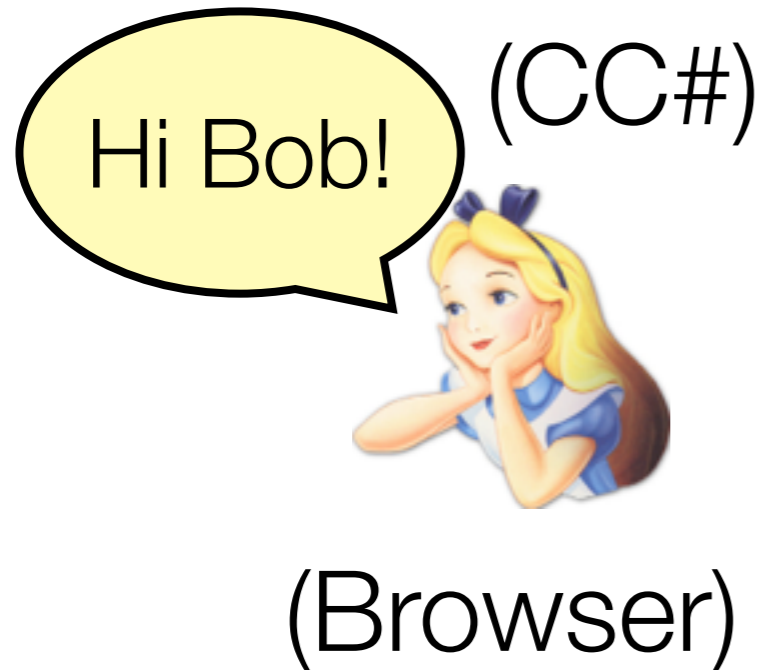
Motivating scenario that founded modern cryptography:



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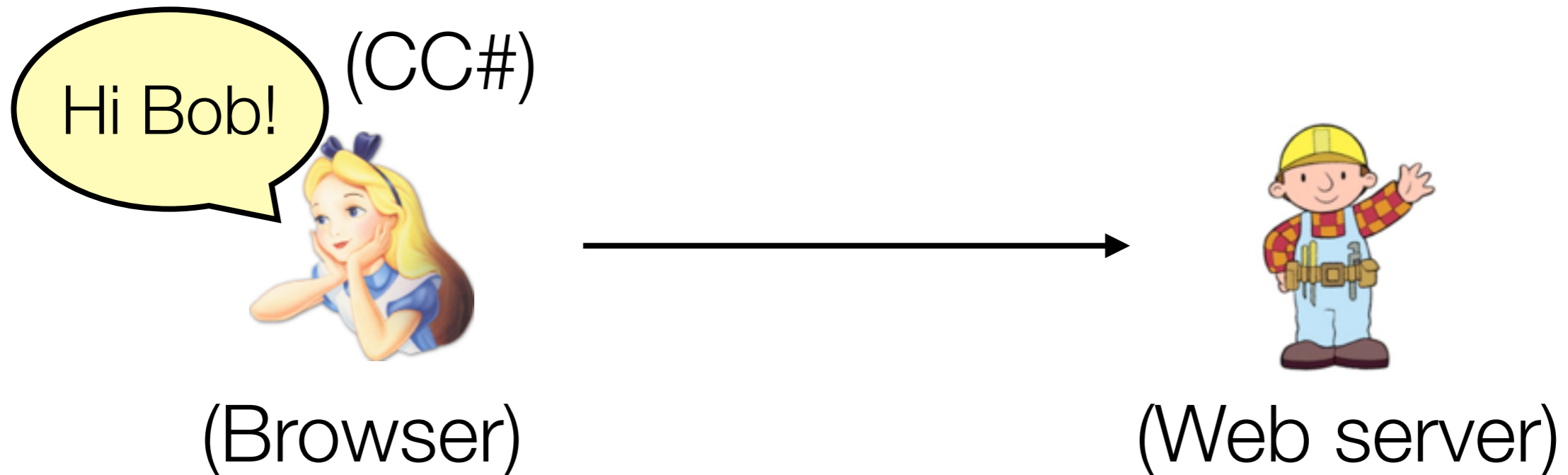
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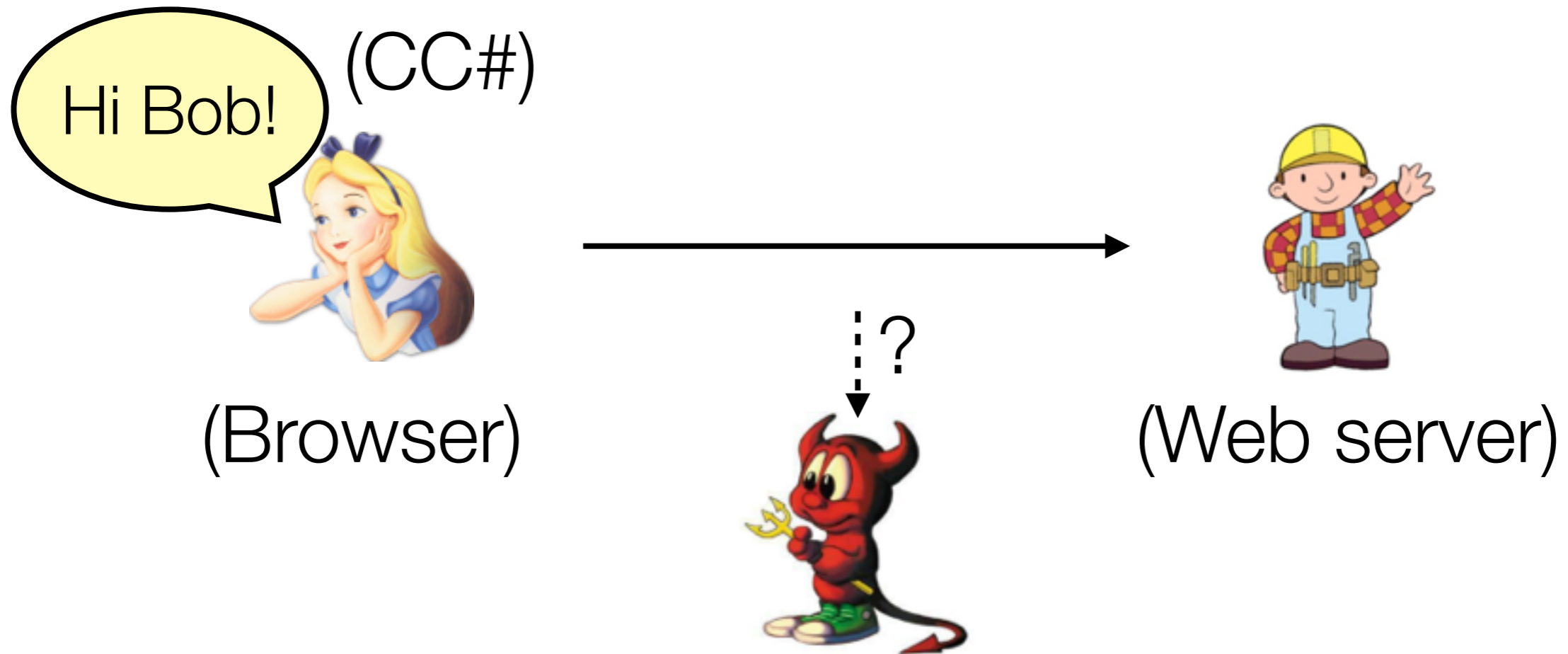


**Security model** for this interaction is **well established**

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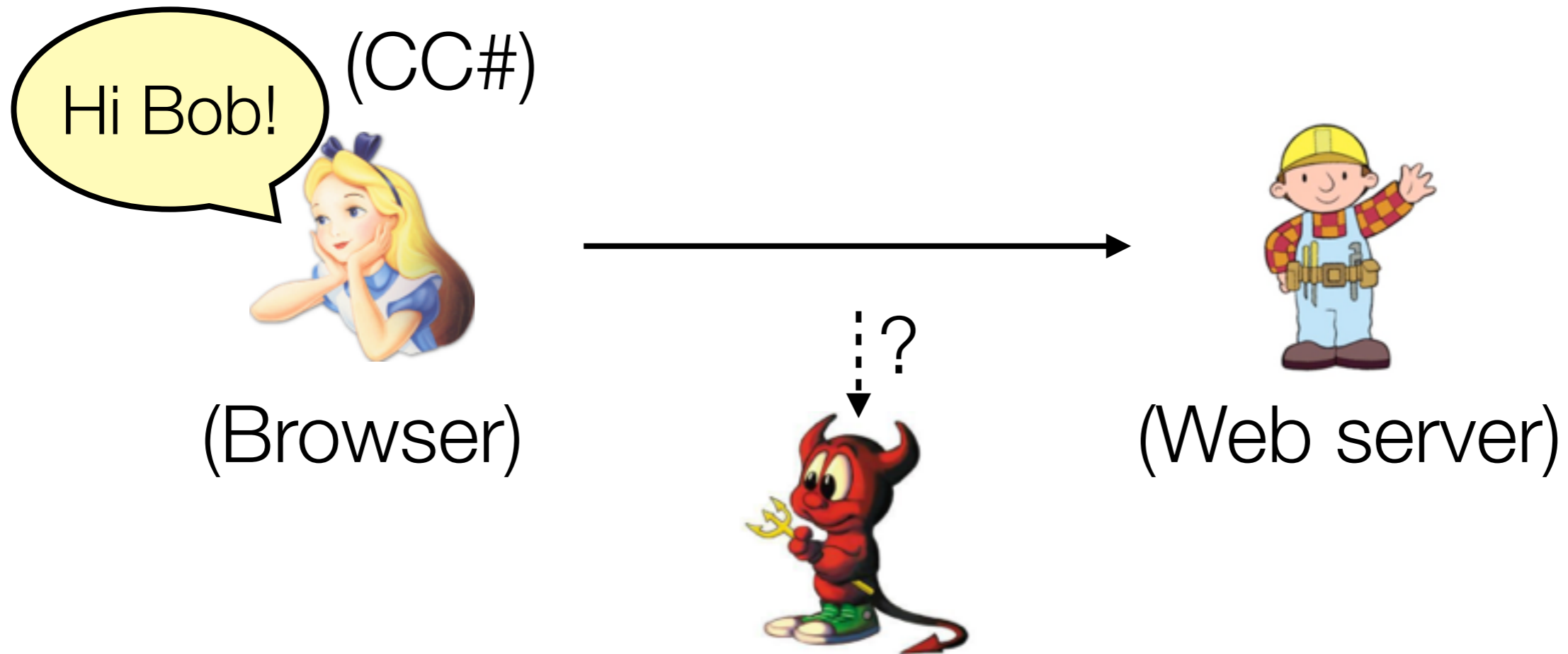


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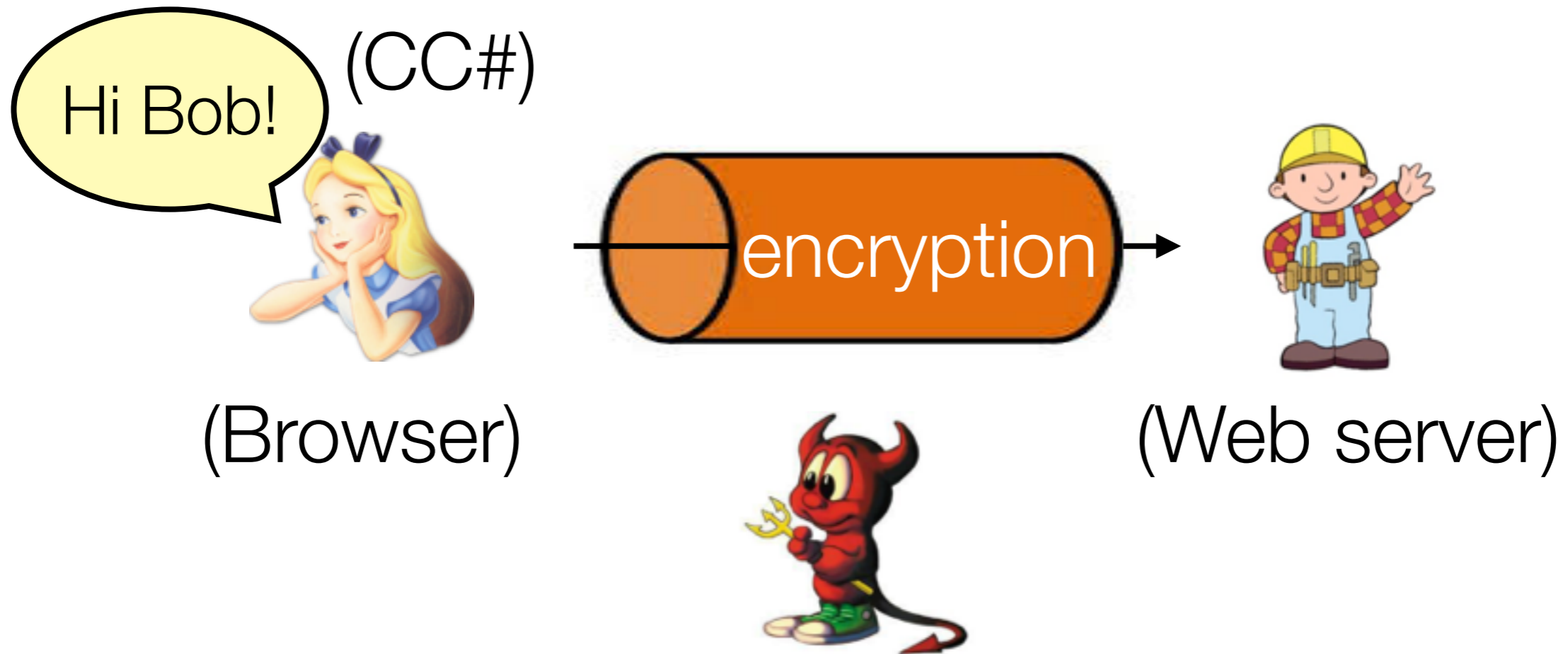
Encryption works for **secure online communication**: SSL/TLS [1996]



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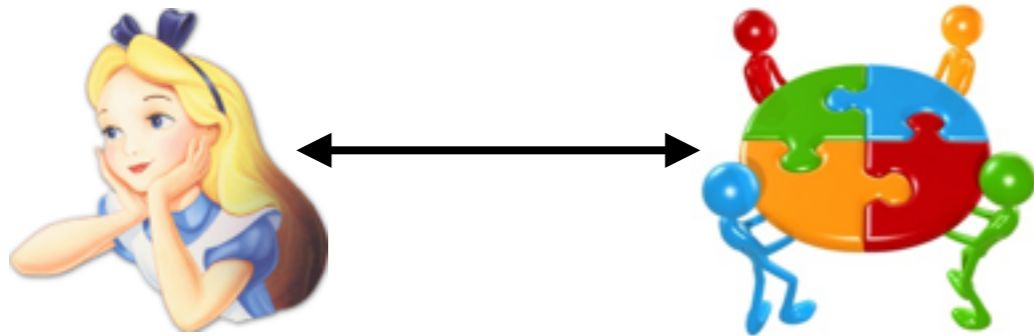
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Fast-forward 15 years...

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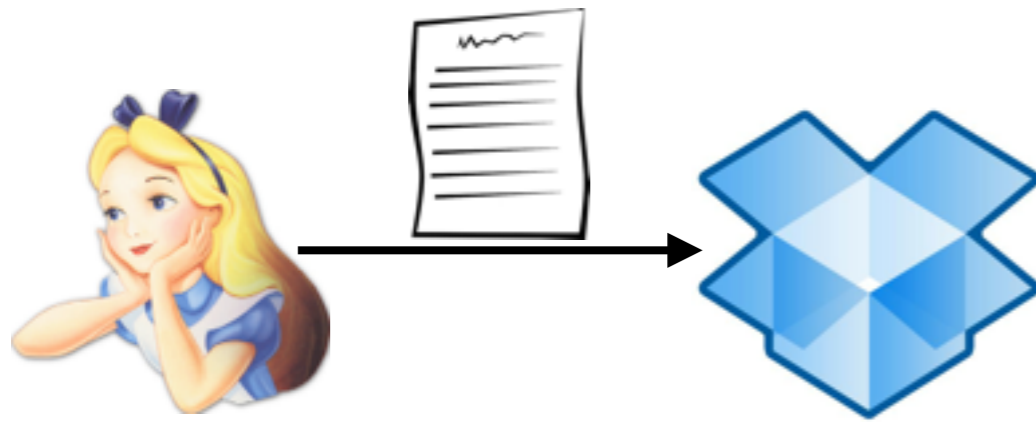
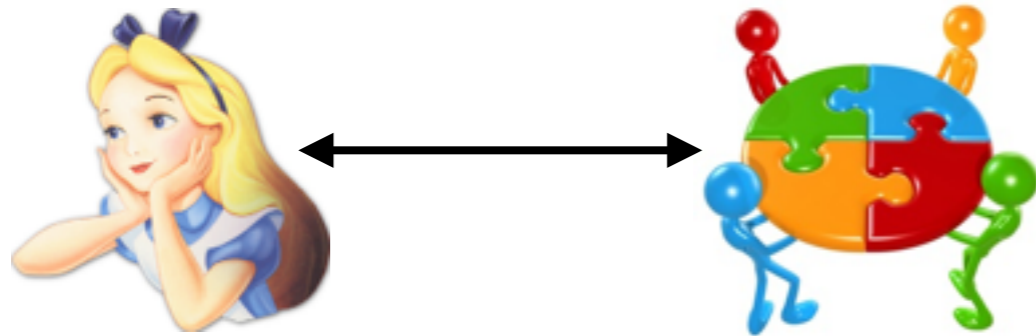
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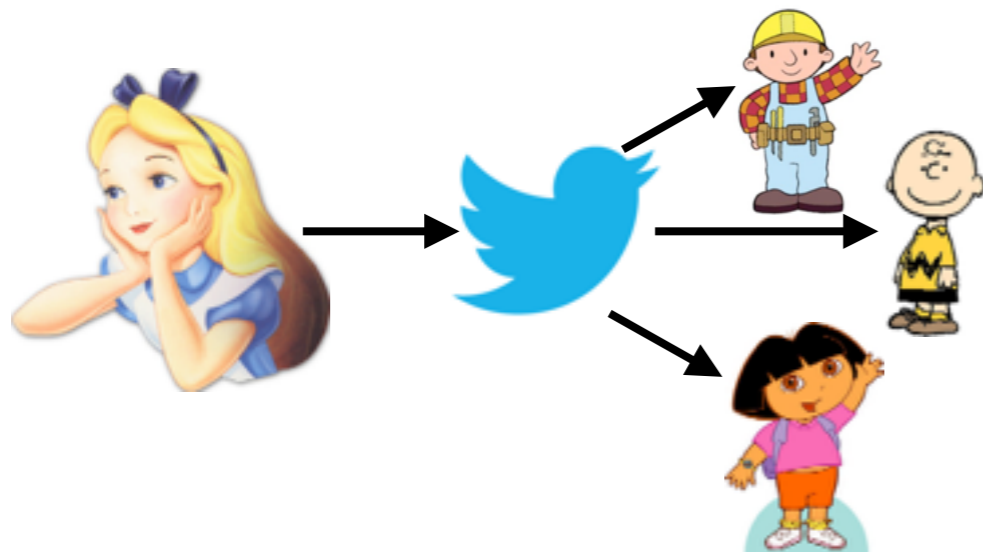
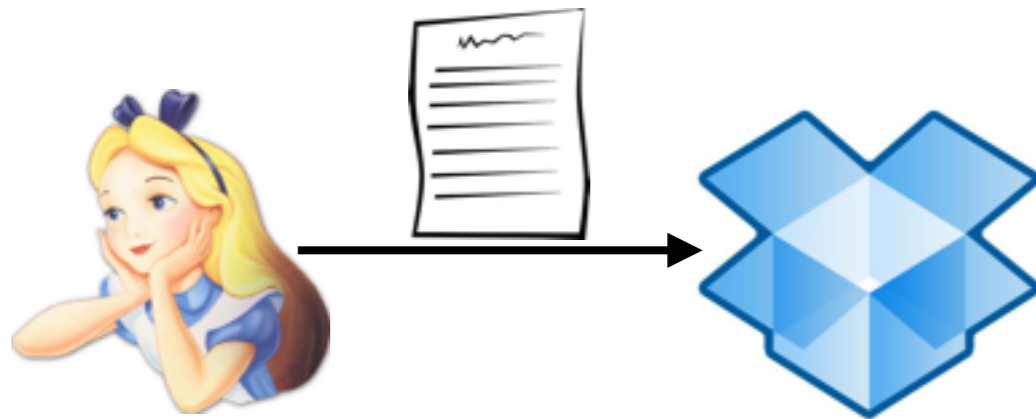
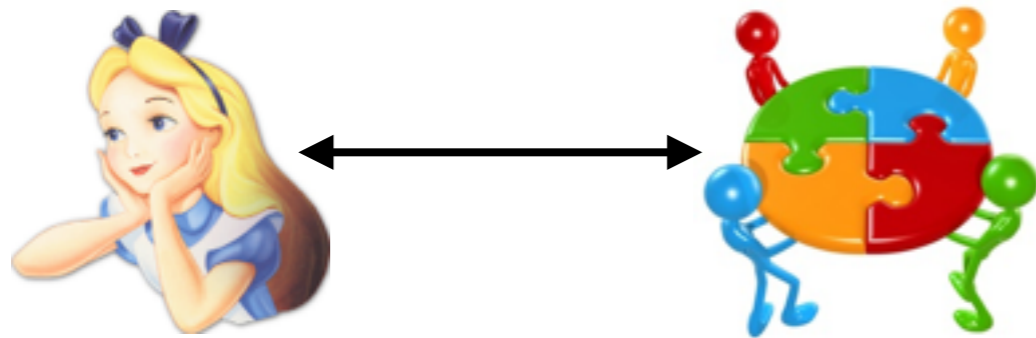
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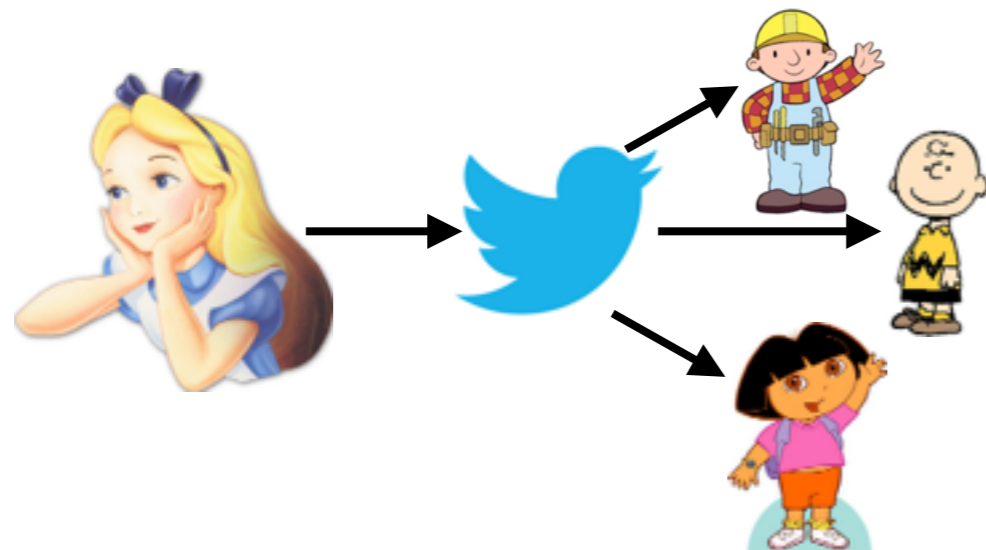
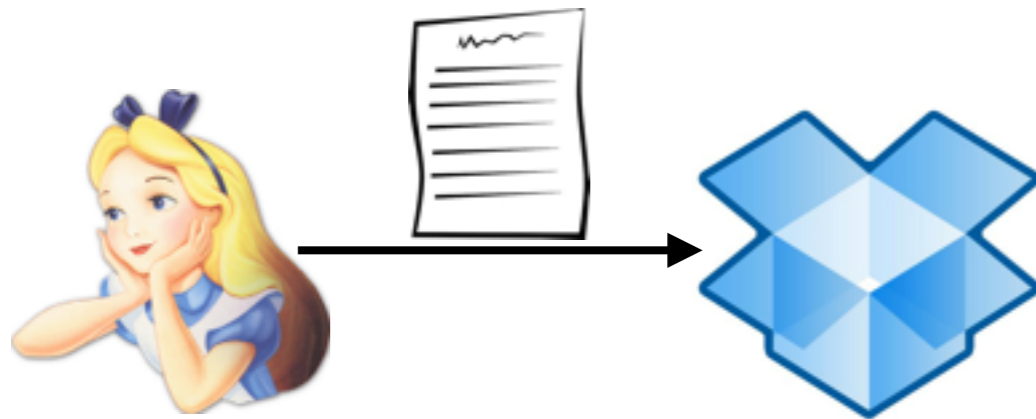
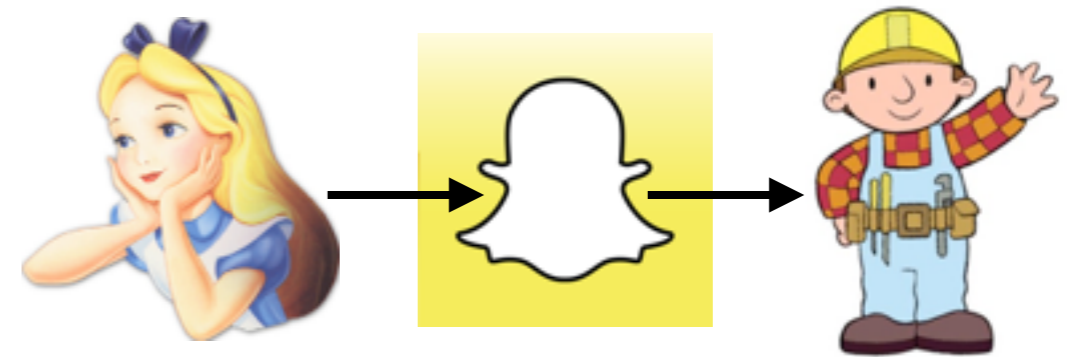
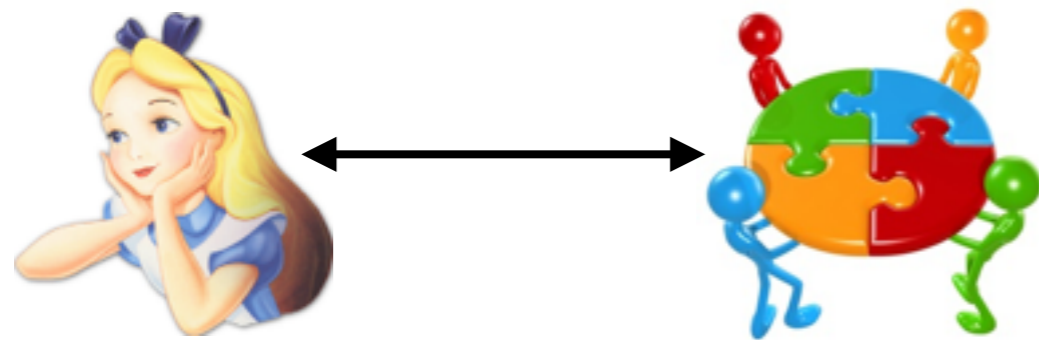
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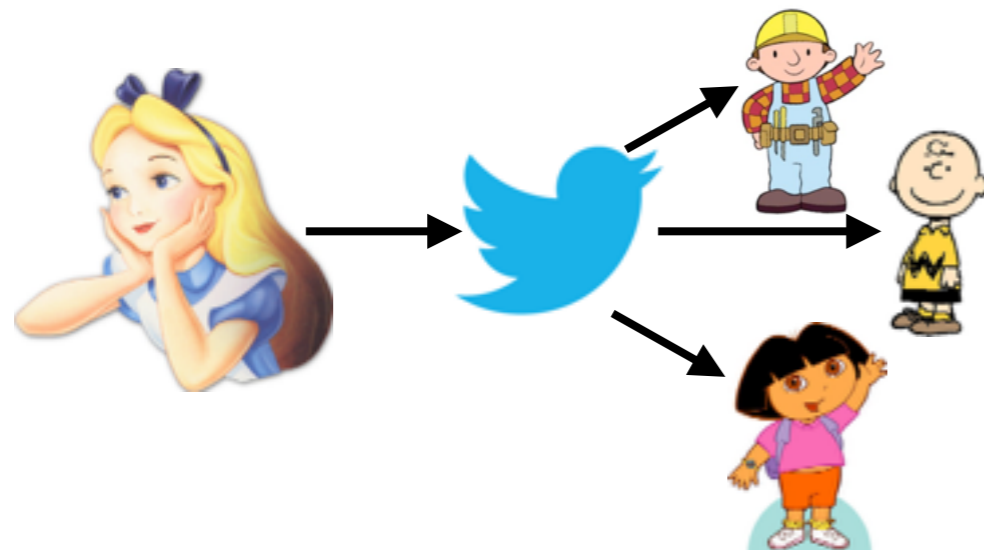
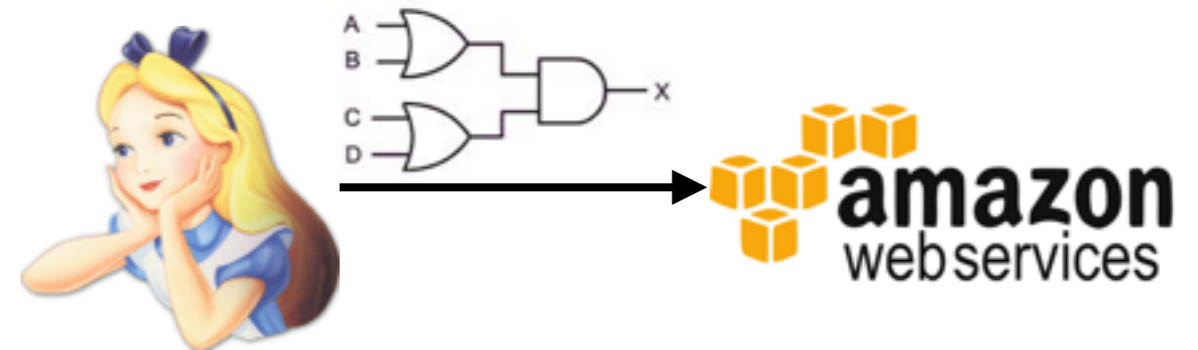
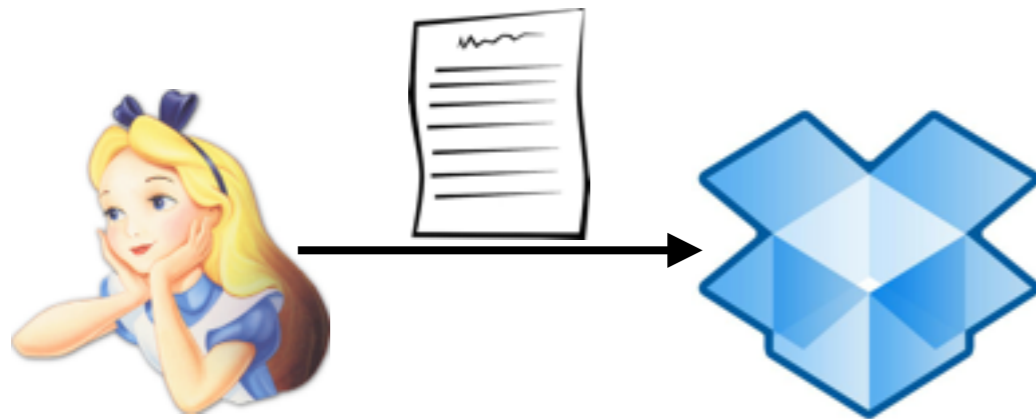
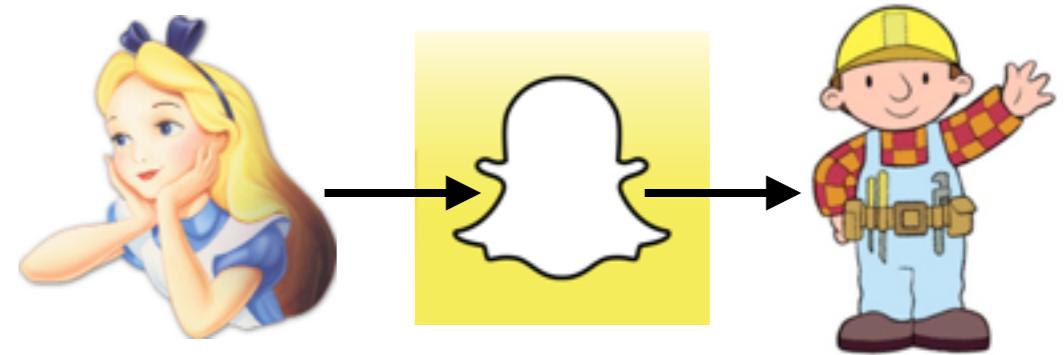
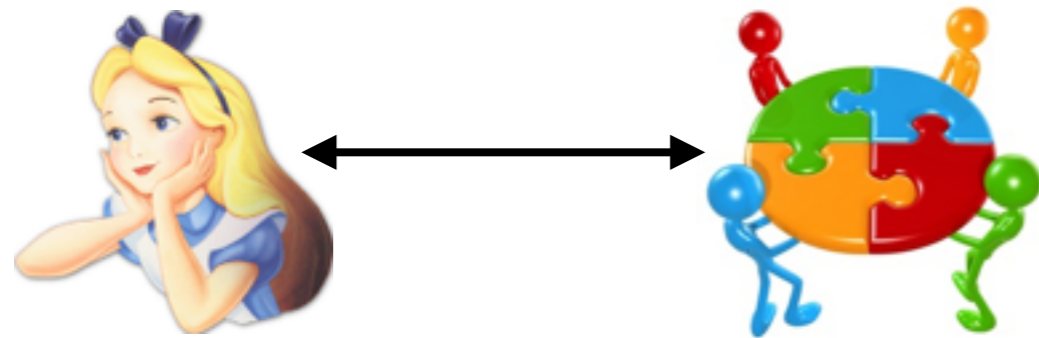
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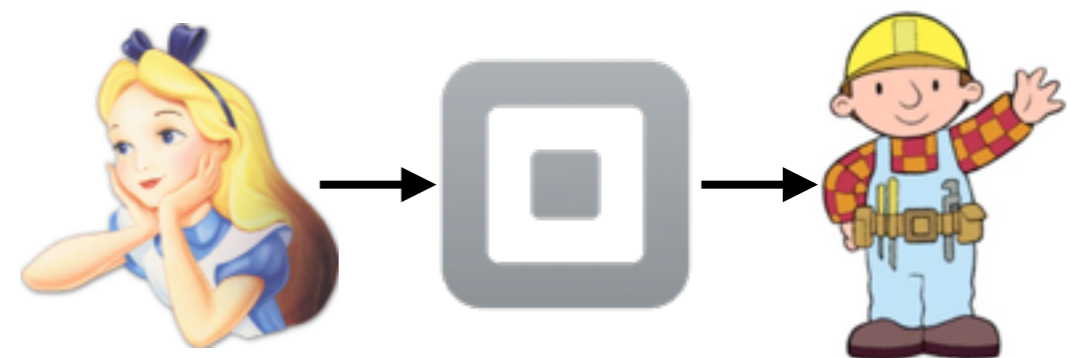
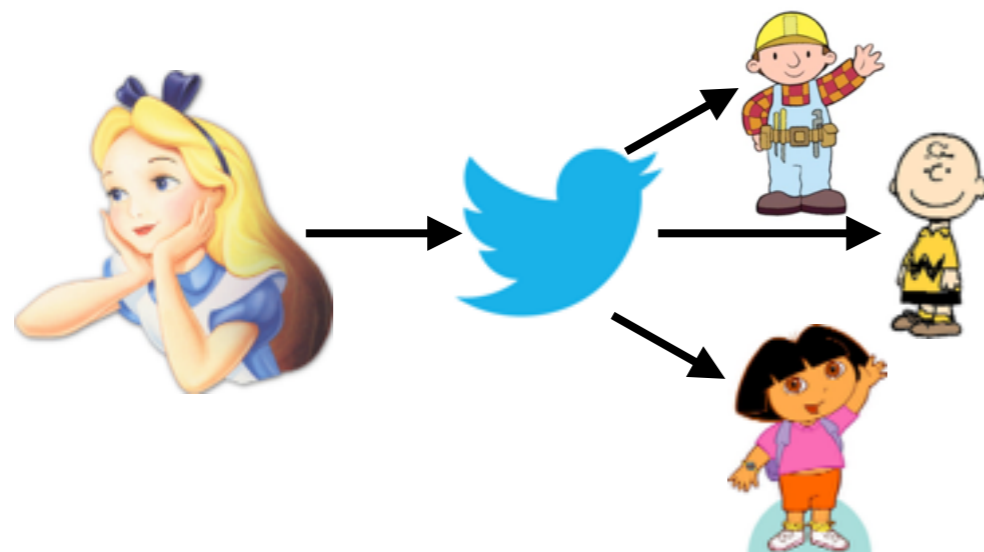
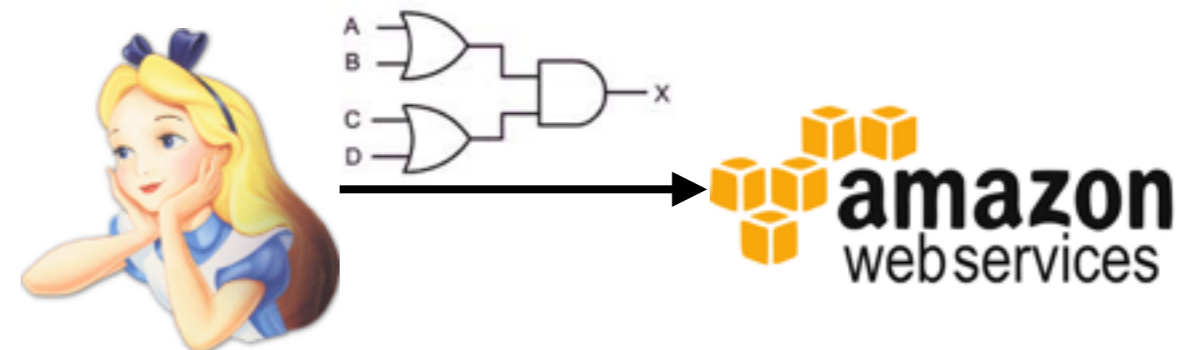
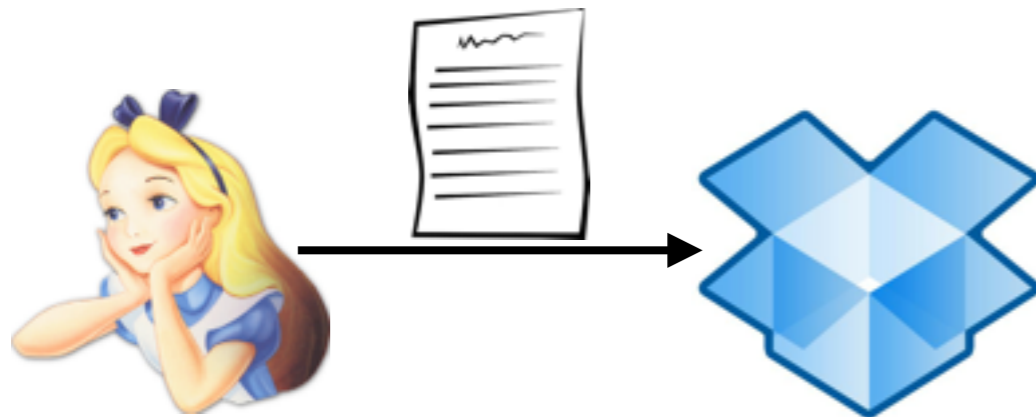
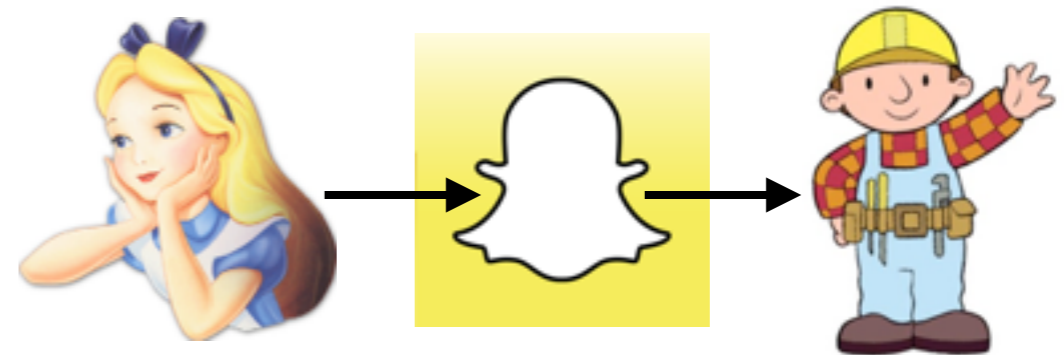
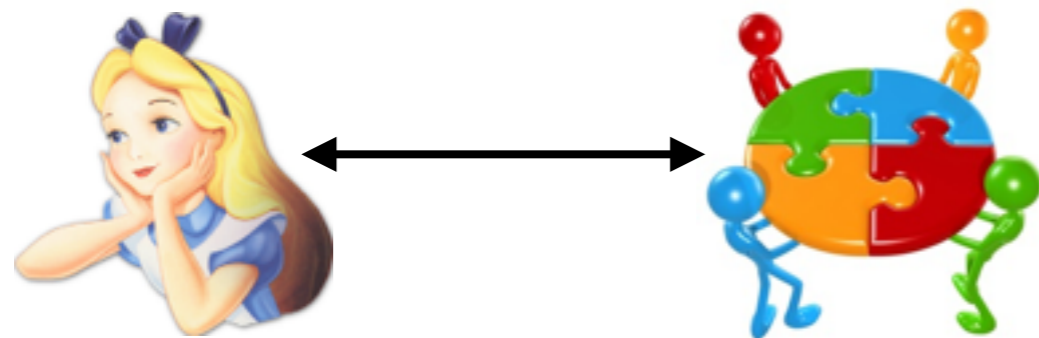
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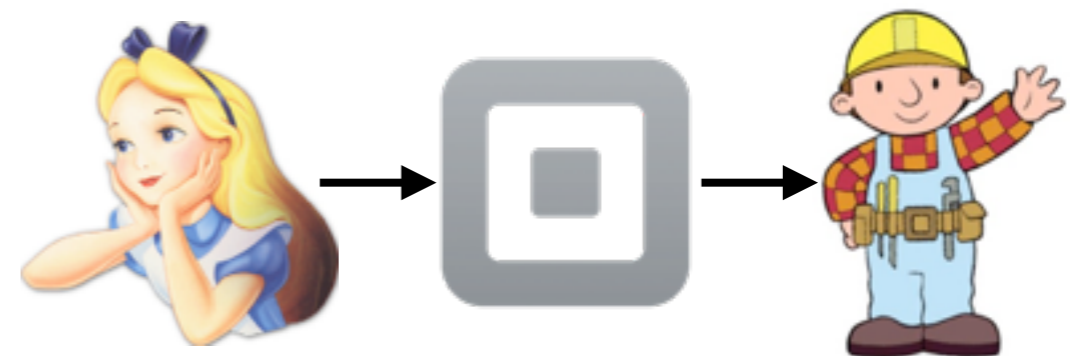
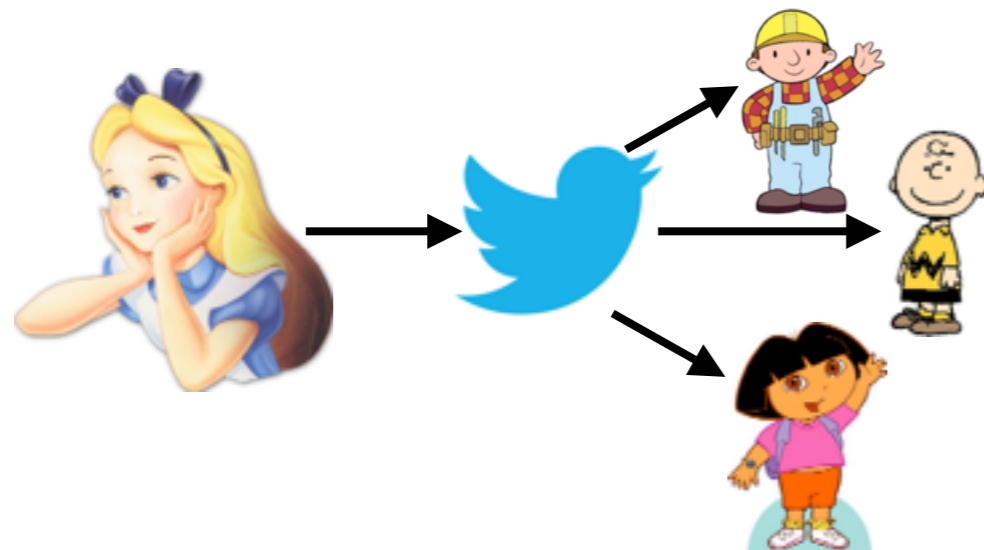
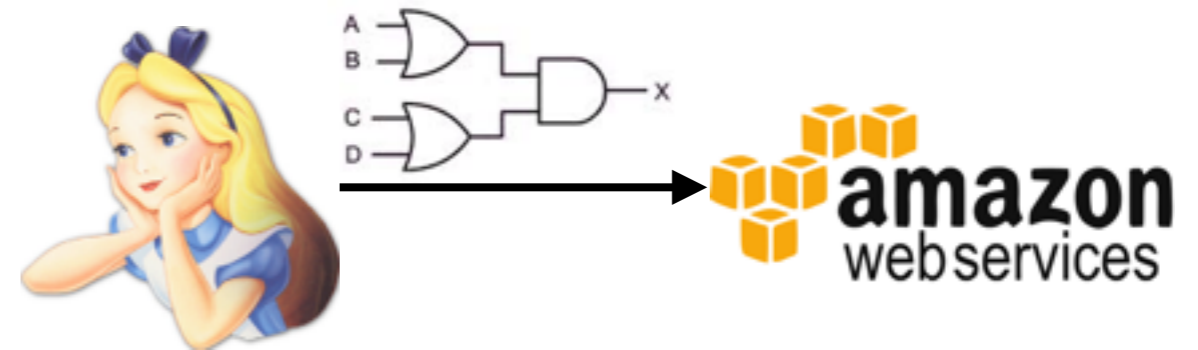
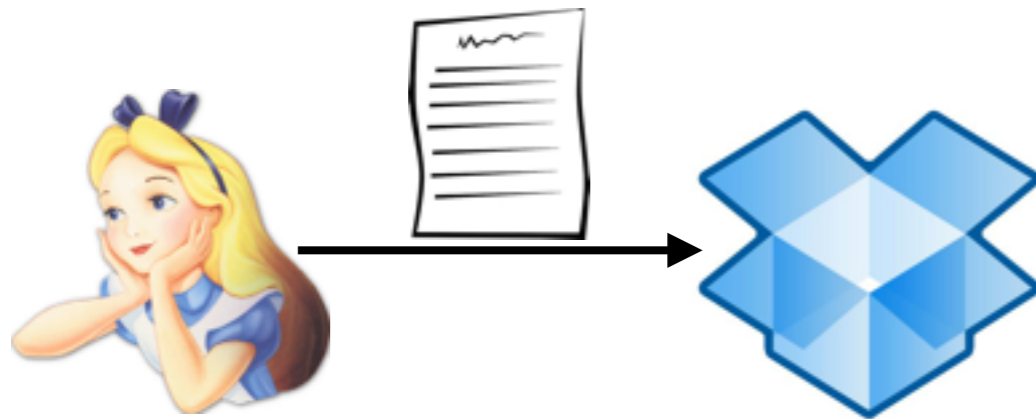
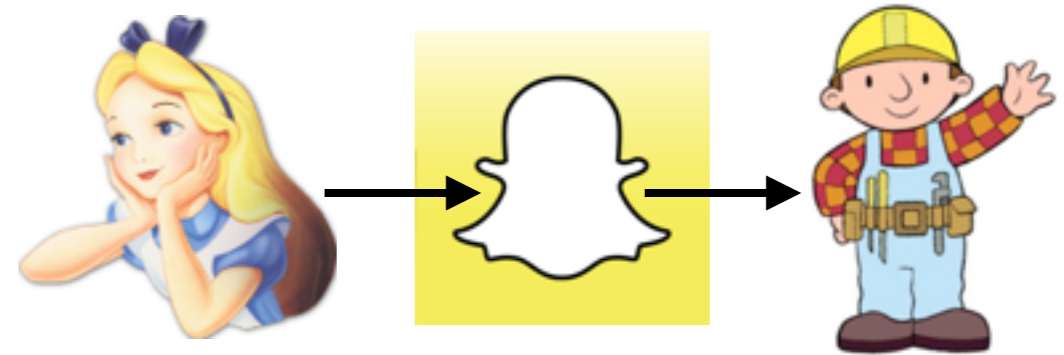
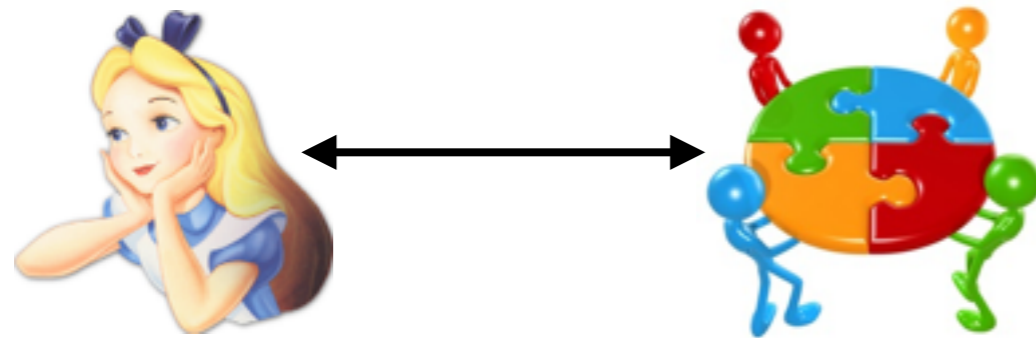
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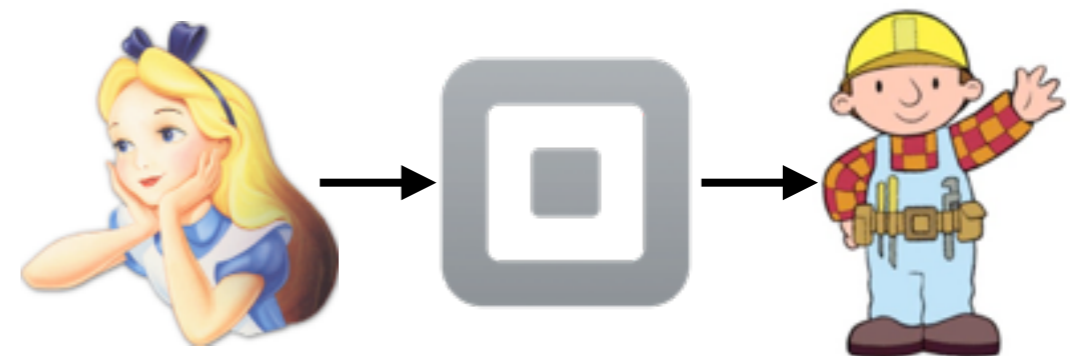
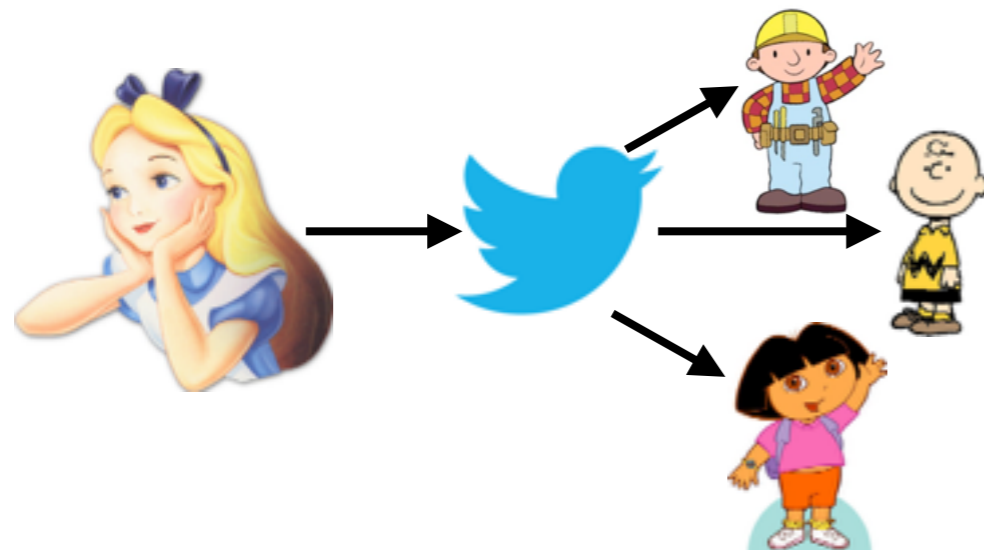
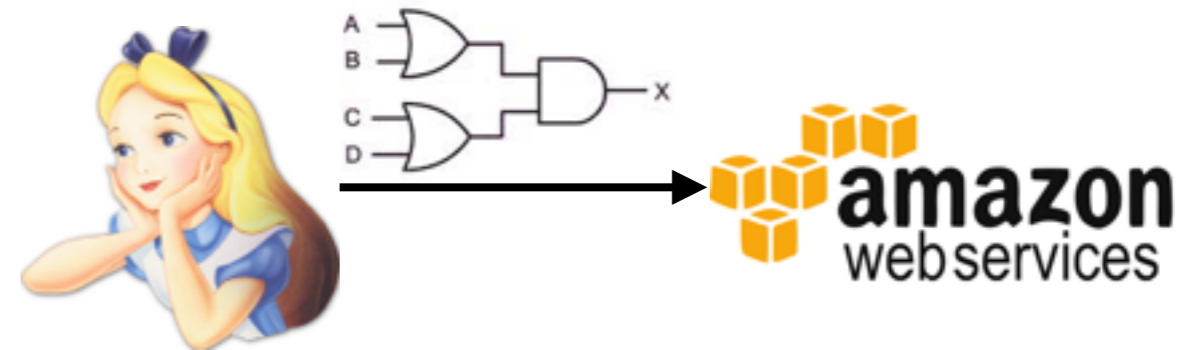
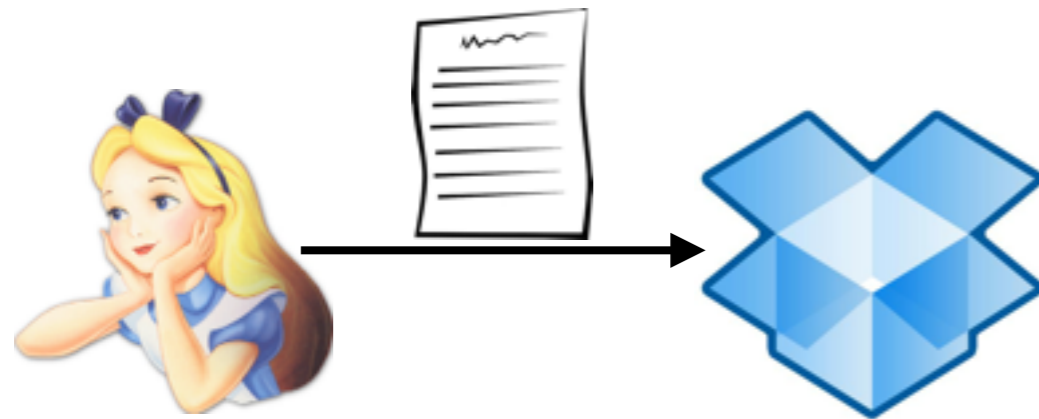
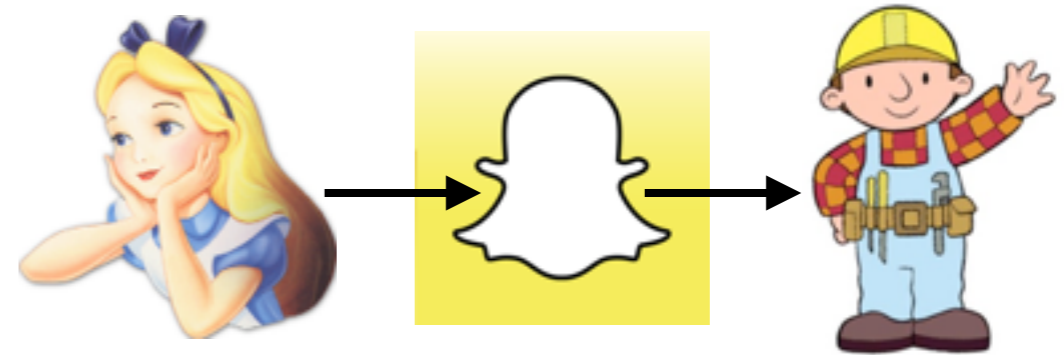
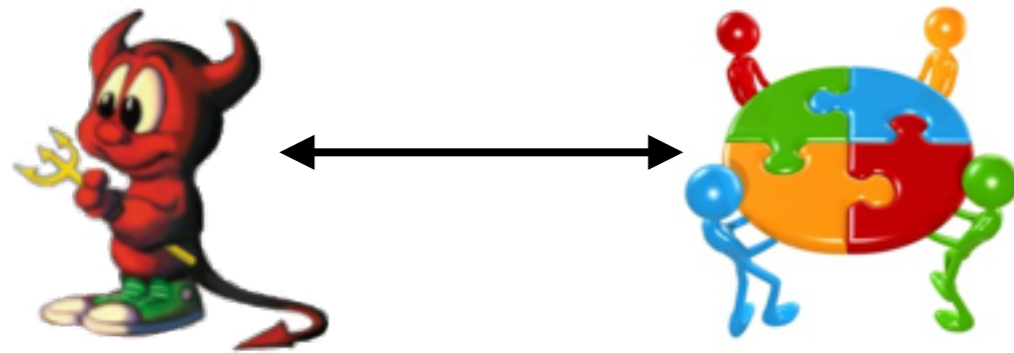
Fast-forward 15 years...

**Problem #1: everyone is an adversary!**



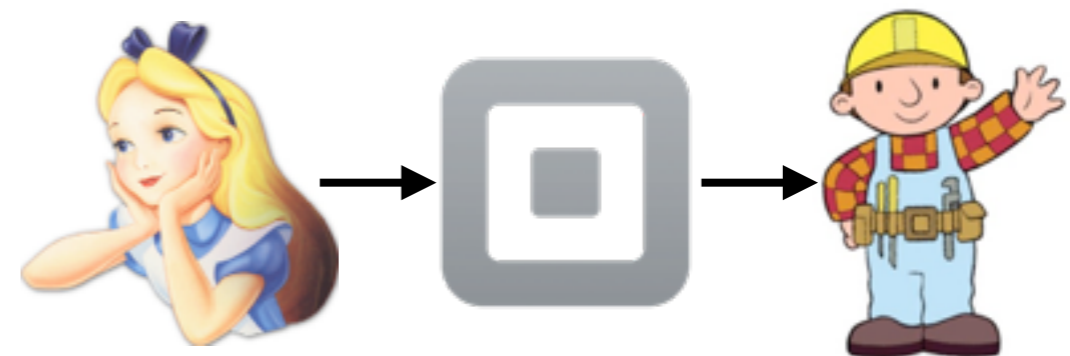
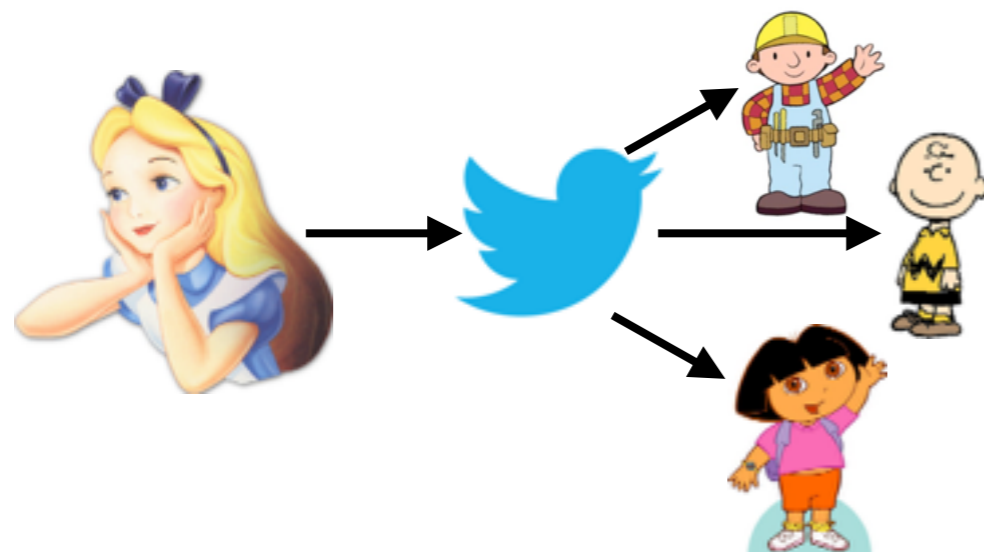
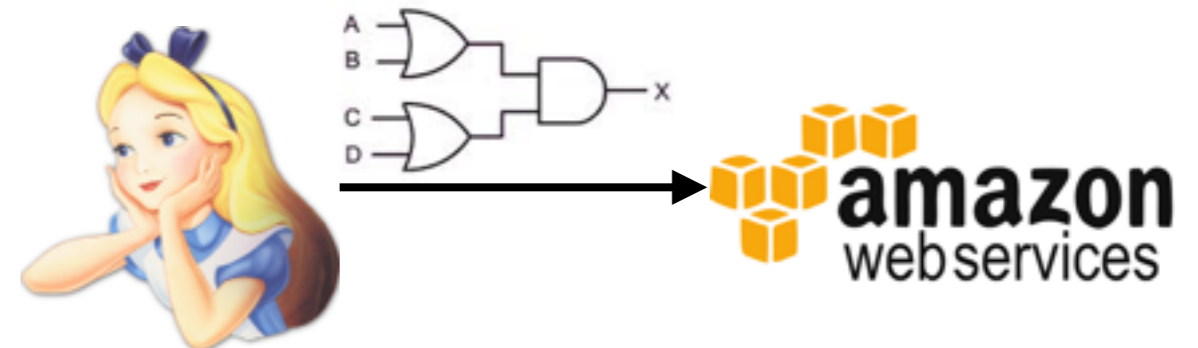
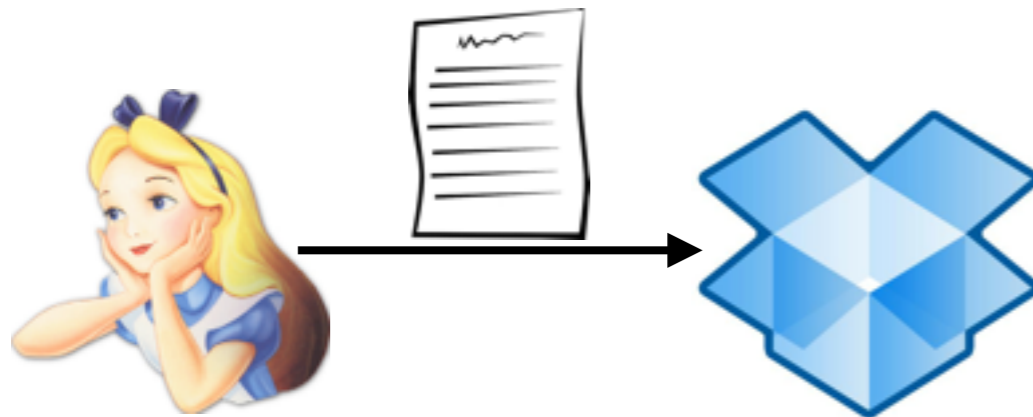
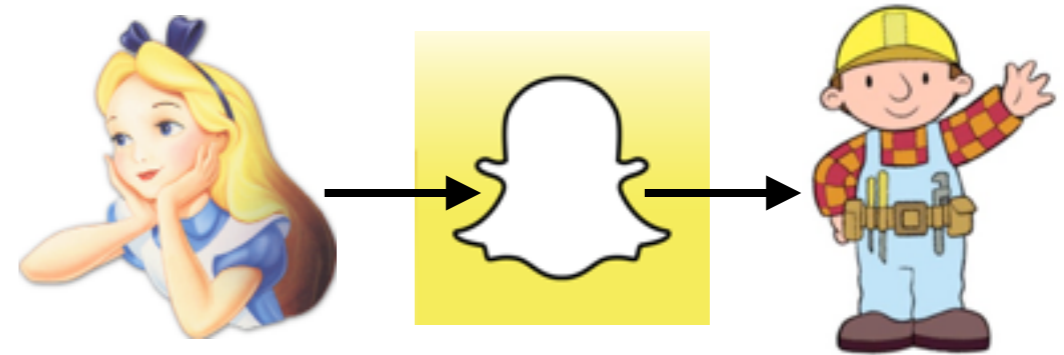
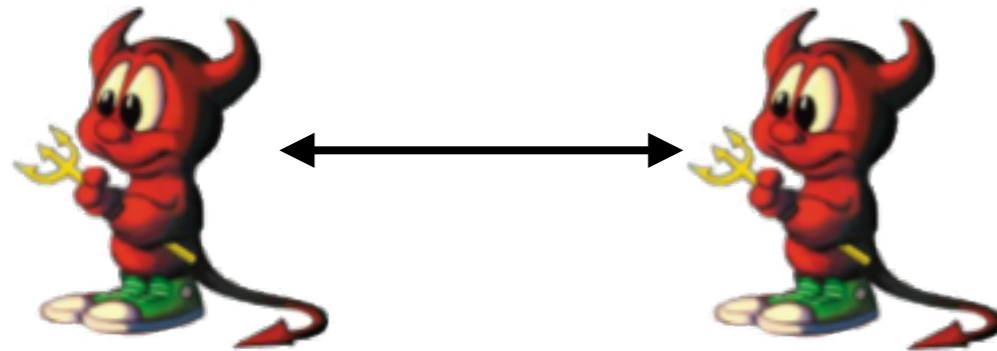
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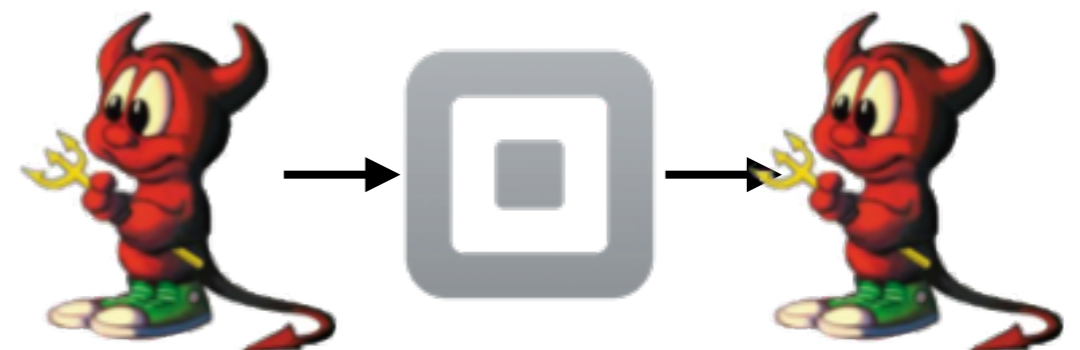
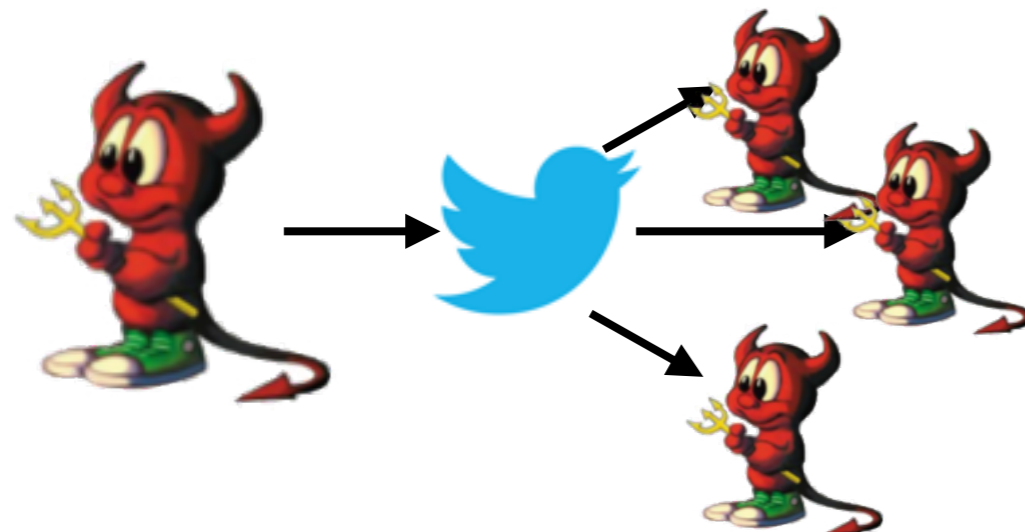
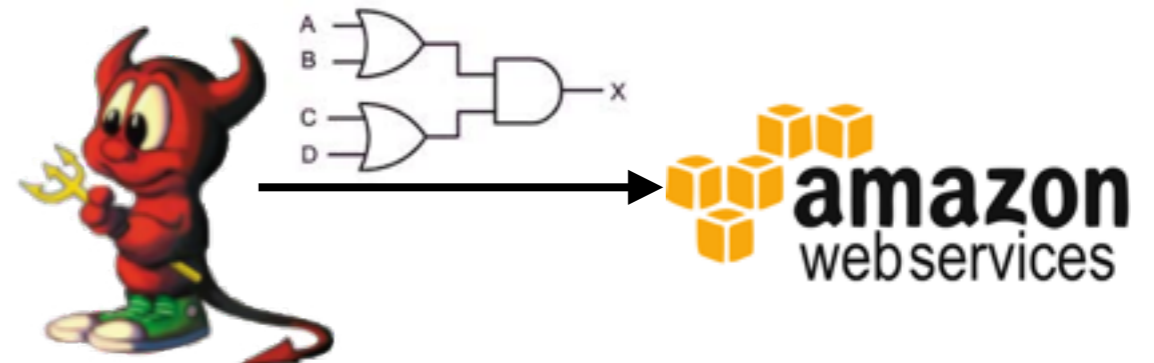
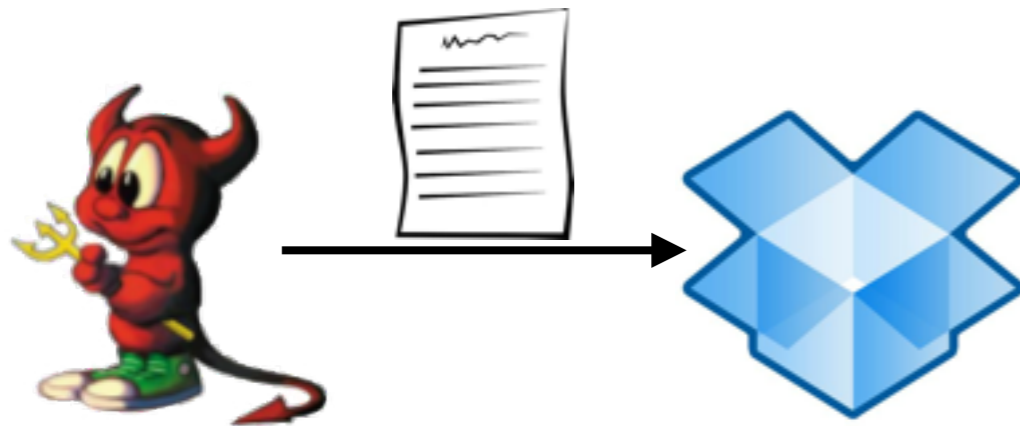
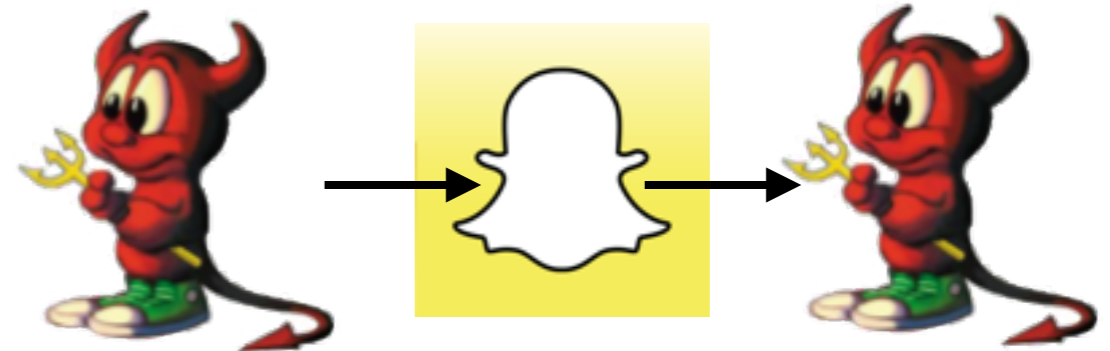
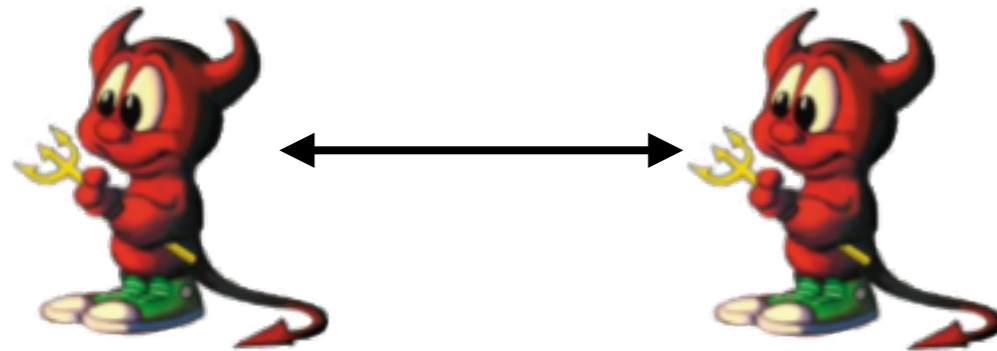
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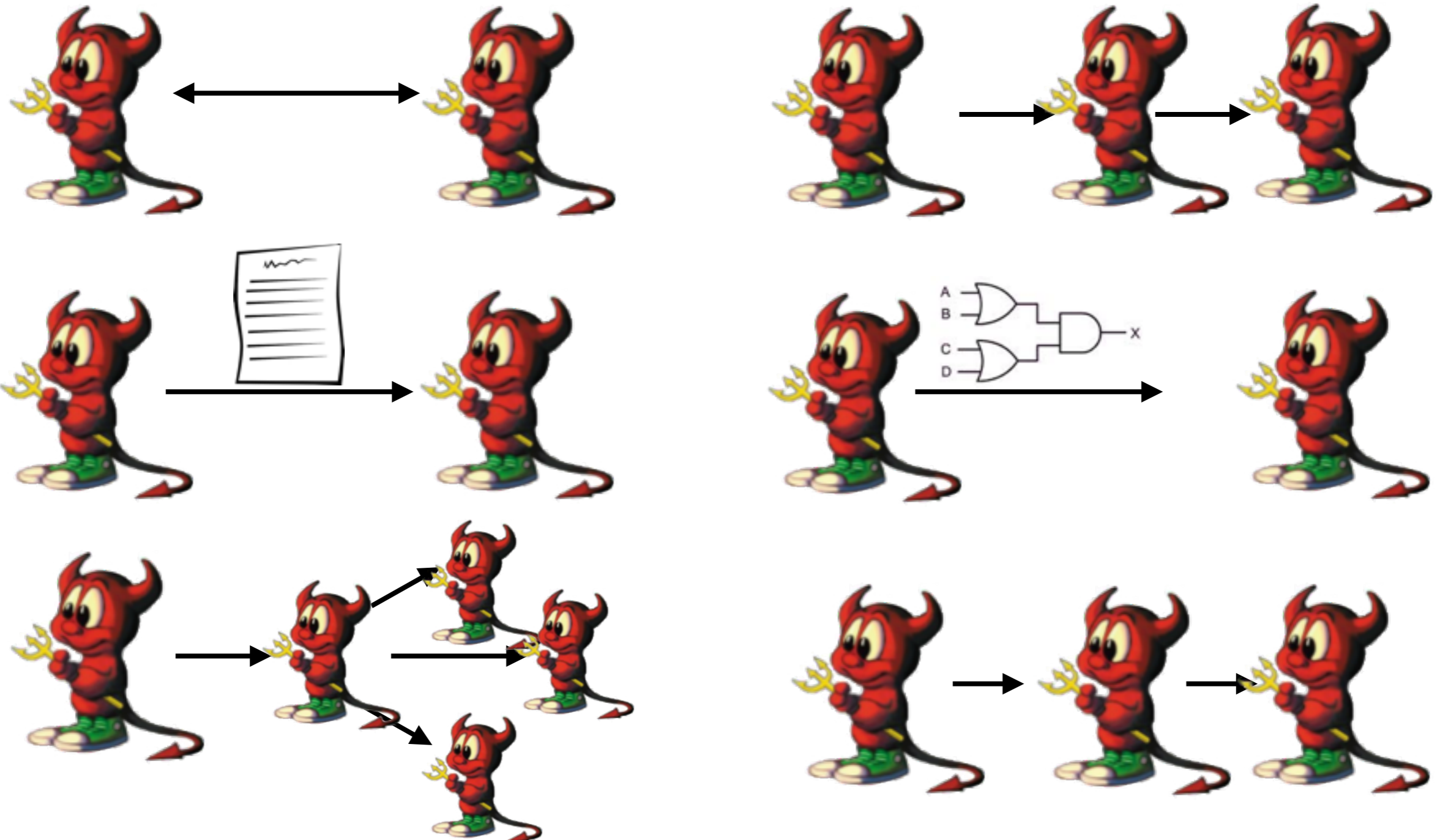
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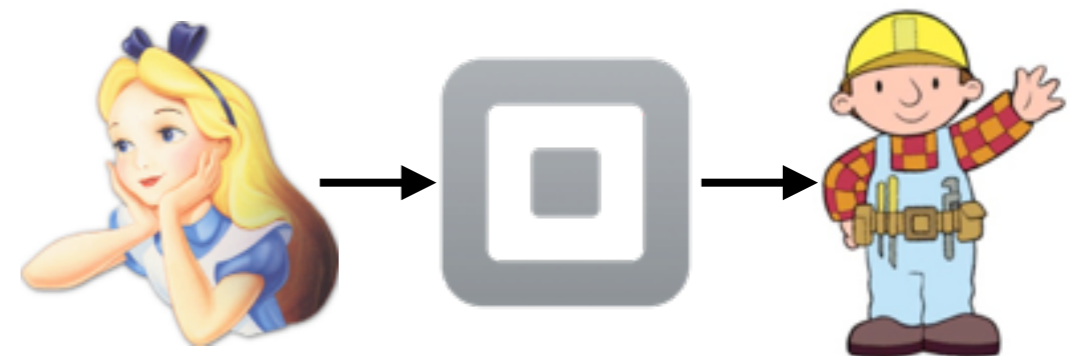
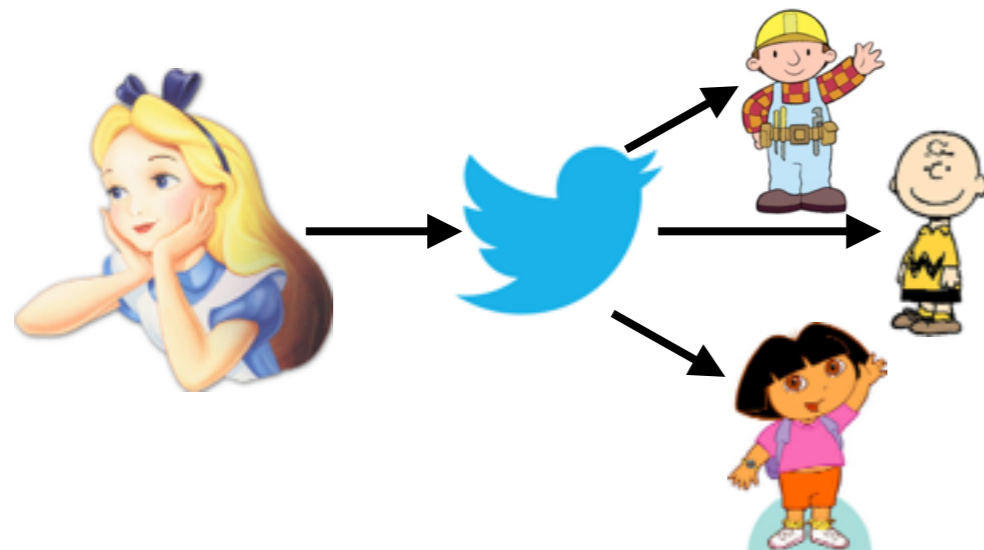
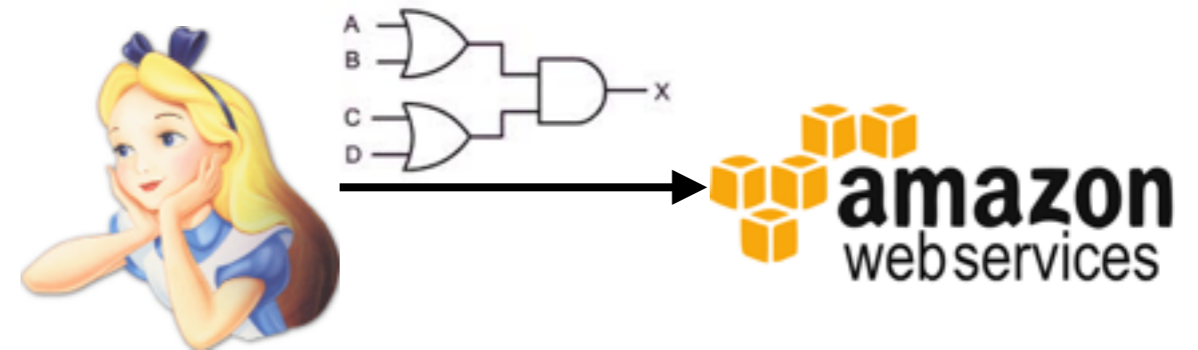
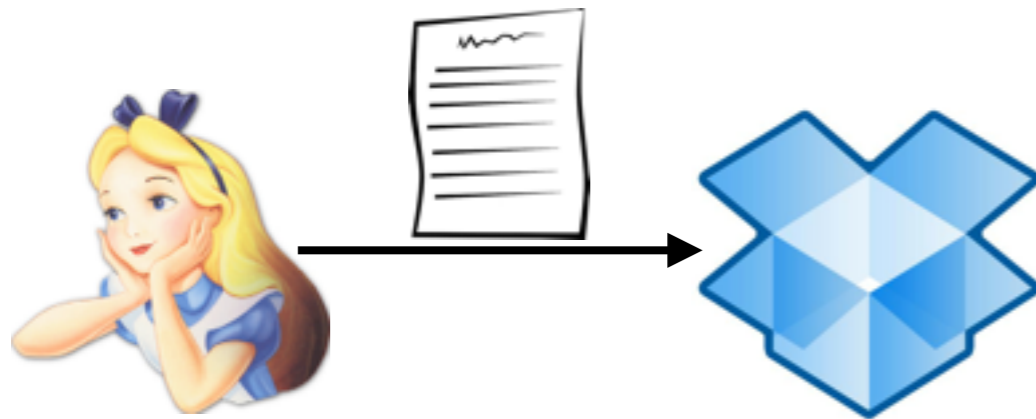
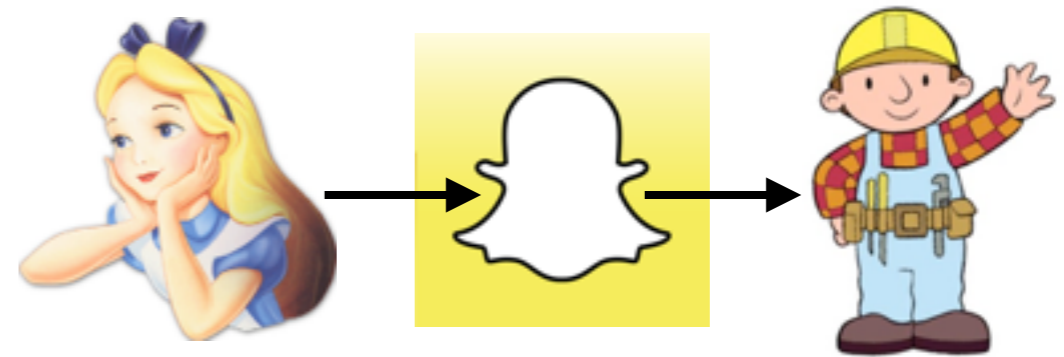
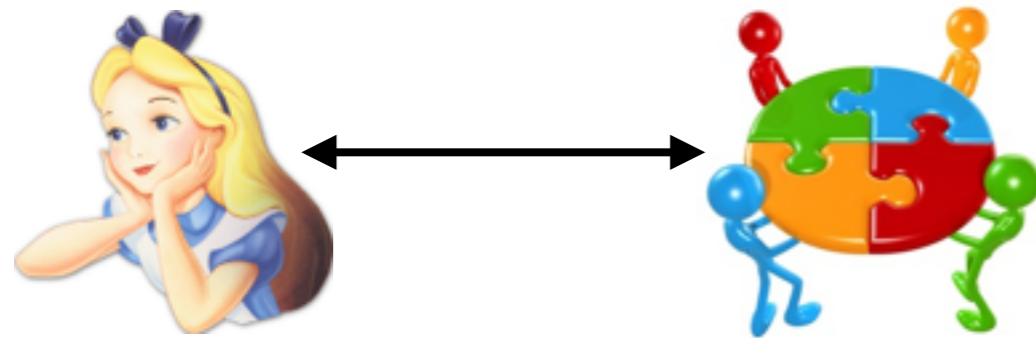
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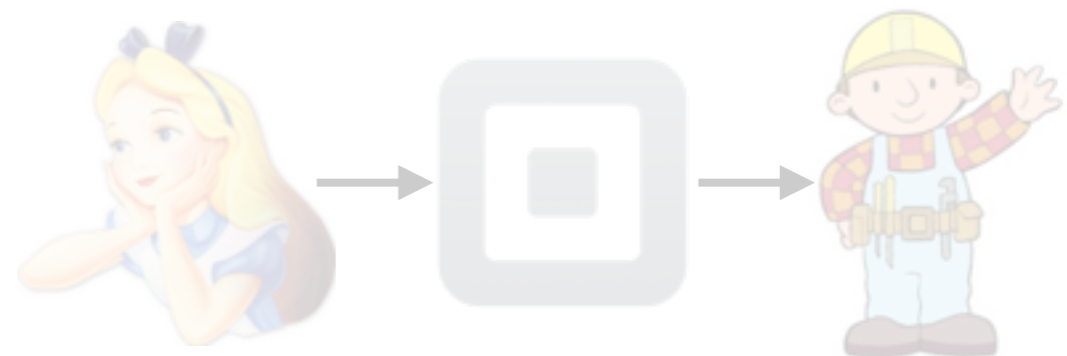
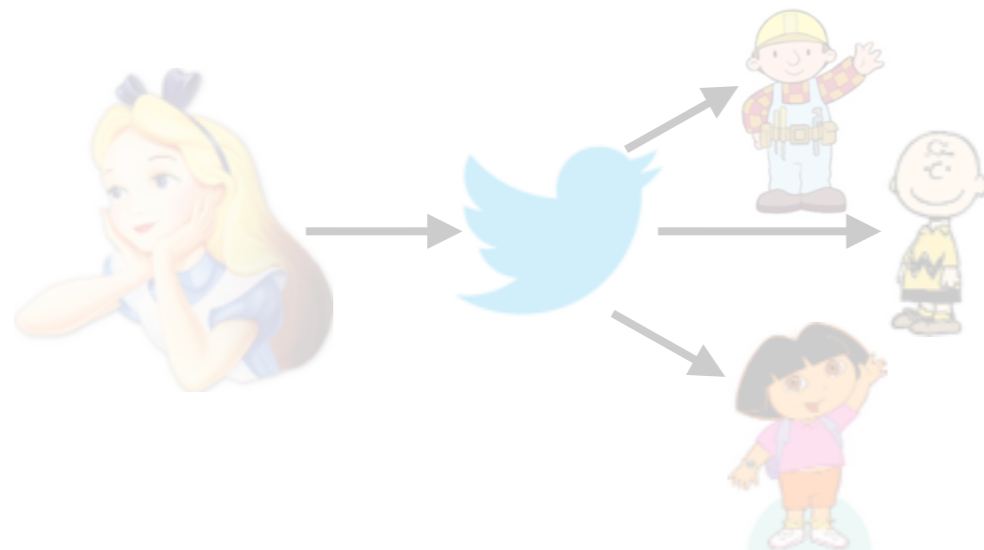
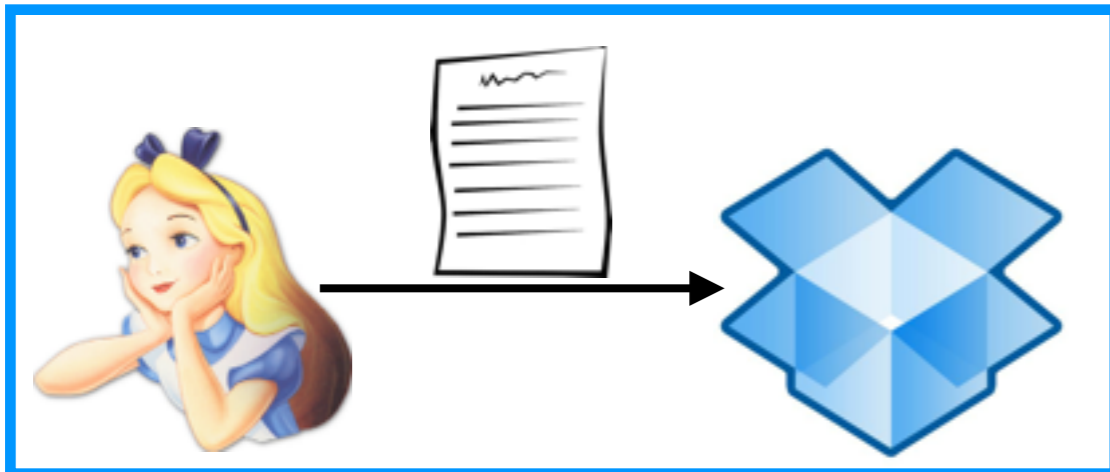
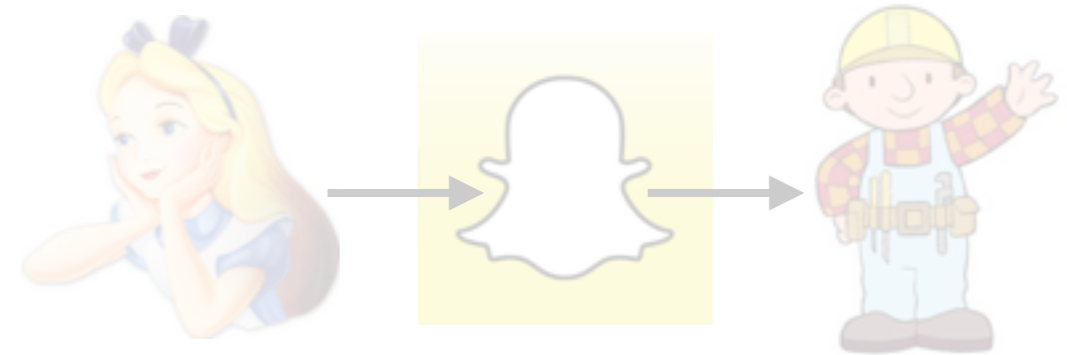
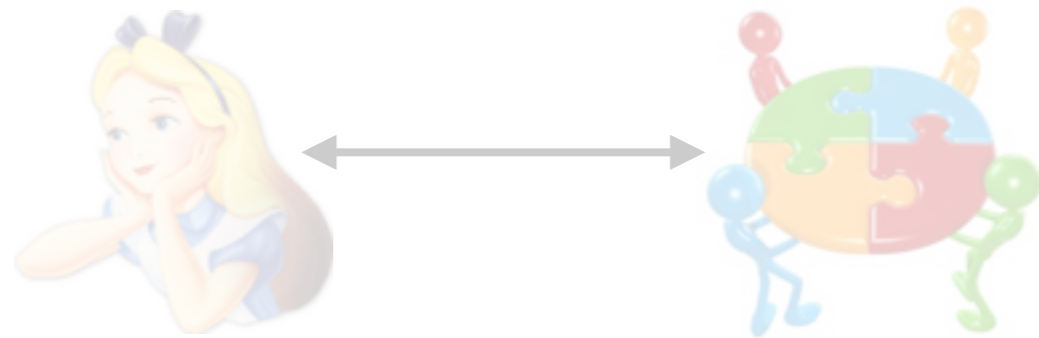
Fast-forward 15 years...

**Problem #2: what are the security goals?**



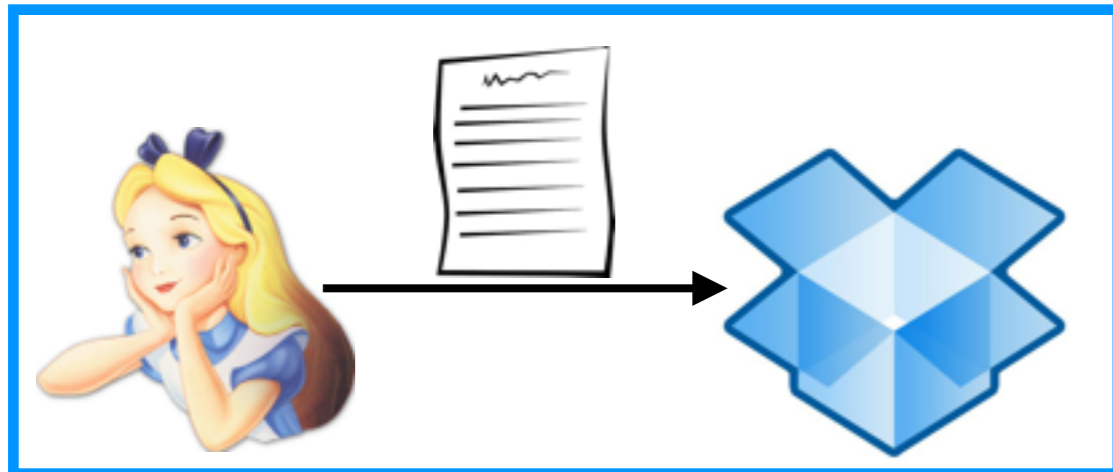
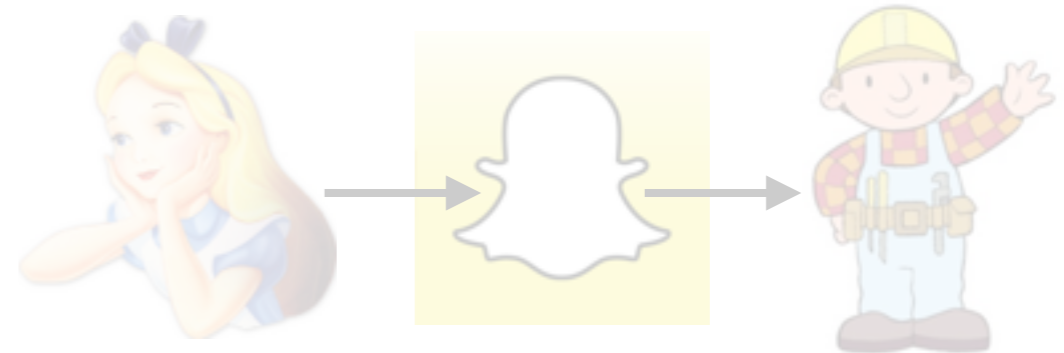
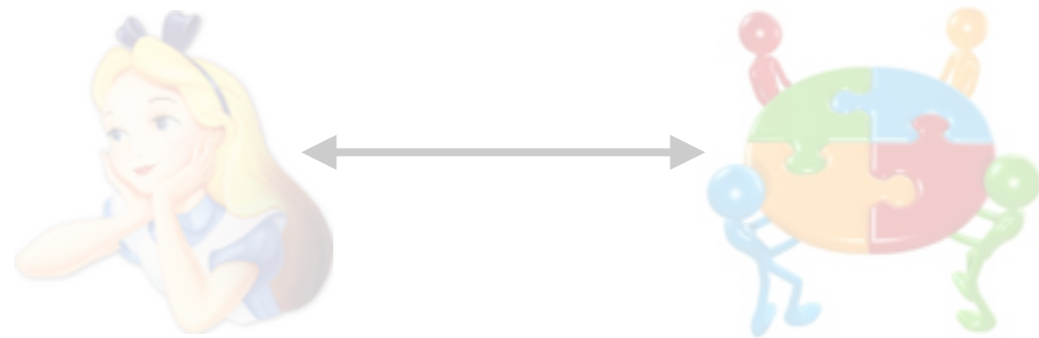
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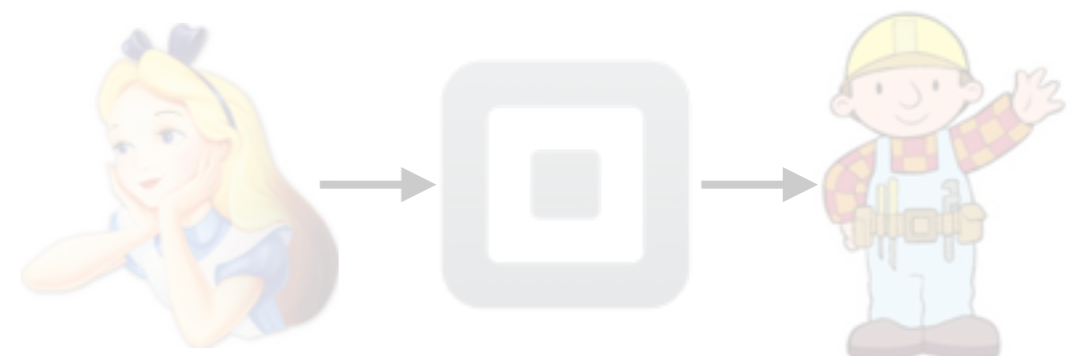
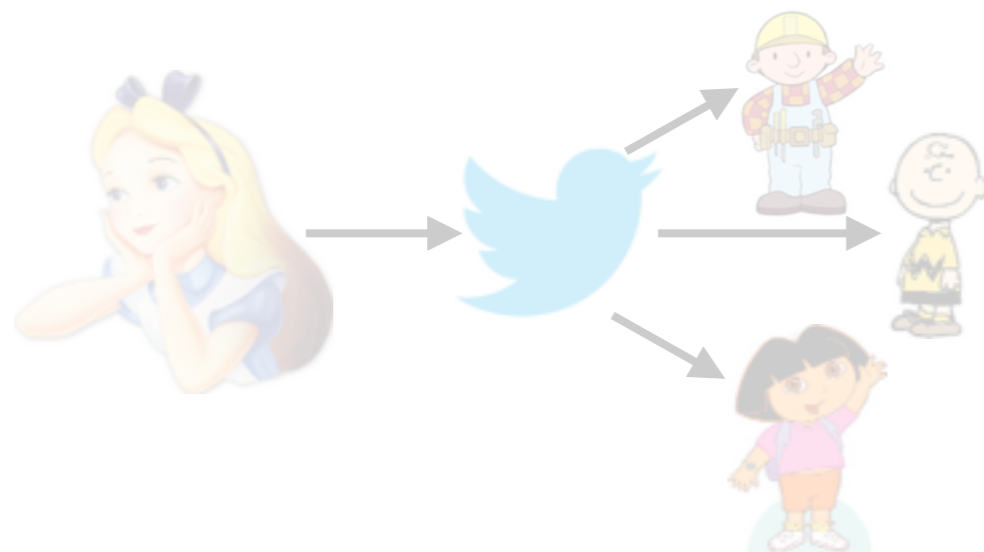


Fast-forward 15 years...

## Problem #2: **what are the security goals?**



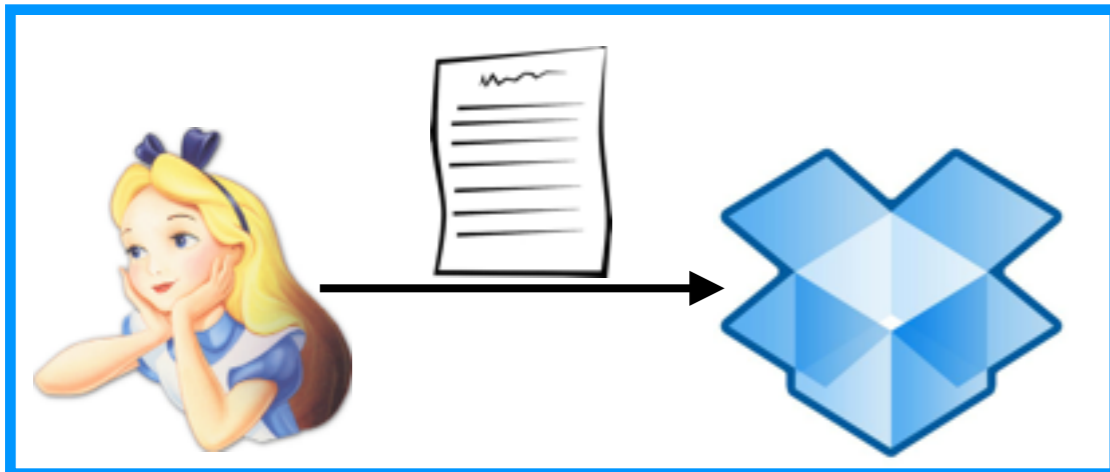
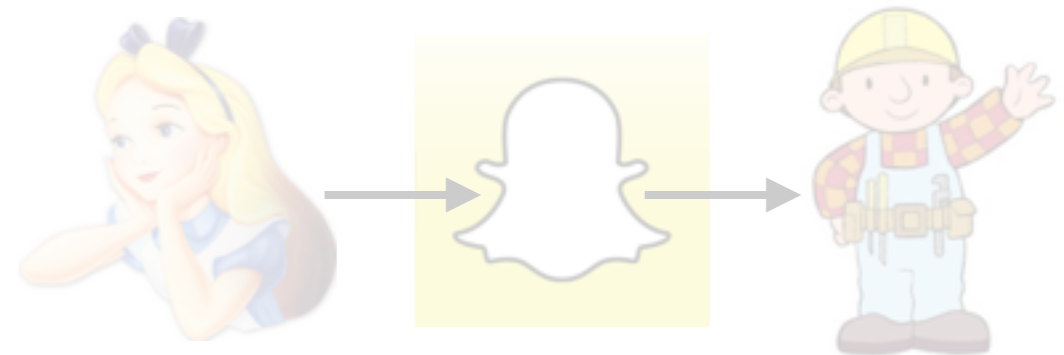
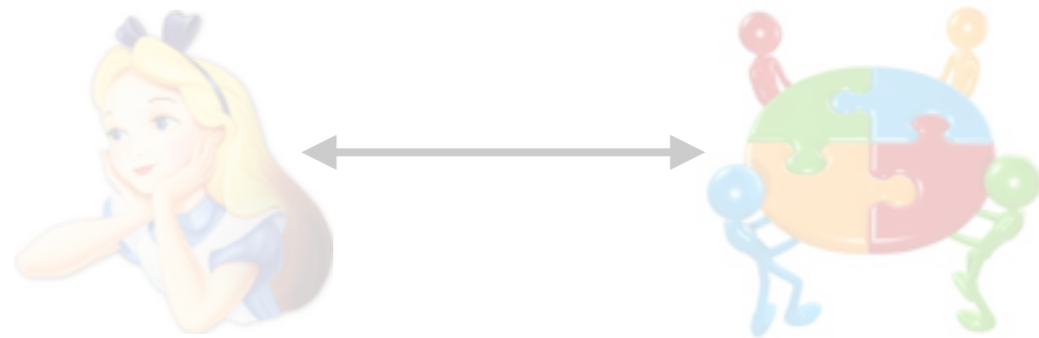
- can Bob retrieve Alice's files?



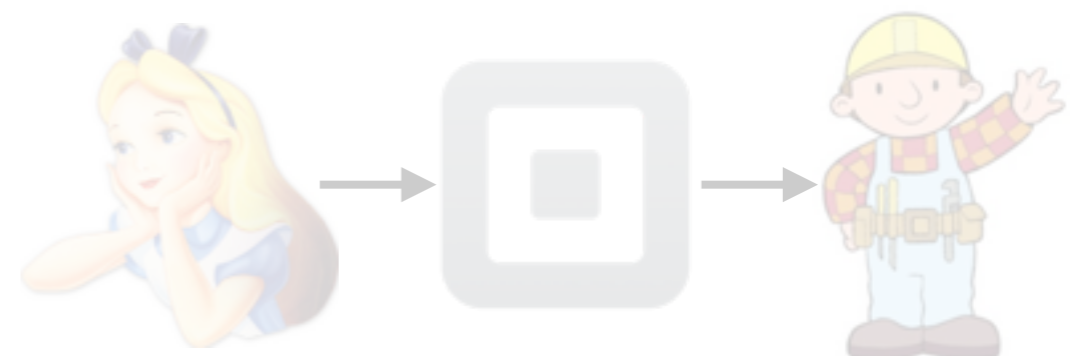
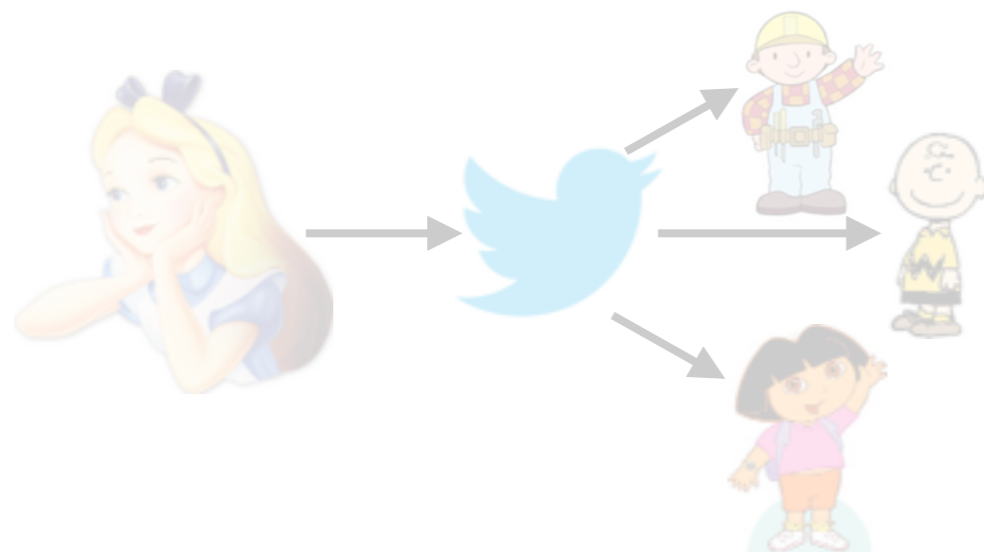


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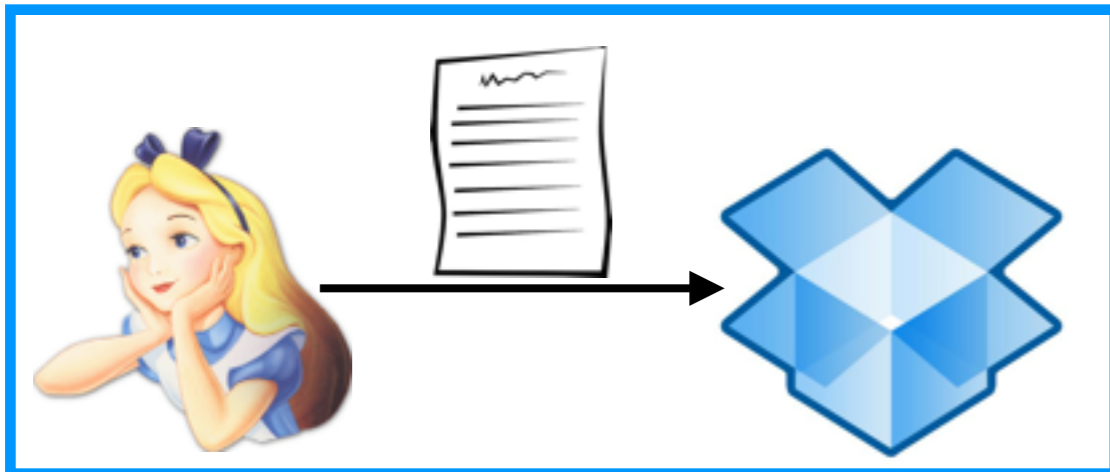
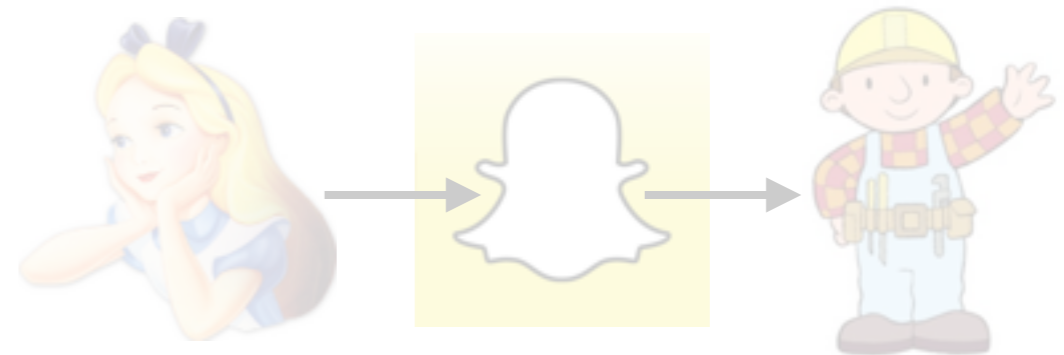
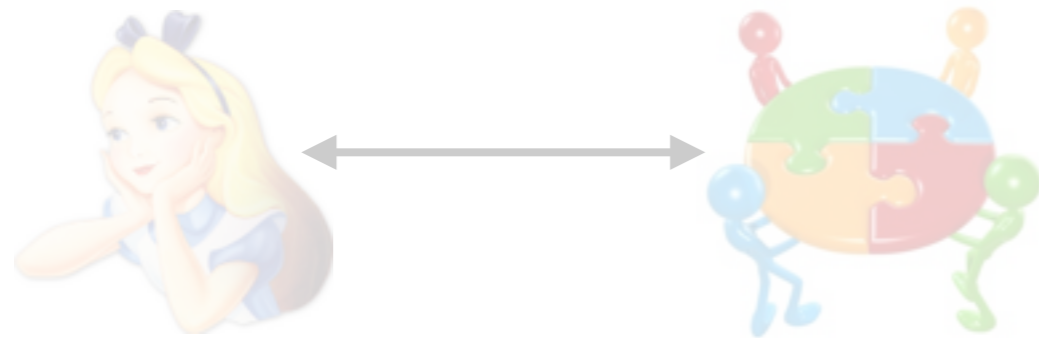


- can Bob retrieve Alice's files?
- can Dropbox read Alice's files?

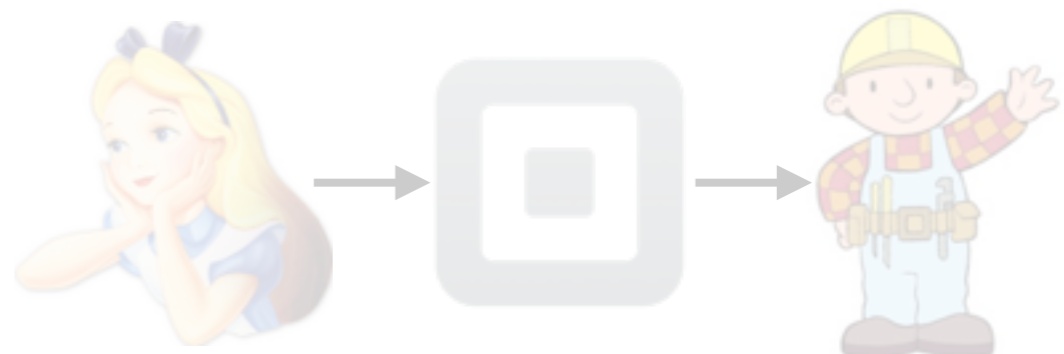
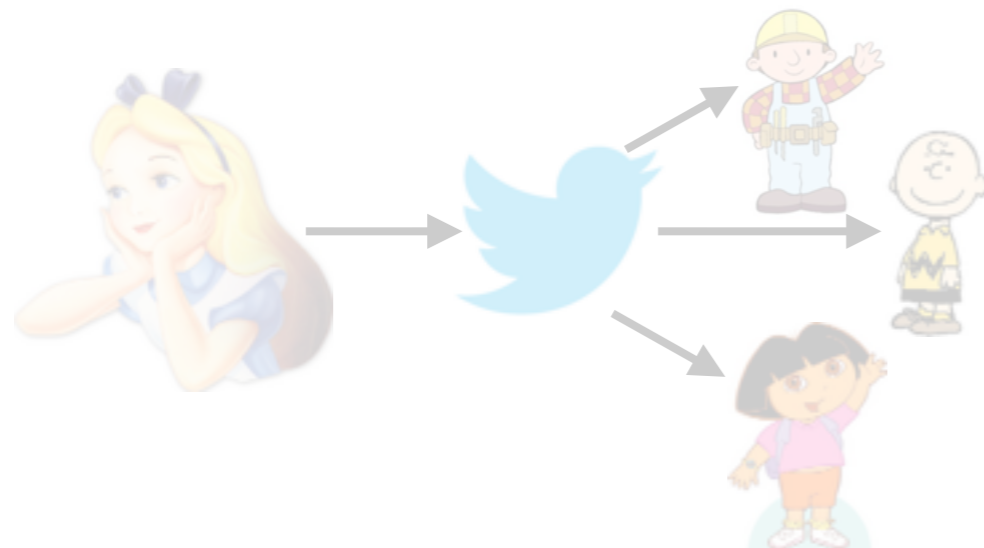


Fast-forward 15 years...

## Problem #2: what are the security goals?

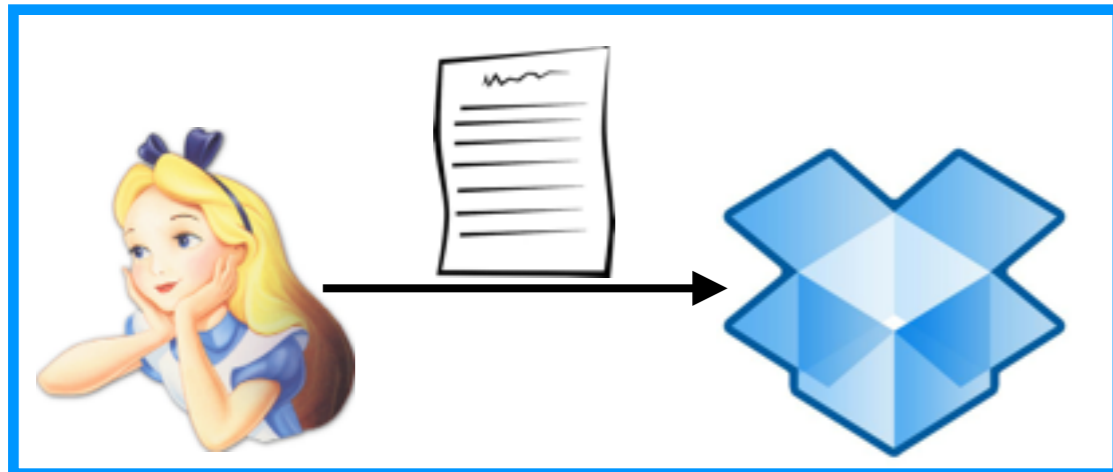
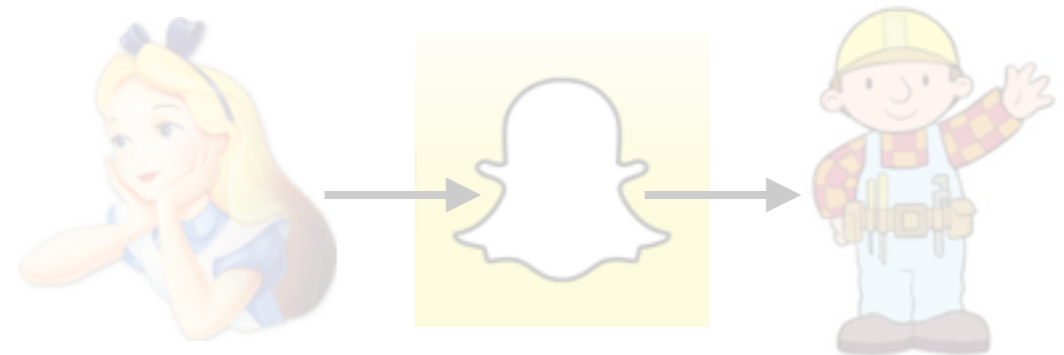
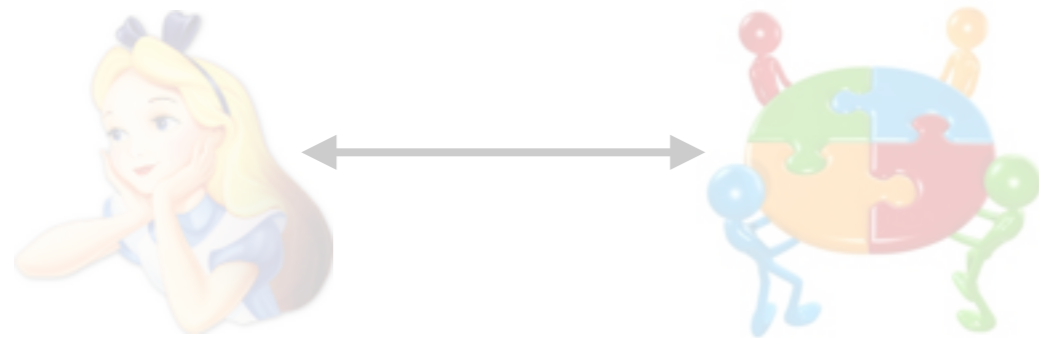


- can Bob retrieve Alice's files?
- can Dropbox read Alice's files?
- did Dropbox delete Alice's files?

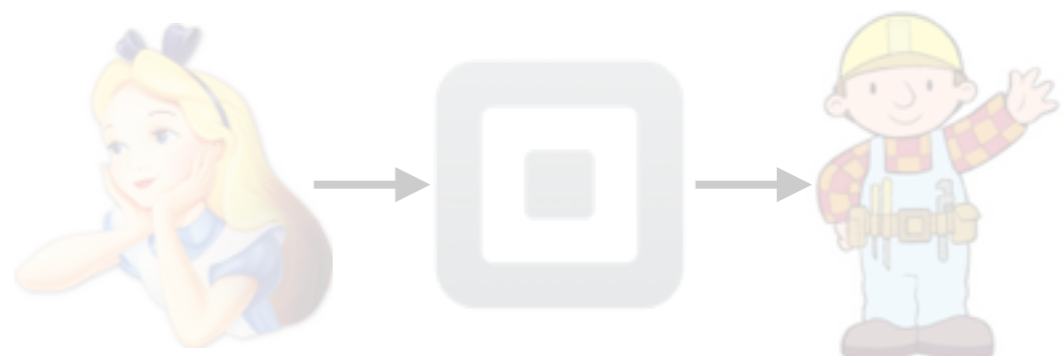
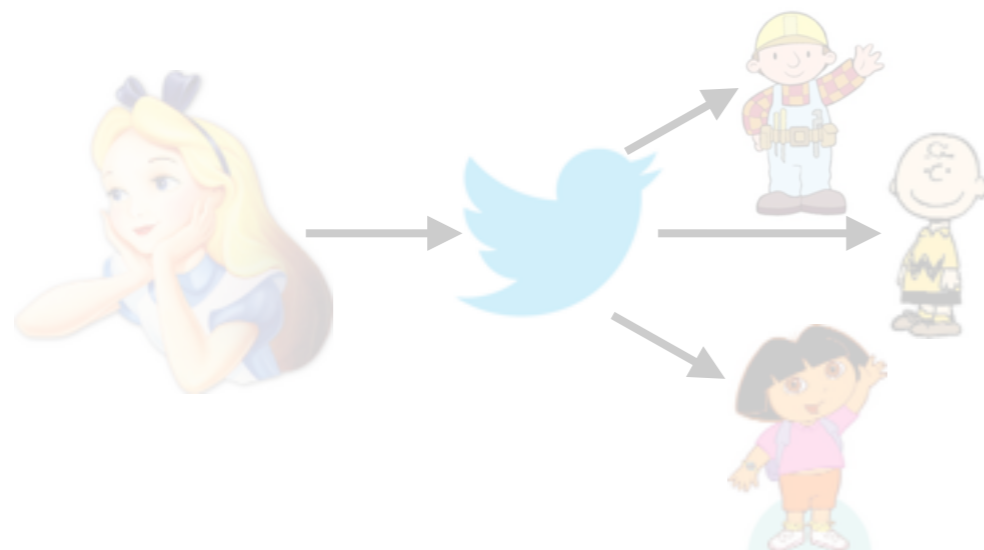


Fast-forward 15 years...

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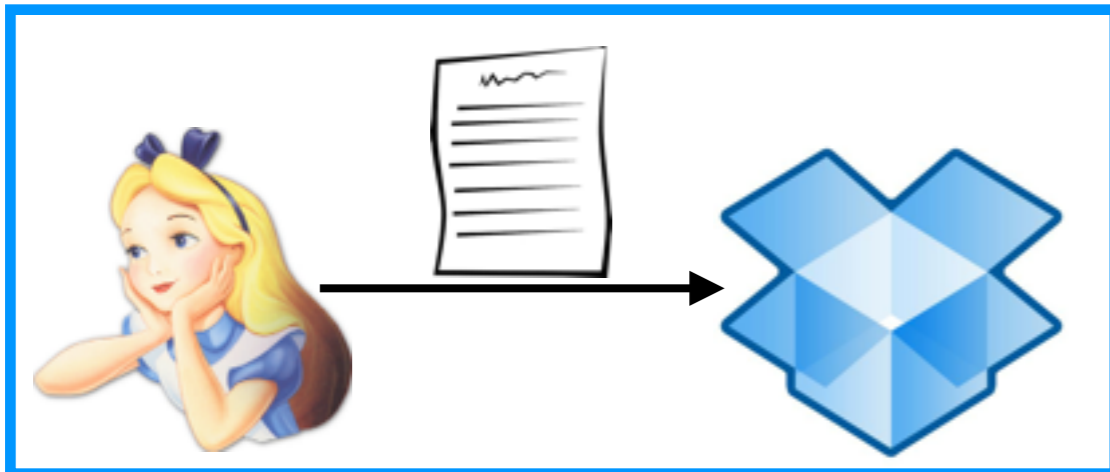
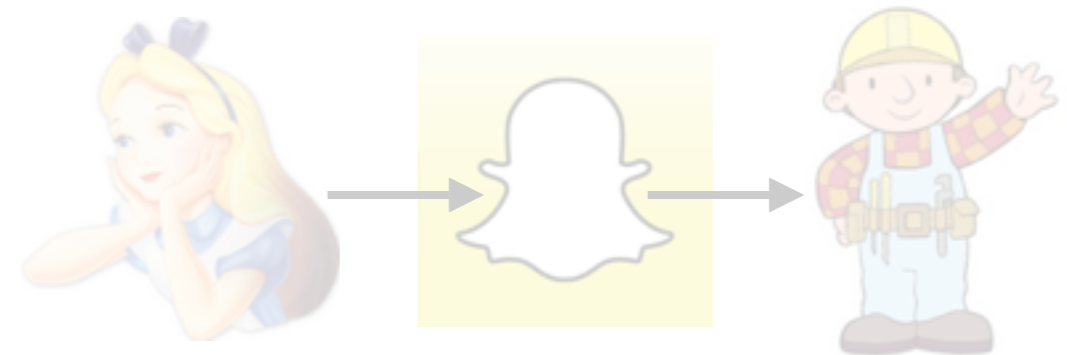
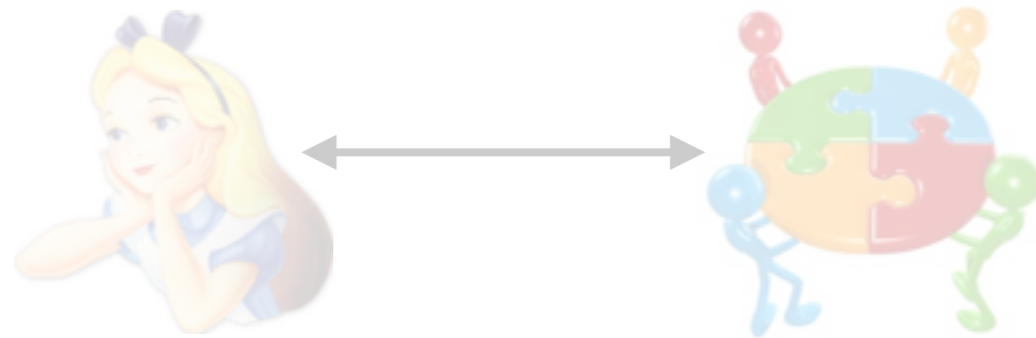


- can Bob retrieve Alice's files?
- can Dropbox read Alice's files?
- did Dropbox delete Alice's files?
- can Dropbox efficiently store files?

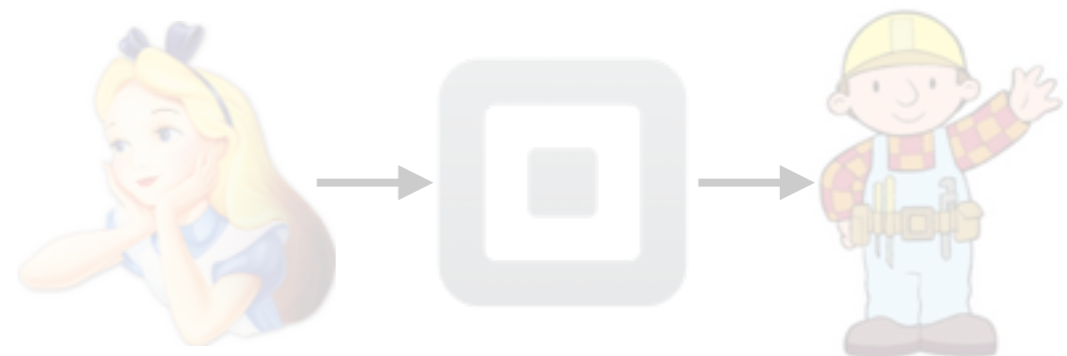
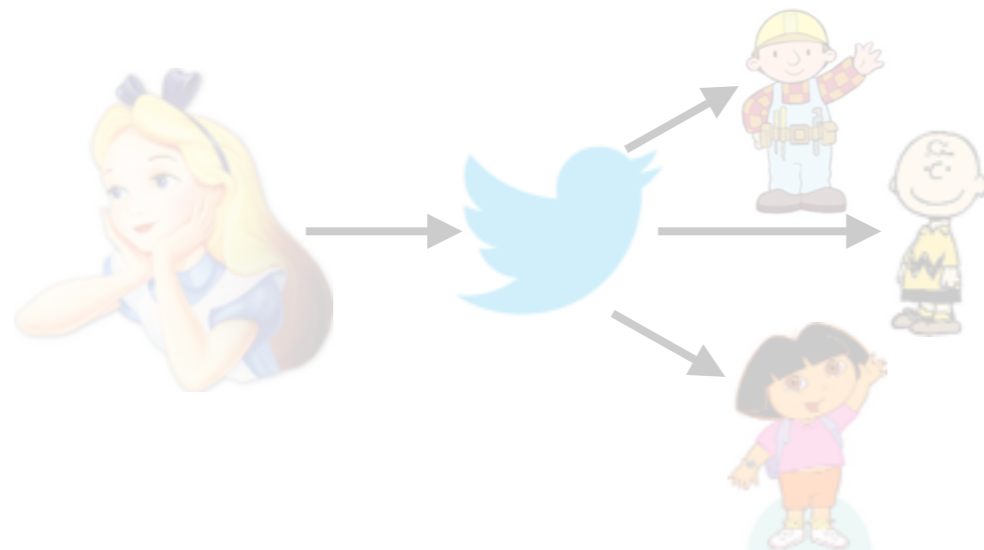


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- can Bob retrieve Alice's files?
- can Dropbox read Alice's files?
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- ?



# A spectrum of solutions

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# A spectrum of solutions

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theory

practice

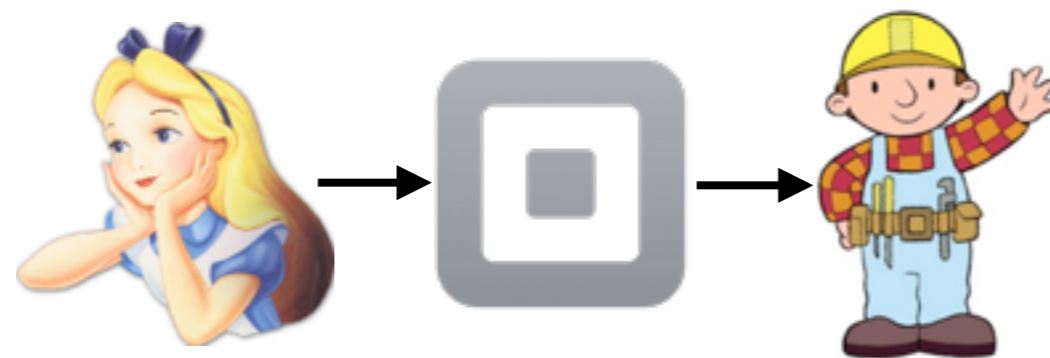
# A spectrum of solutions

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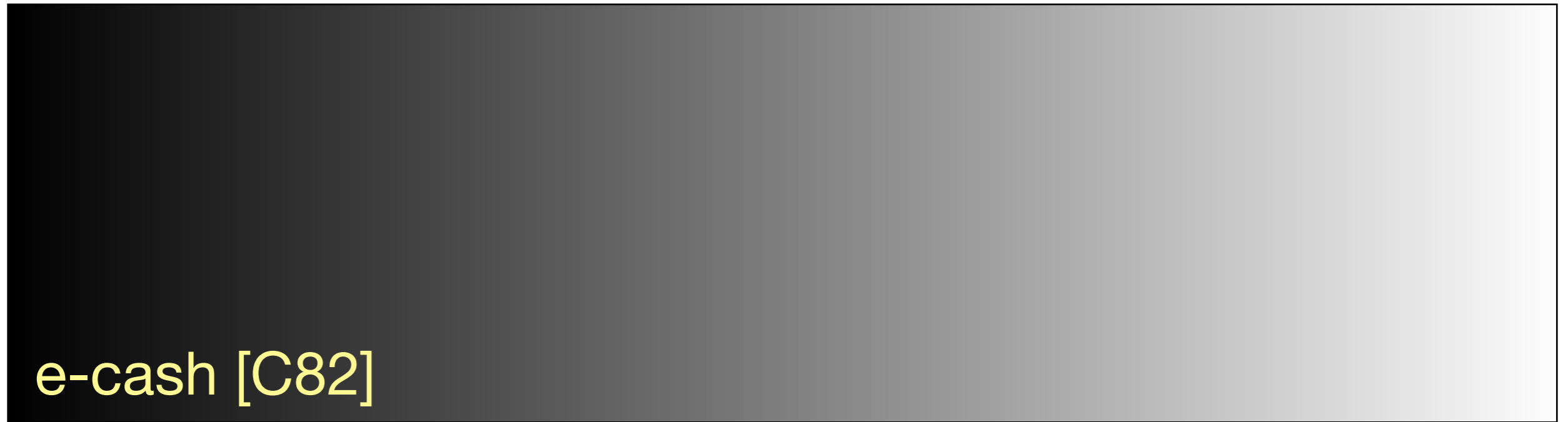
theory

practice



# A spectrum of solutions

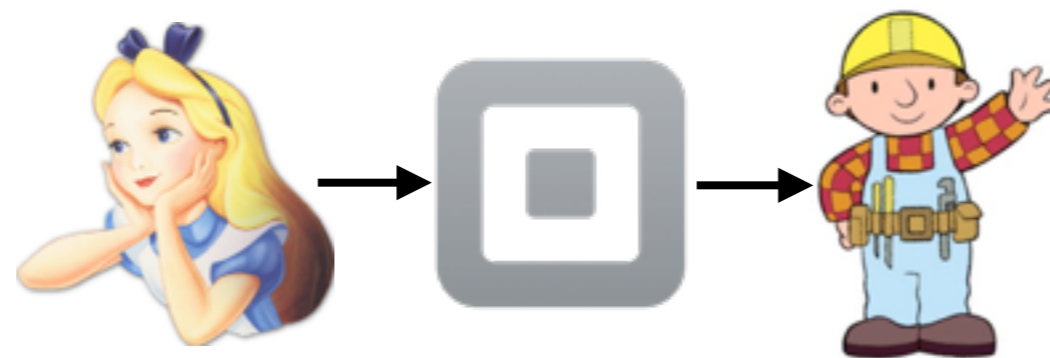
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e-cash [C82]

theory

practice





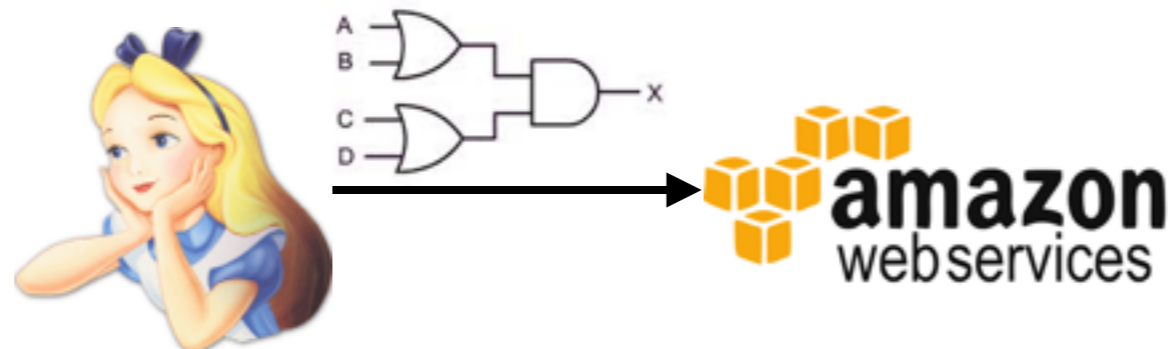
# A spectrum of solutions

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e-cash [C82]

theory

practice



# A spectrum of solutions

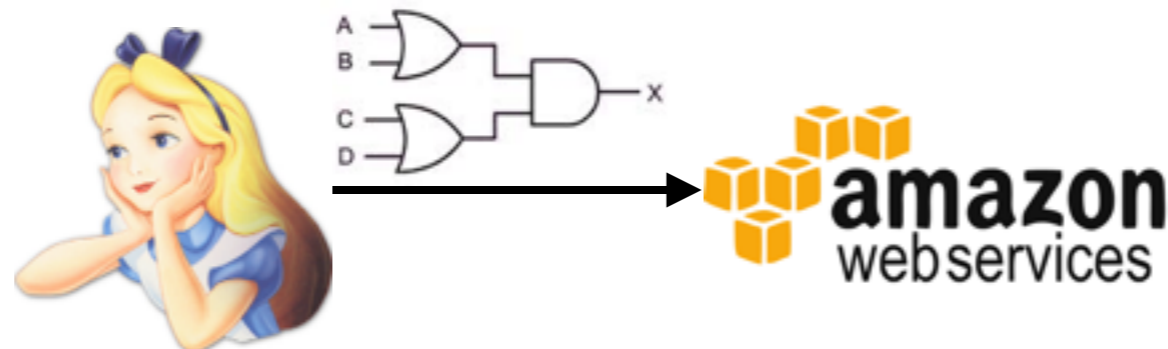
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outsourced comp. [GGP10]

e-cash [C82]

theory

practice



# A spectrum of solutions

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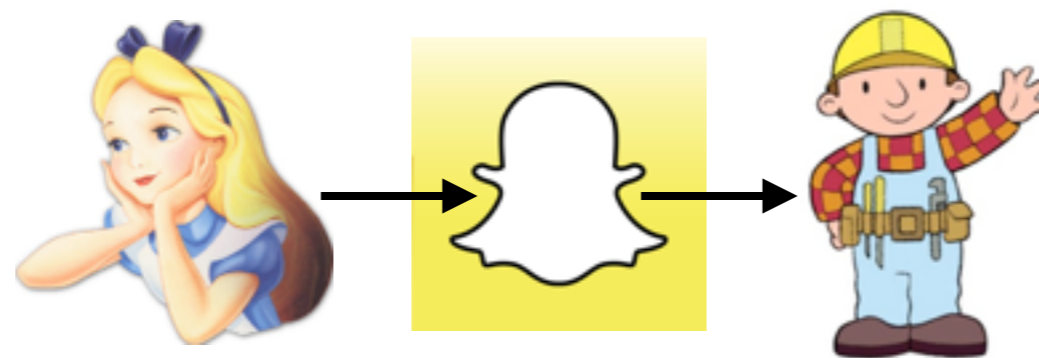
# A spectrum of solutions

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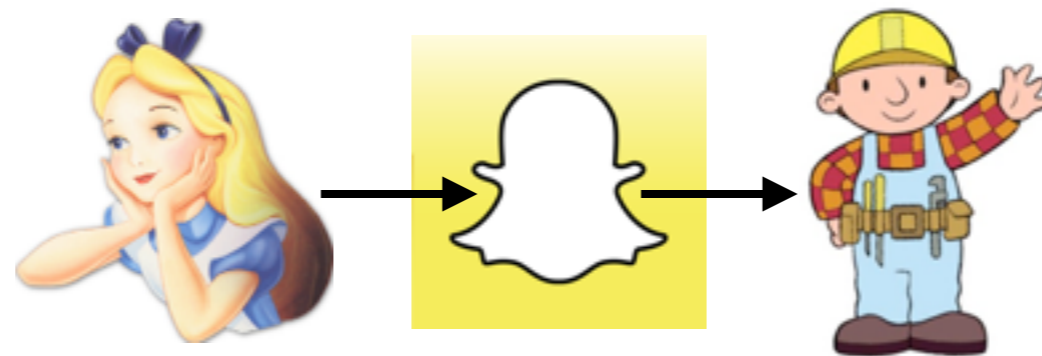
RKA [B93,K93]  
MPC [Y82] FHE [G09]  
outsourced comp. [GGP10]  
e-cash [C82] ORAM [G096]

theory

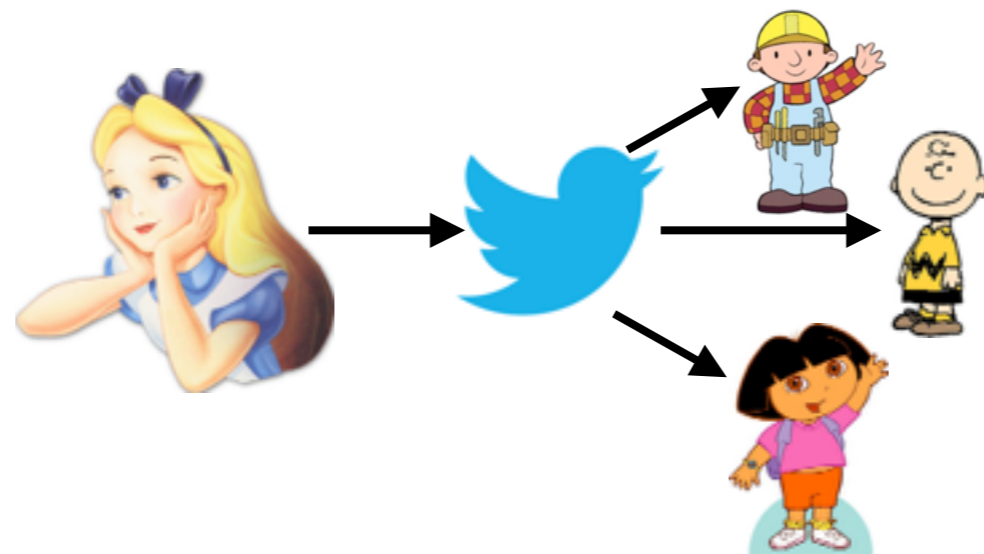
practice



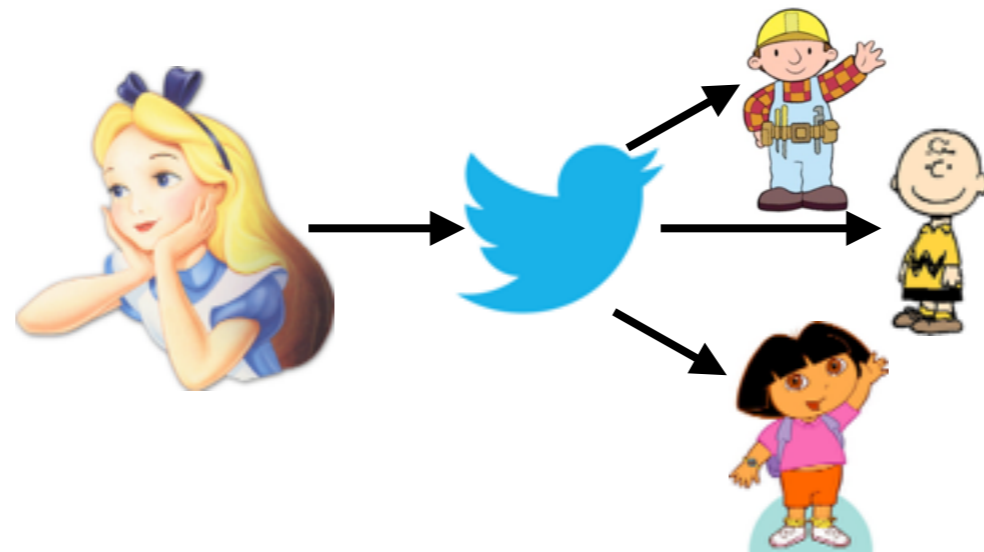
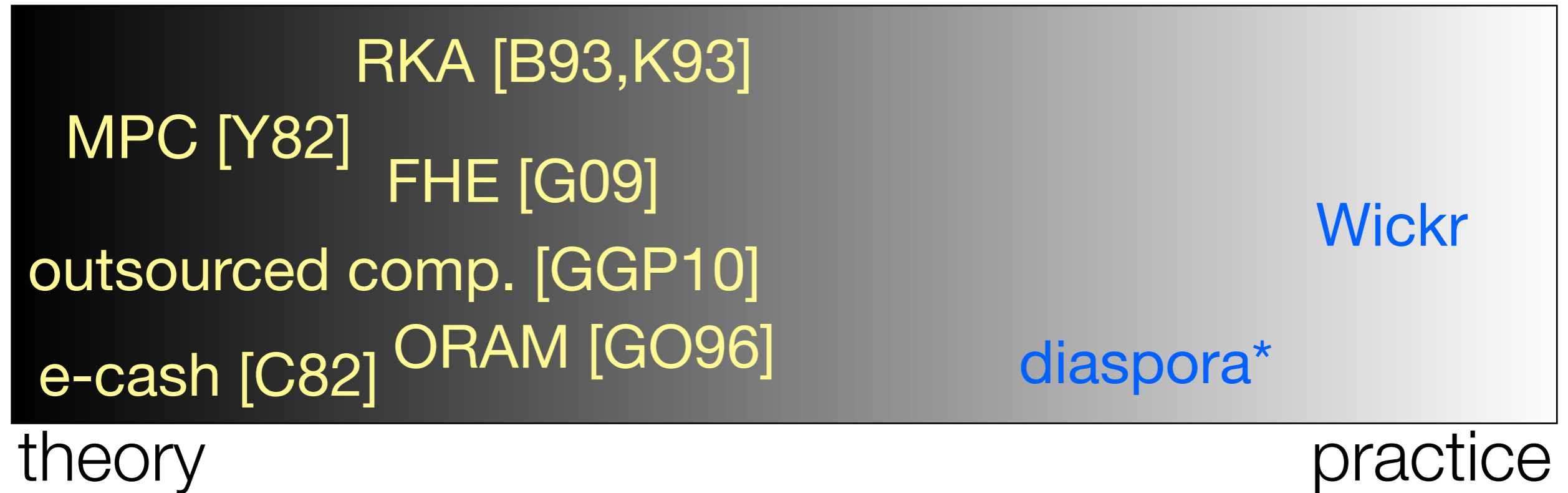
# A spectrum of solutions



# A spectrum of solutions

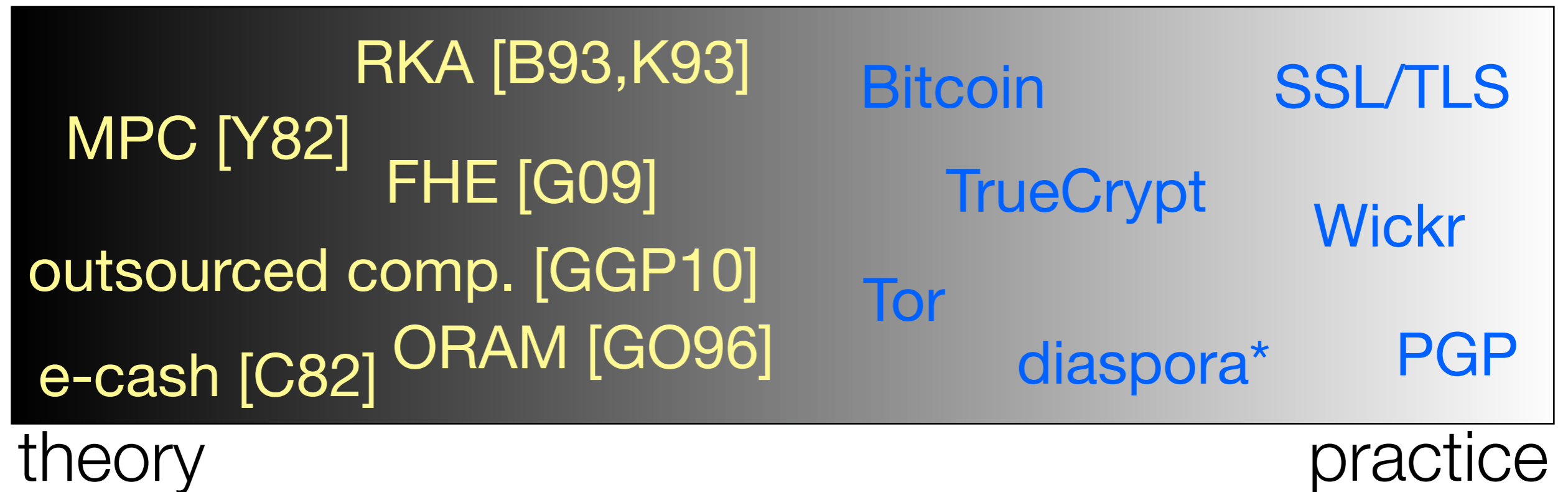


# A spectrum of solutions



# A spectrum of solutions

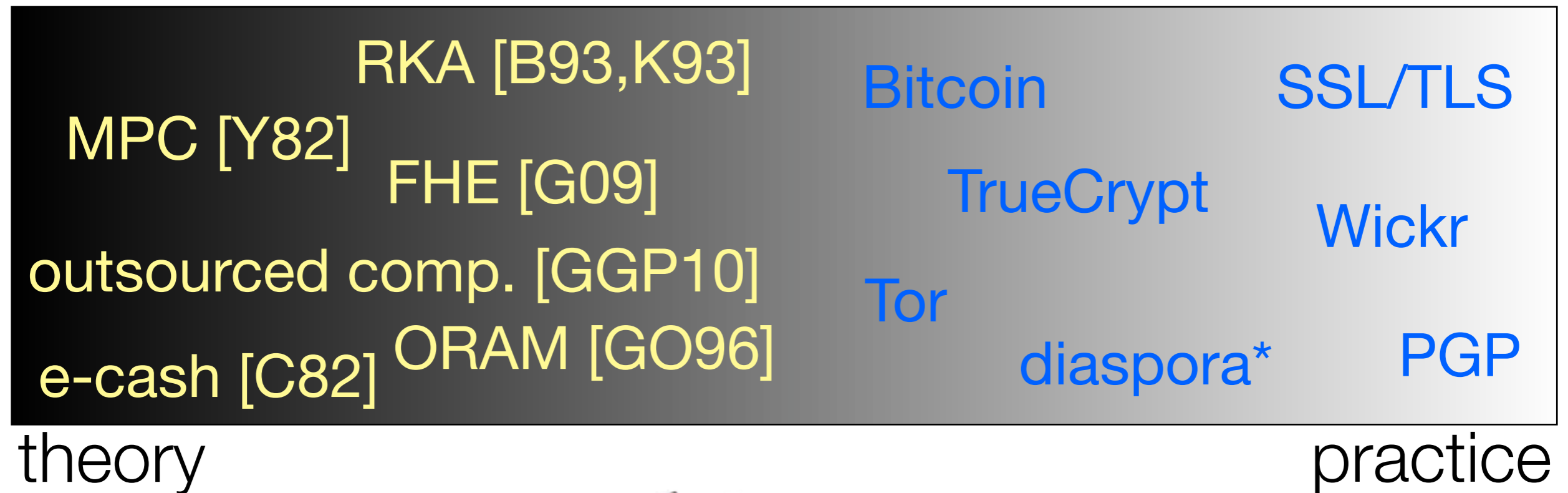
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# A spectrum of solutions

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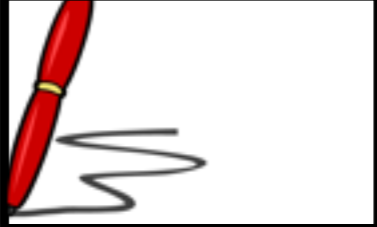
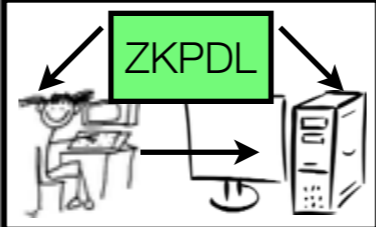

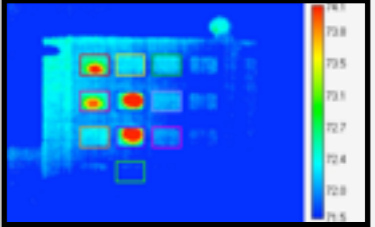
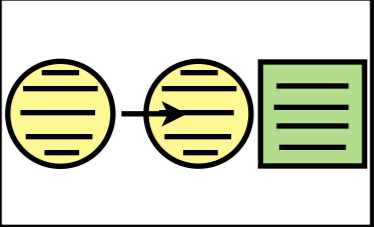
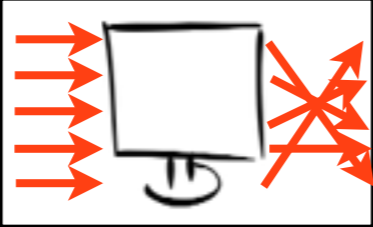


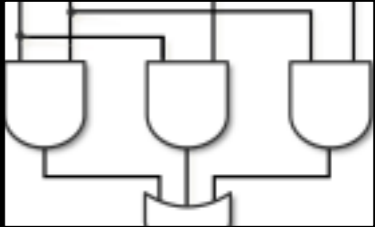


# A spectrum of solutions


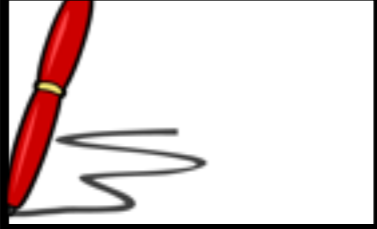
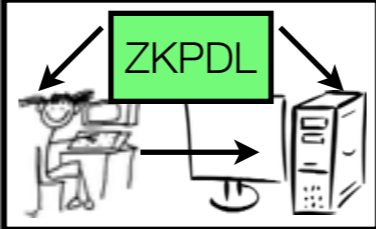

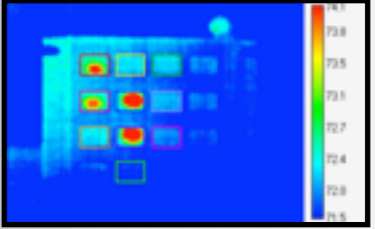
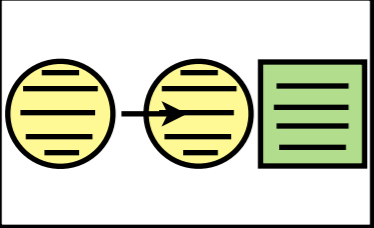
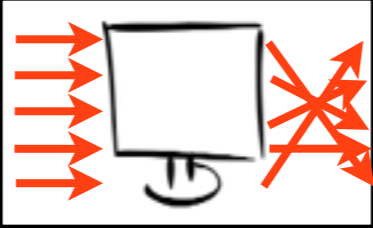


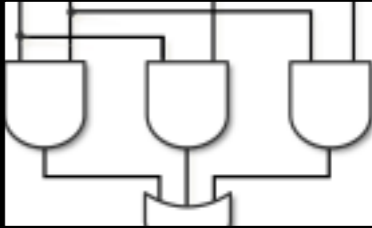
	RKA [B93,K93]	Bitcoin	SSL/TLS
MPC [Y82]	FHE [G09]	TrueCrypt	Wickr
outsourced comp. [GGP10]		Tor	
e-cash [C82]	ORAM [GO96]	diaspora*	PGP
theory			practice



# My research

				
[MSF10,LM13]	[BMT14]	[MEKHL10]	[MMCS11]	[MMS11]
				
[CM14]	[CKLM12,13a,13b]	[CMZ13]	[MP+13,HDM+14]	[OMSK13]

# My research

 [MSF10,LM13]	 [BMT14]	 [MEKHL10]	 [MMCS11]	 [MMS11]
 [CM14]	 [CKLM12,13a,13b]	 [CMZ13]	 [MP+13,HDM+14]	 [OMSK13]


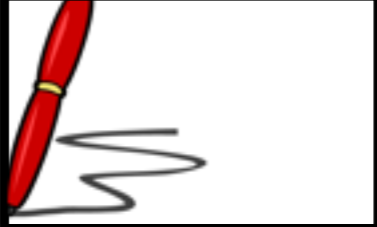
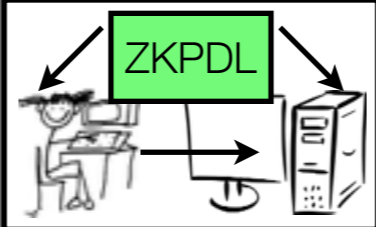

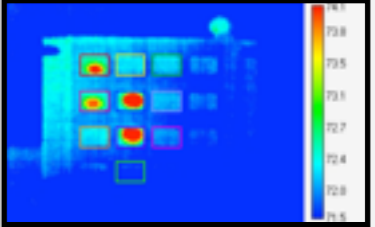
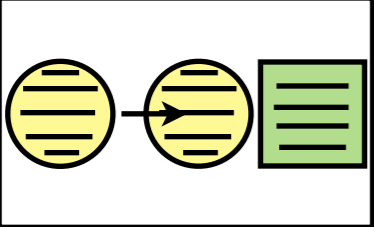
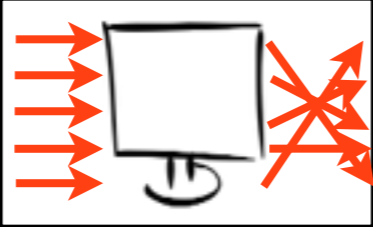


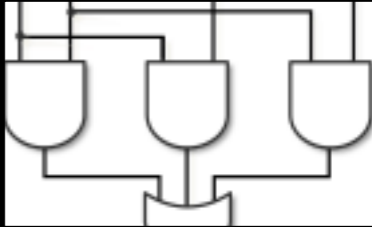



RKA




Bitcoin

# My research



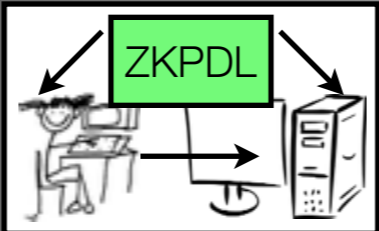

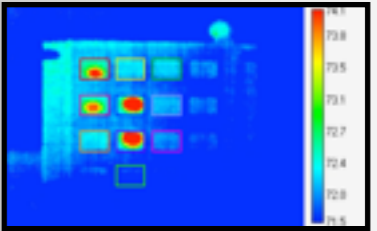
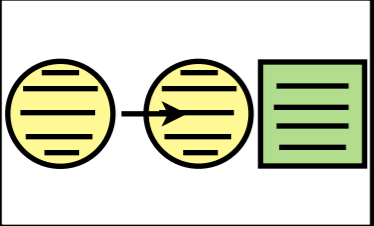
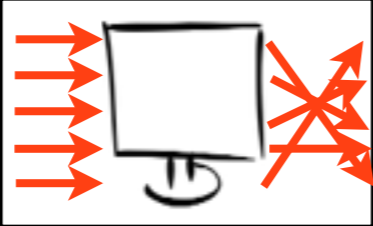


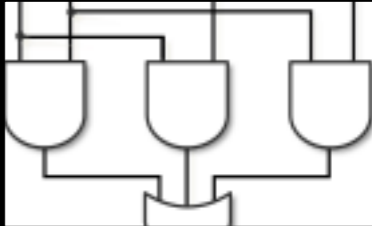
 [MSF10,LM13]	 [BMT14]	 [MEKHL10]	 [MMCS11]	 [MMS11]
 [CM14]	 [CKLM12,13a,13b]	 [CMZ13]	 [MP+13,HDM+14]	 [OMSK13]

  
RKA



  
Bitcoin

# My research

 [MSF10,LM13]	 [BMT14]	 [MEKHL10]	 [MMCS11]	 [MMS11]
 [CM14]	 [CKLM12,13a,13b]	 [CMZ13]	 [MP+13,HDM+14]	 [OMSK13]

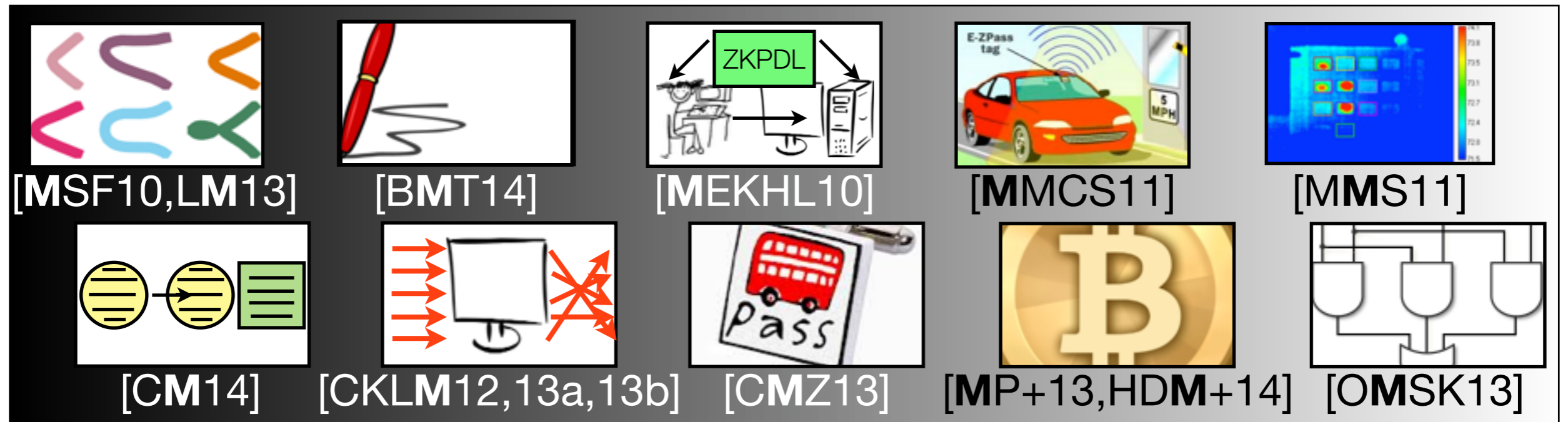


RKA



Bitcoin

# My research



# Digital signatures are everywhere

---



# Digital signatures are everywhere

---



The server's host key is not cached in the registry. You have no guarantee that the server is the computer you think it is.

The server's rsa2 key fingerprint is:

ssh-rsa 1024 0a:27:d5:4f:00:9c:d1:a3:ff:ad:5c:cd:b3:7c:83:42

If you trust this host, hit Yes to add the key to PuTTY's cache and carry on connecting.

If you want to carry on connecting just once, without adding the key to the cache, hit No.

If you do not trust this host, hit Cancel to abandon the connection.

# Digital signatures are everywhere

---

```
17ijmE4nZstNnevbHLawnhCW9nZ 0.37 BTC
1cTHK2B4D3qg4kj44wxfeQCTE6N 3.11 BTC
1ZhKkzRLLfpNGNHf8qDDH7uRZta 0.20 BTC
1QJ3FK8grGXKEPqVUC1tx6G5Hw 5.16 BTC
```



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# Digital signatures are everywhere

```
-----BEGIN PGP SIGNATURE-----  
Version: GnuPG v1.4.11 (GNU/Linux)  
Comment: Using GnuPG with Thunderbird - http://www.enigmail.net/  
  
iQEcBAEBAgAGBQJSbpK5AAoJEKAI9HCTr8nwh8slAIIvIE5OmpHbzpcatKMdUL9q  
0ehAanFyH9WEVxHuv/DAW9Mq35hsYRJL+2wDBUbyeCtClhjpgfW0jmgYc0MevQva  
w0MUOleYwBOVkdM6I6E5KN+fRC5qqjeLZvFO2yVrEdItCZeRvNzKm1MREbKnSBPd  
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WWvIrYWM21p8eShdcoukW3aar3ovNqQ6B/8xzLeblAcruvll3ejE2xAR20Btm50=  
=jT/5  
-----END PGP SIGNATURE-----
```

```
17ijmE4nZstNnevbHLawnhCW9nZ 0.37 BTC  
1cTHK2B4D3qg4kj44wxfeQCTE6N 3.11 BTC  
1ZhKkzRLLfpNGNHf8qDDH7uRZta 0.20 BTC  
1QJ3FK8grGXKEPqVUC1tx6G5Hw 5.16 BTC
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# Digital signatures are everywhere


Signature Algorithm	SHA-1 with RSA Encryption ( 1 2 840 113549 1 1 5 )
Parameters	none
Not Valid Before	Wednesday, July 20, 2011 5:00:00 PM PT
Not Valid After	Thursday, July 18, 2013 4:59:59 PM PT
Public Key Info	
Algorithm	RSA Encryption ( 1 2 840 113549 1 1 1 )
Parameters	none
Public Key	128 bytes : D5 14 57 A0 96 40 9F 84 08 C6 66 8D EE EC E3 03 B2 66 85 AC 5D BB 1C EF 15 93 FD 1F 20 A7 10 49 24 5B 39 D2 60 C8 9A DC C0 CE 40 34 E6 59 95 B6 52 50 FE 08 25 45 57 73 5F 3A ED 5F DF B6 5C 9D 8A 9C 62 FD 0F 61 BE DC F6 87 1D 80 9D 7F 7C 17 13 77 64 3C 47 F3 87 24 1F 60 61 E0 81 11 46 E4 DC 50 5C 39 53 E6 68 3D 86 3C 55 87 C8 BE FC 87 13 D9 5A AA 5D CC 3F 07 C1 74 CD C2 5E 27 16 11
Exponent	65537
Key Size	1024 bits
Key Usage	Encrypt, Verify, Derive
Signature	128 bytes : 84 FB EF B0 38 C7 B4 E6 BB 74 41 34 6C 52 6F 0E F7 7B 67 D4 D7 AD A7 EF 03 36 EF C0 40 DE 80 D3 0A A6 3C C9 C3 9E 31 52 07 EA 0F 44 63 EA 51 C2 D0 CE 9B A1 6D 99 F8 29 39 2C 40 98 67 12 8C A7 BF 43 30 D2 02 63 B3 F8 0C 36 85 50 8F 29 C2 87 CD E6 F0 EA 57 F2 A4 81 0E 94 B0 D8 46 67 2C 20 AE B6 89 64 A6 B0 DA 8E CF D4 09 7F 57 DC 9C 32 05 06 62 B2 08 14 FE 8B EA 11 13 BC F7 3B 7E F5

OK

```
-----BEGIN PGP SIGNATURE-----
Version: GnuPG v1.4.11 (GNU/Linux)
Comment: Using GnuPG with Thunderbird - http://www.enigmail.net/

iQEcBAEBAgAGBQJSbpK5AAoJEKAI9HCTr8nwh8sIAIIVIE5OmpHbzpcatKMdUL9q
0ehAanFyH9WEVxHuv/DAW9Mq35hsYRJL+2wDBUbyeCtClhjpgfW0jmgYc0MevQva
w0MUOleYwBOVkdM6I6E5KN+fRC5qqjeLZvFO2yVrEdItCZeRvNzKm1MREbKnSBPd
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WWvIrYWM21p8eShdcoukW3aar3ovNqQ6B/8xzLeblAcruvll3ejE2xAR20Btm50=
=jT/5
-----END PGP SIGNATURE-----
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17ijmE4nZstNnevbHLawnhCW9nZ 0.37 BTC
1cTHK2B4D3qg4kj44wxfeQCTE6N 3.11 BTC
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1QJ3FK8grGXKEPqVUC1tx6G5Hw 5.16 BTC
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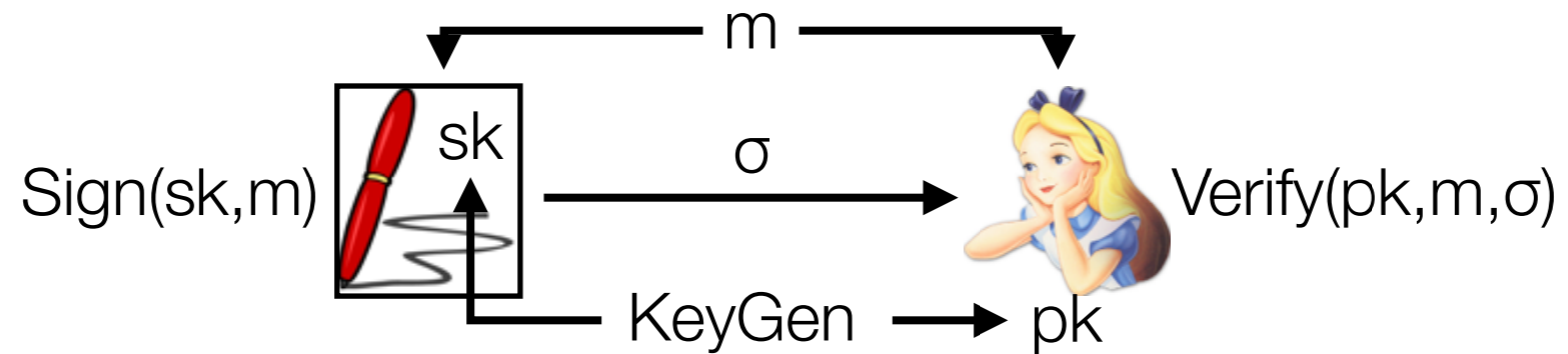
# Practical security of digital signatures

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# Practical security of digital signatures

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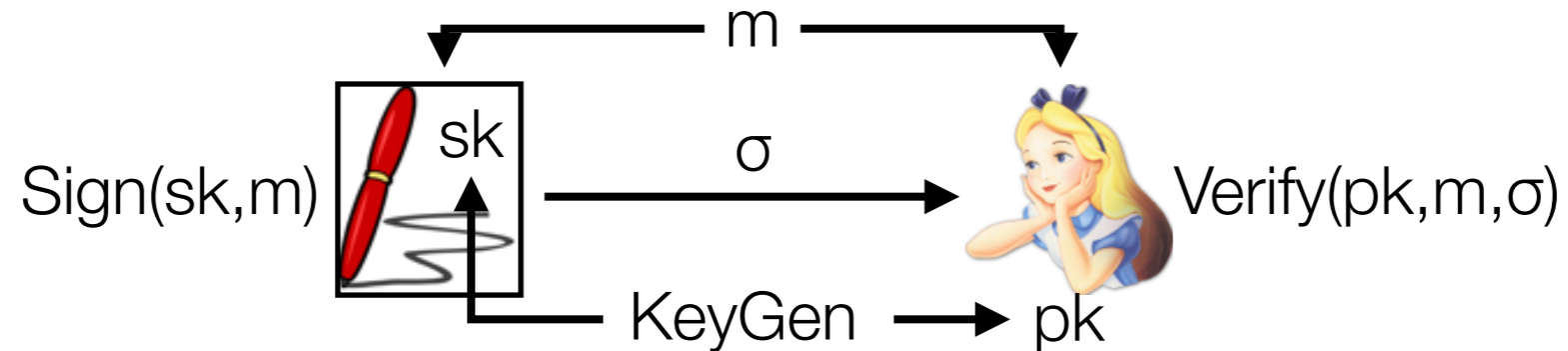
Signatures are proved secure in **standard cryptographic models**



# Practical security of digital signatures

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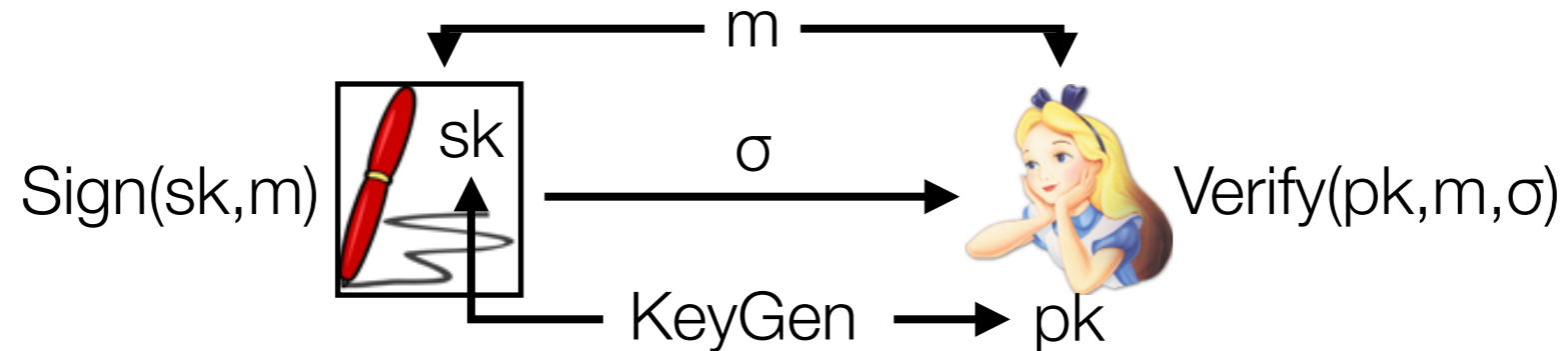
Signatures are proved secure in **standard cryptographic models**



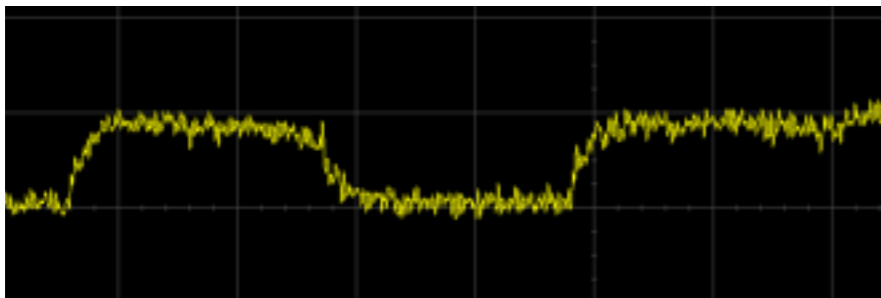
**Standard model is useless** against side channels and fault injection

# Practical security of digital signatures

Signatures are proved secure in **standard cryptographic models**



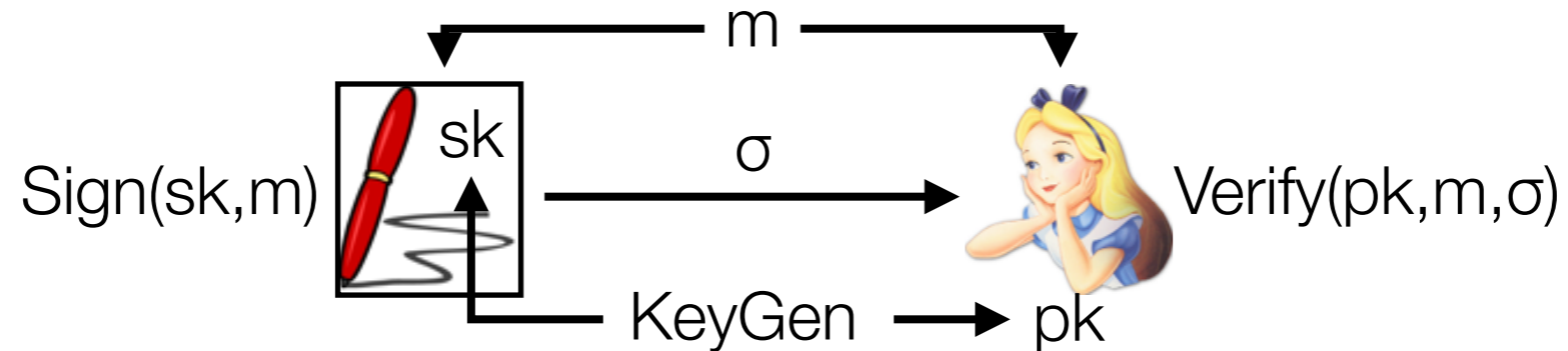
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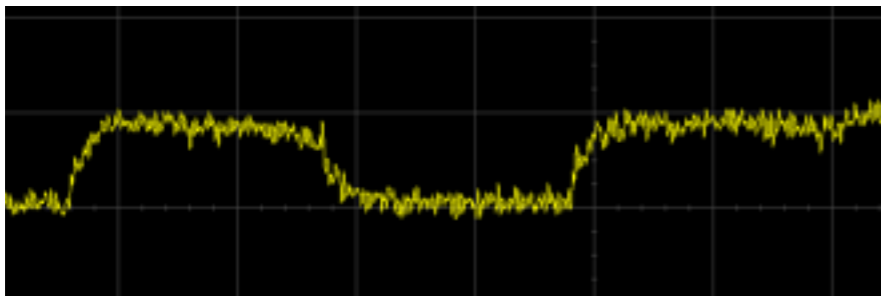


# Practical security of digital signatures

Signatures are proved secure in **standard cryptographic models**

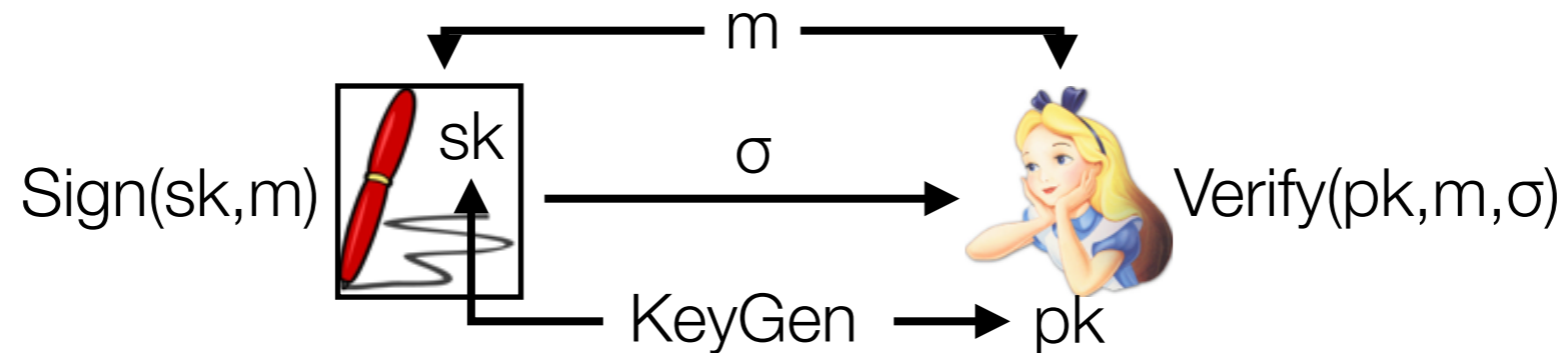


**Standard model is useless** against side channels and fault injection

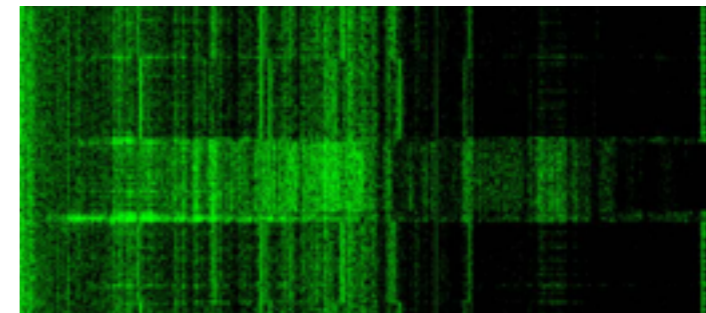
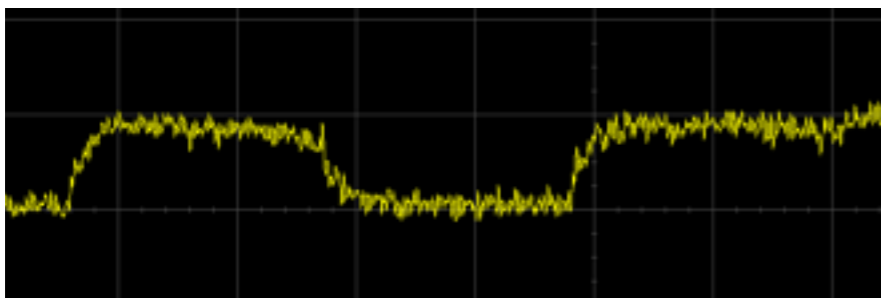


# Practical security of digital signatures

Signatures are proved secure in **standard cryptographic models**

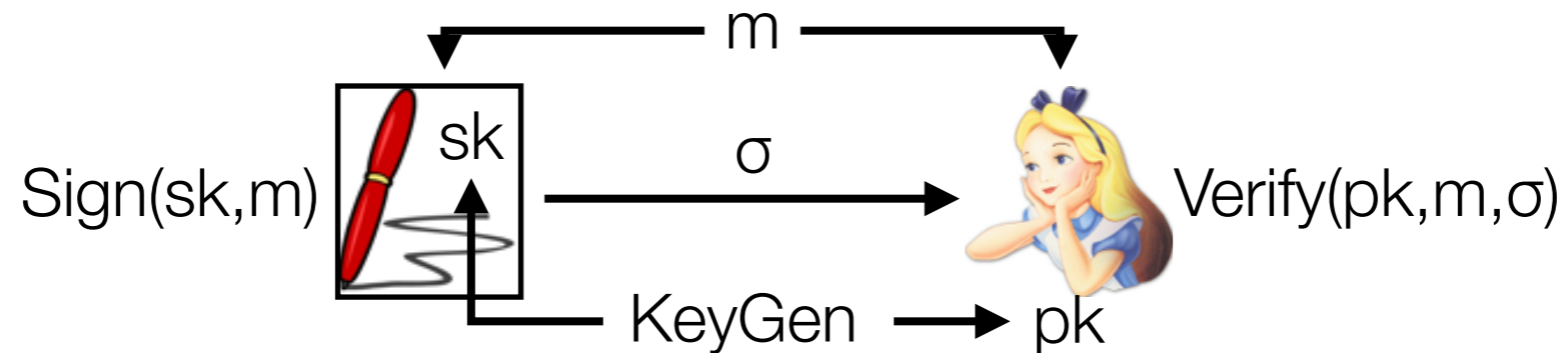


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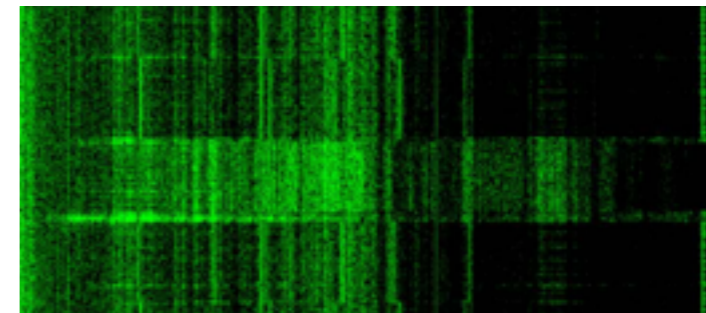
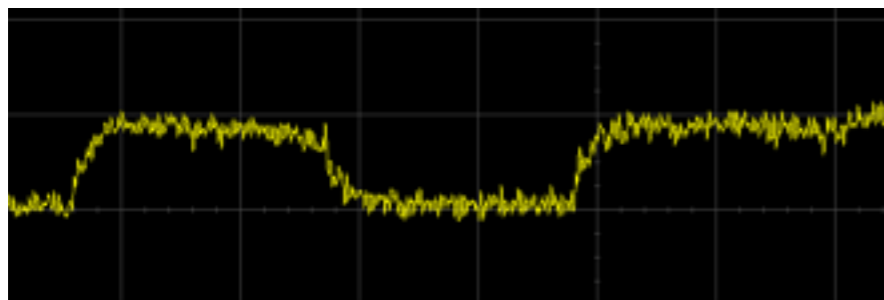


# Practical security of digital signatures

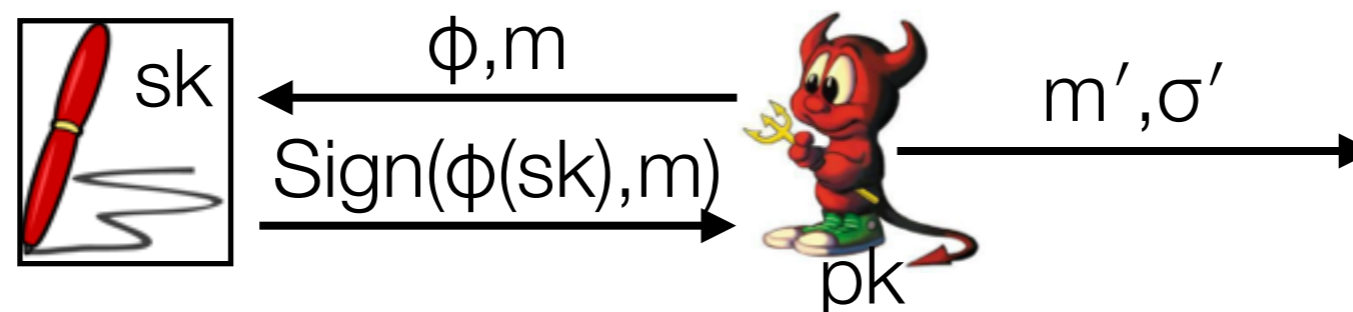
Signatures are proved secure in **standard cryptographic models**



**Standard model is useless** against side channels and fault injection

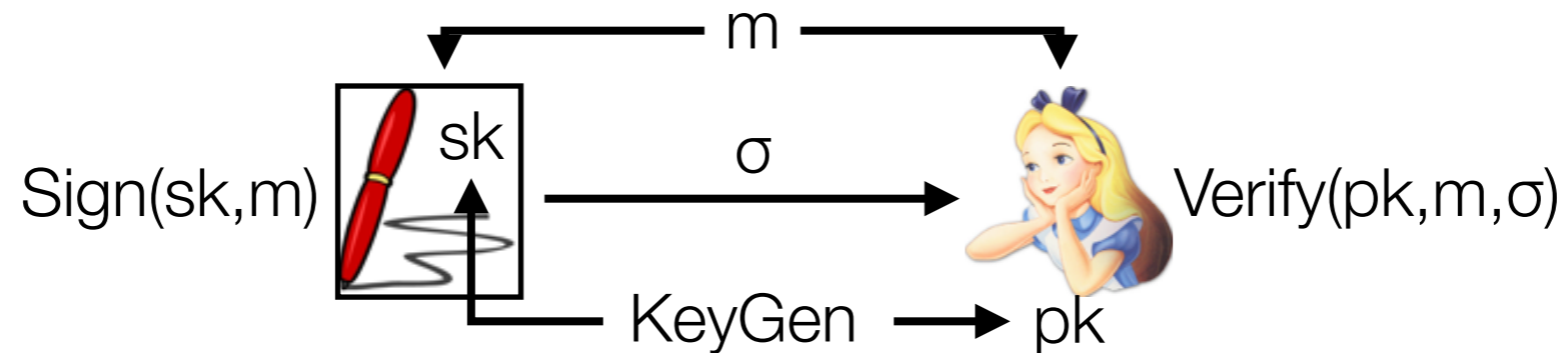


**RKA (related key attack) security** considers these attacks

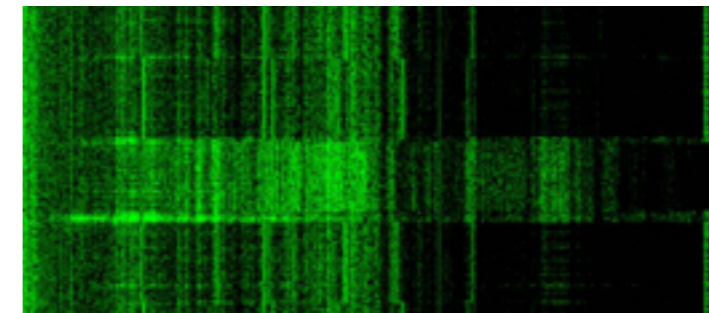
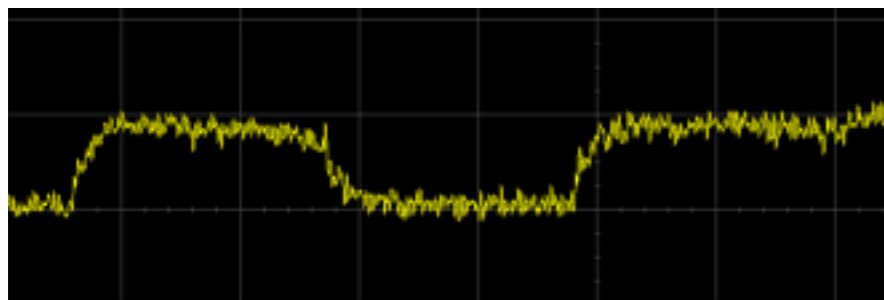


# Practical security of digital signatures

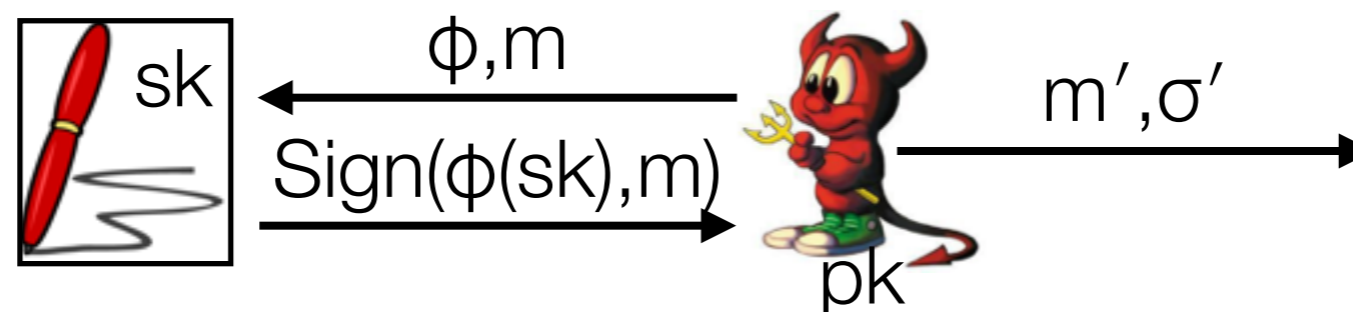
Signatures are proved secure in **standard cryptographic models**



**Standard model is useless** against side channels and fault injection



**RKA (related key attack) security** considers these attacks



Our research can help **create better RKA schemes**

# Standard definitions for signatures [GMR88]

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# Standard definitions for signatures [GMR88]

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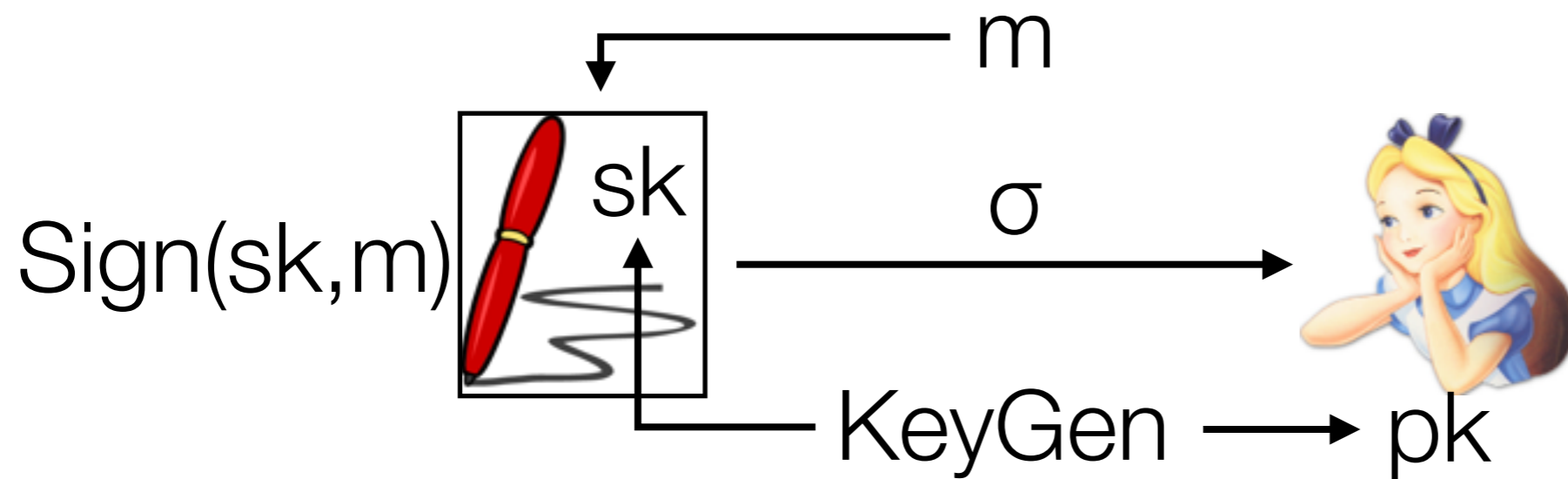
# Standard definitions for signatures [GMR88]

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# Standard definitions for signatures [GMR88]

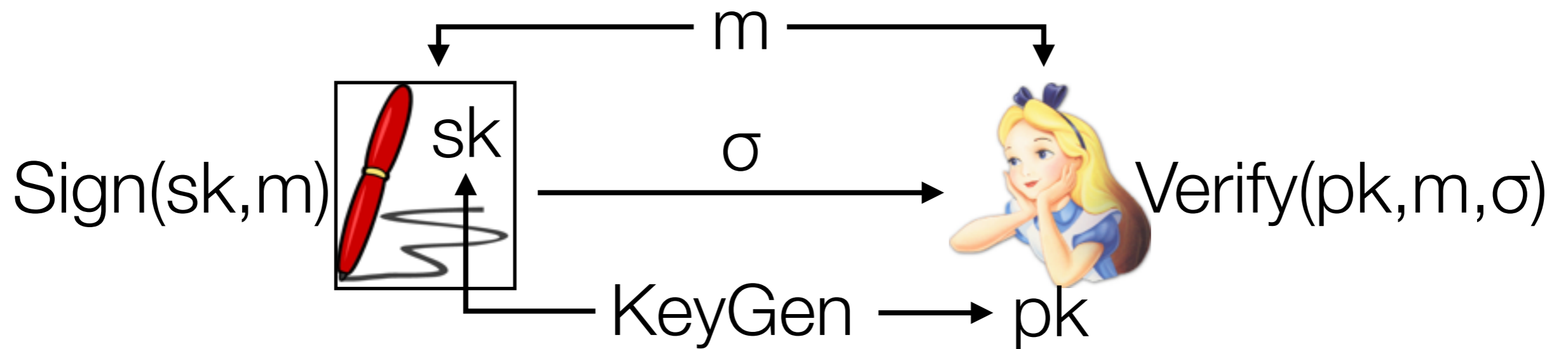
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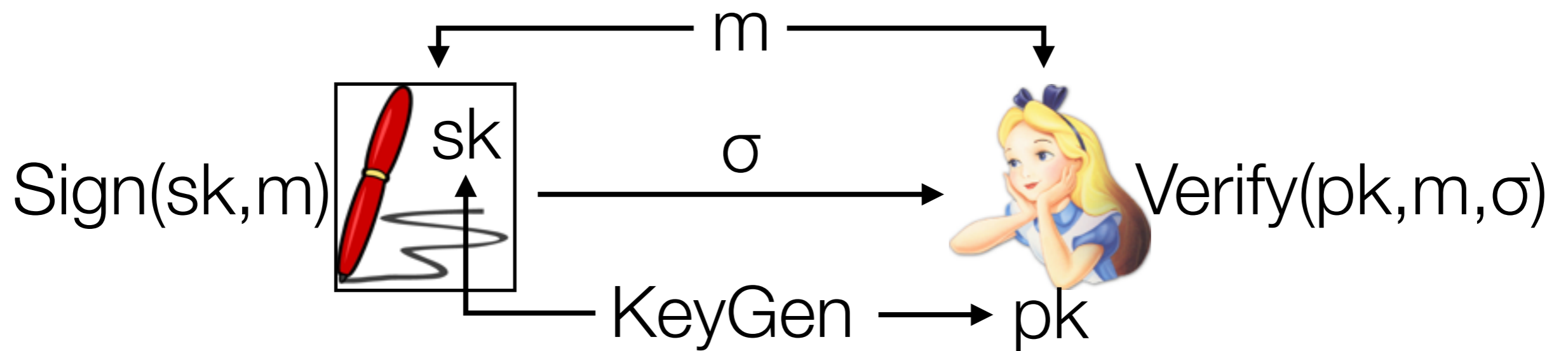


# Standard definitions for signatures [GMR88]

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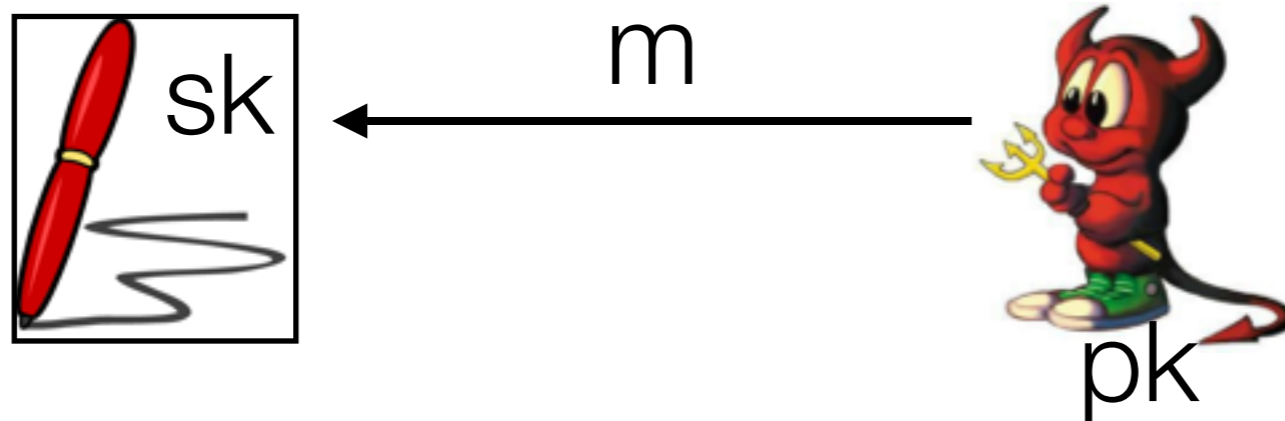
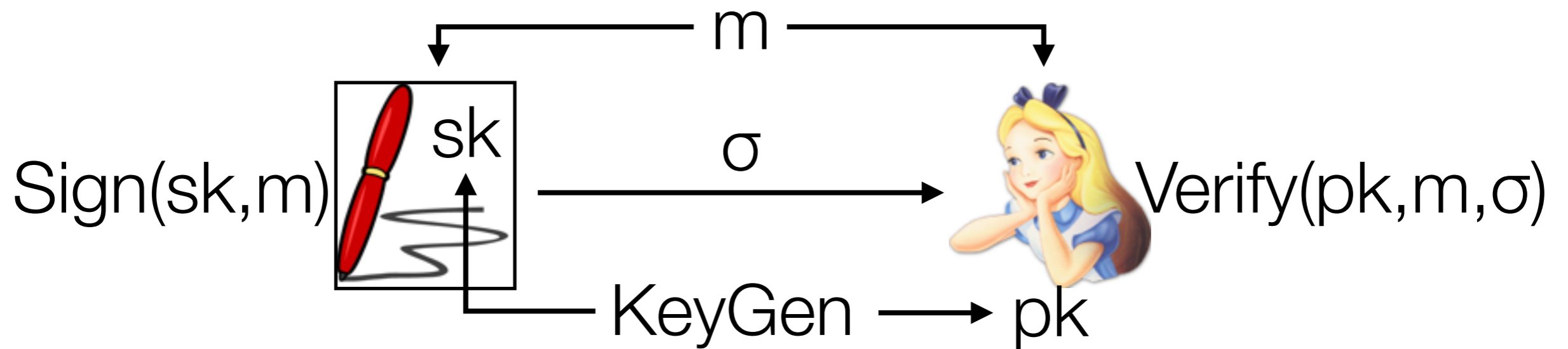


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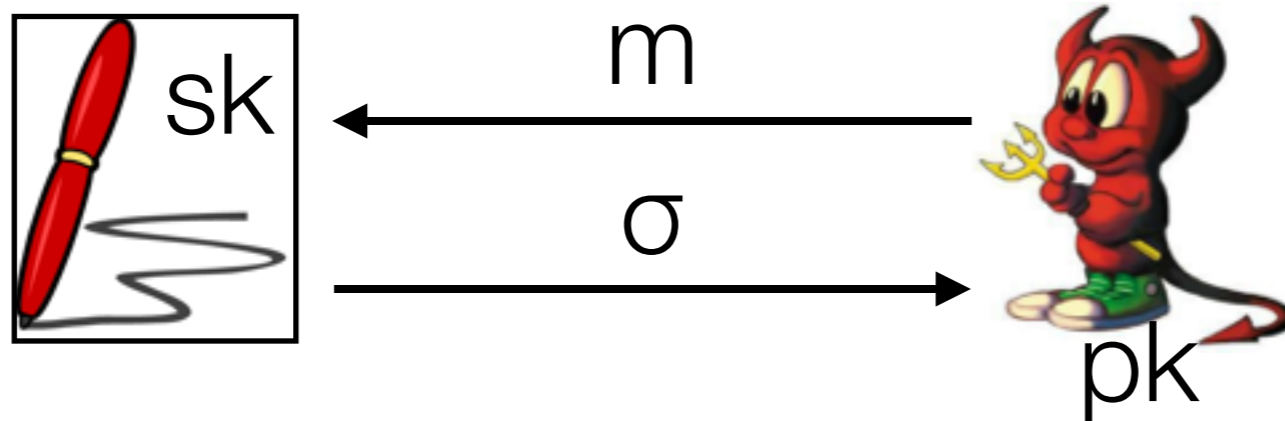
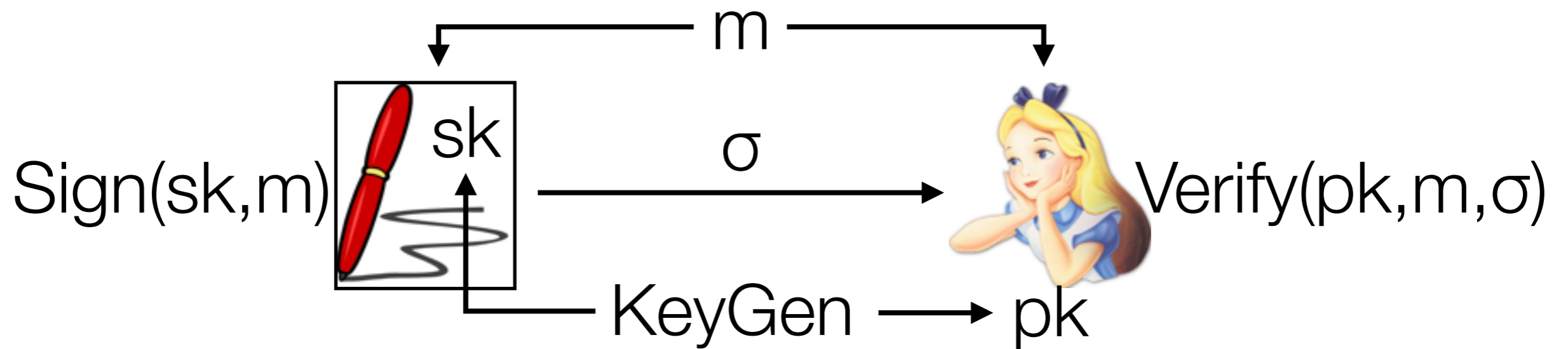
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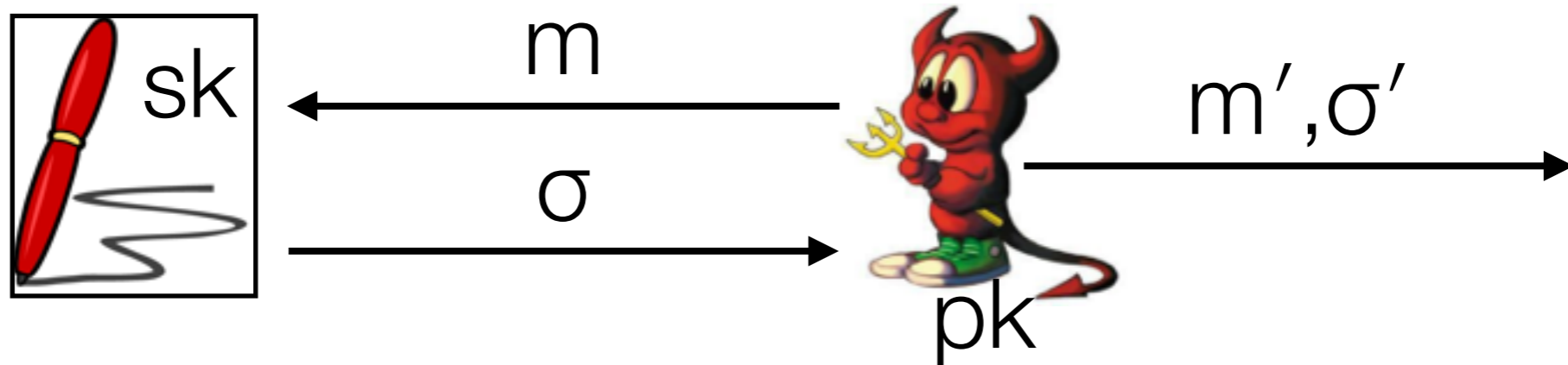
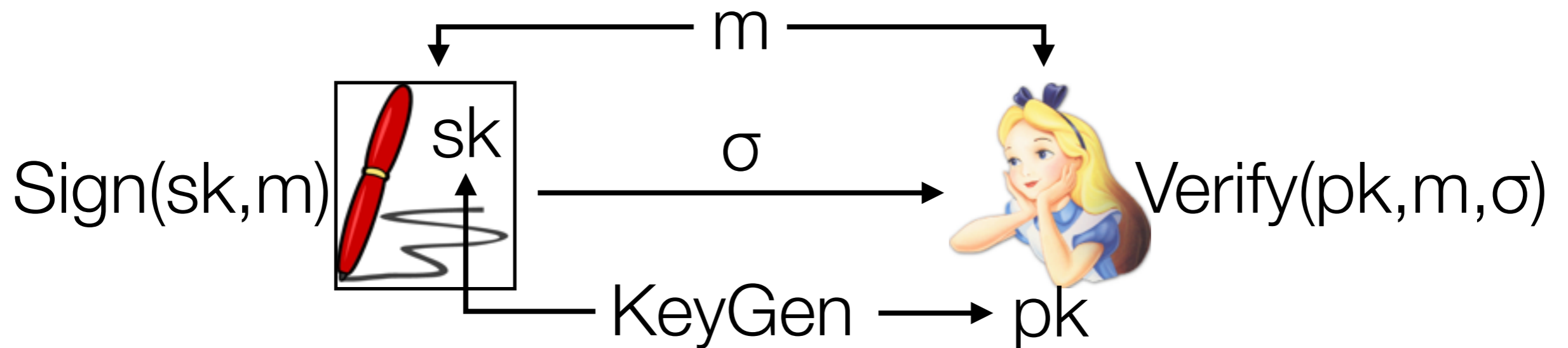


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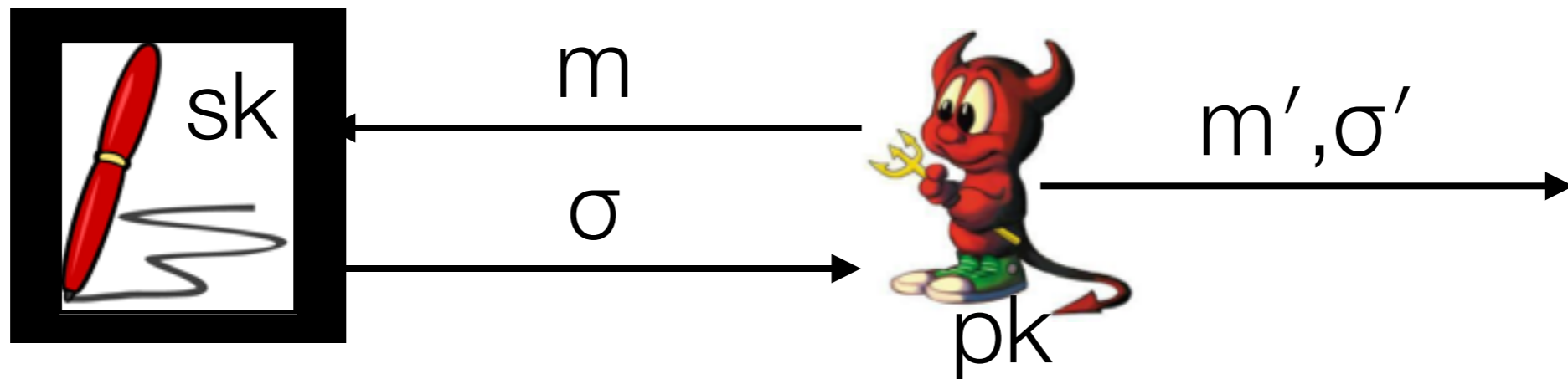
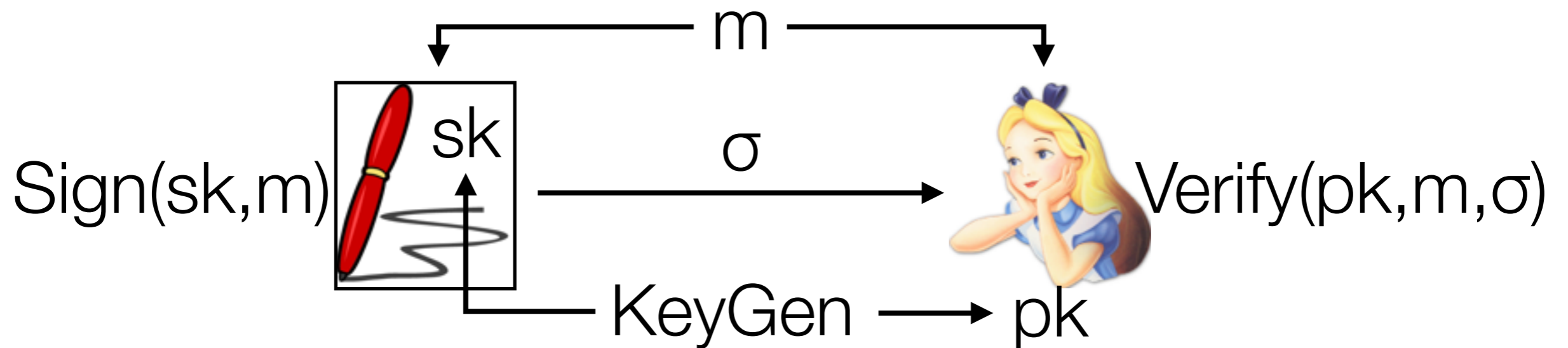


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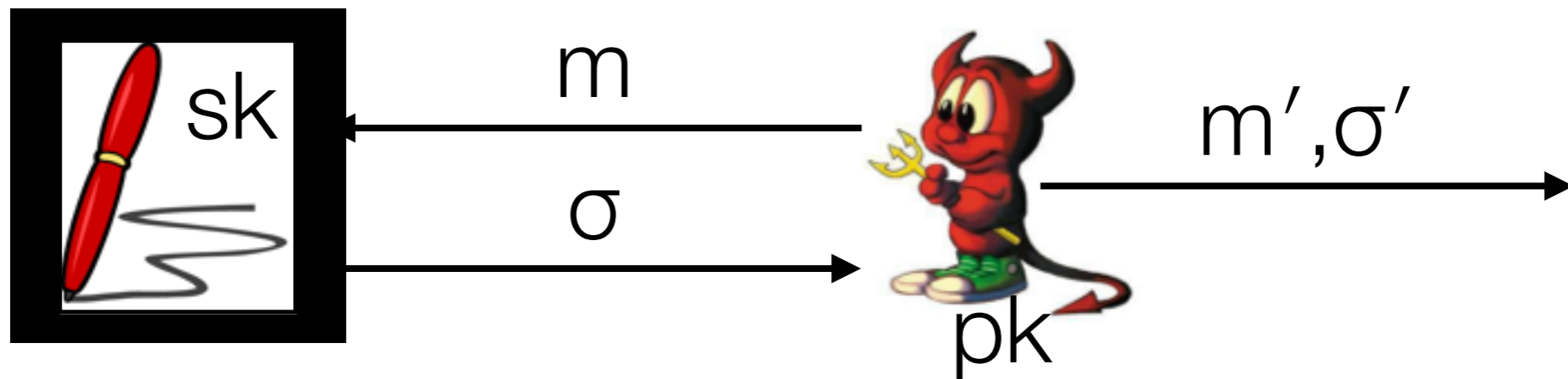
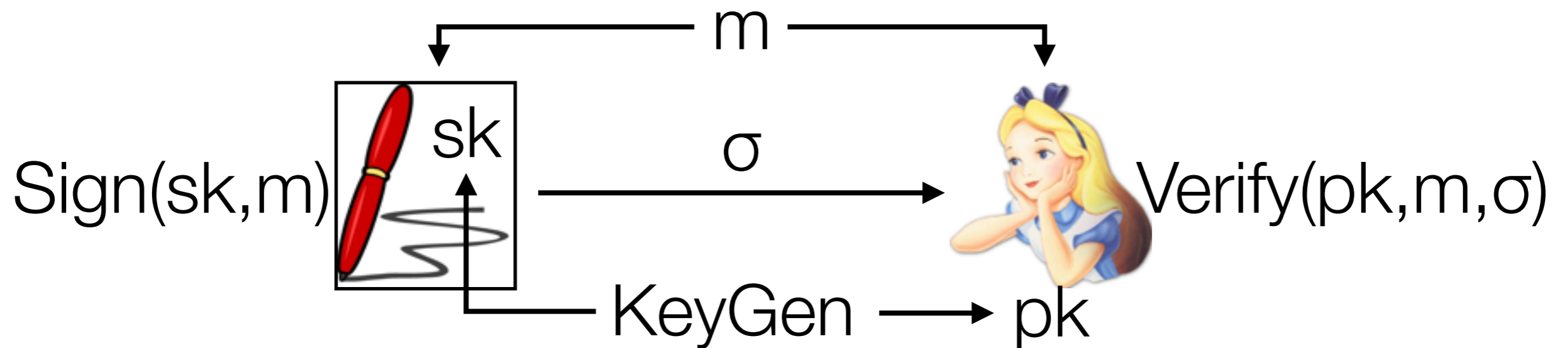
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**Problem:** This assumption is **violated** by **tampering** [AK96,...], **side channels** [W91, KJJ99,...] and **fault injection** [BS97, BdML97,...]

# Related key attacks (RKA)

---

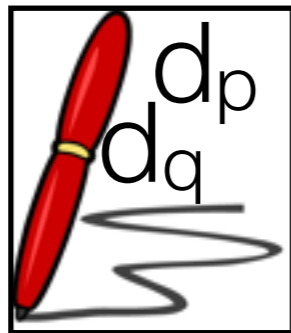
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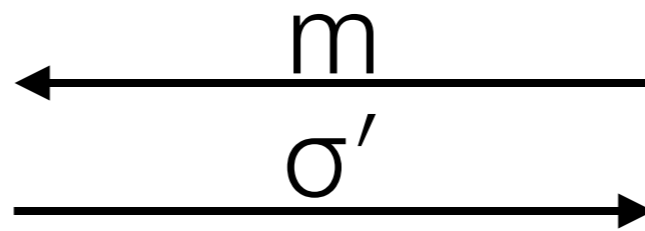
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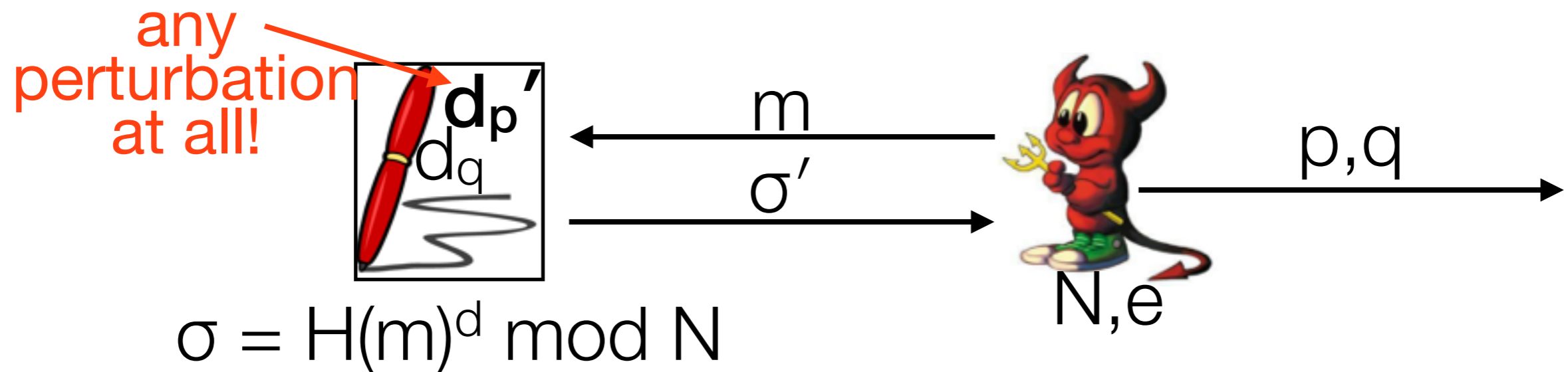


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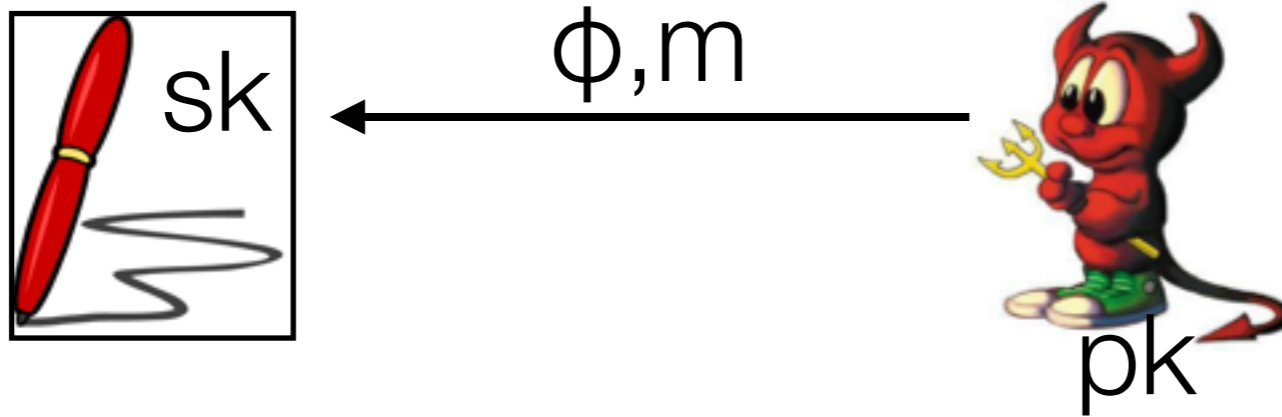
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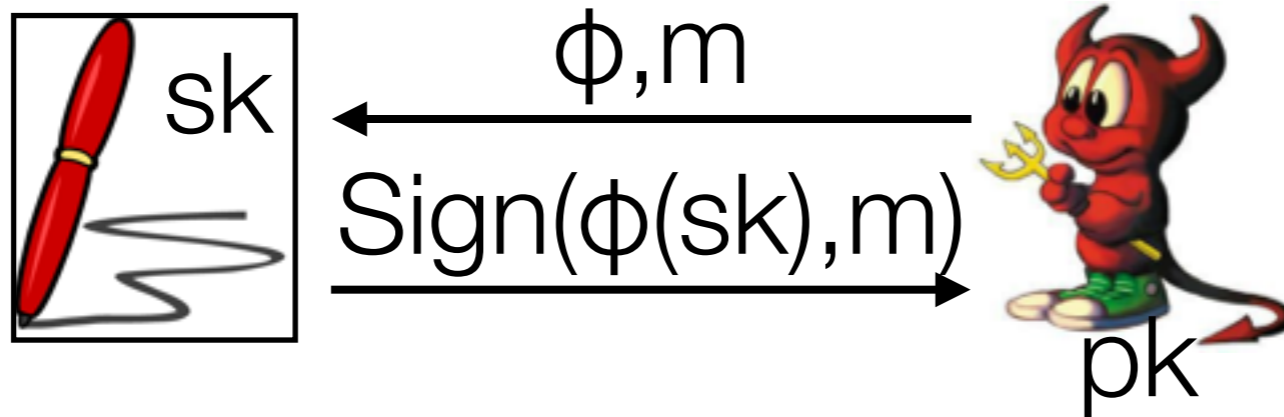
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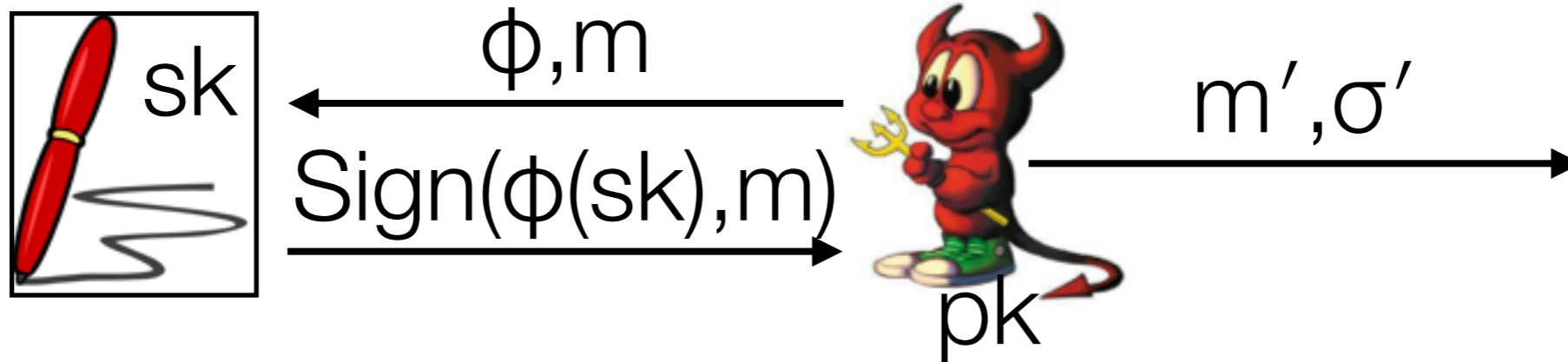
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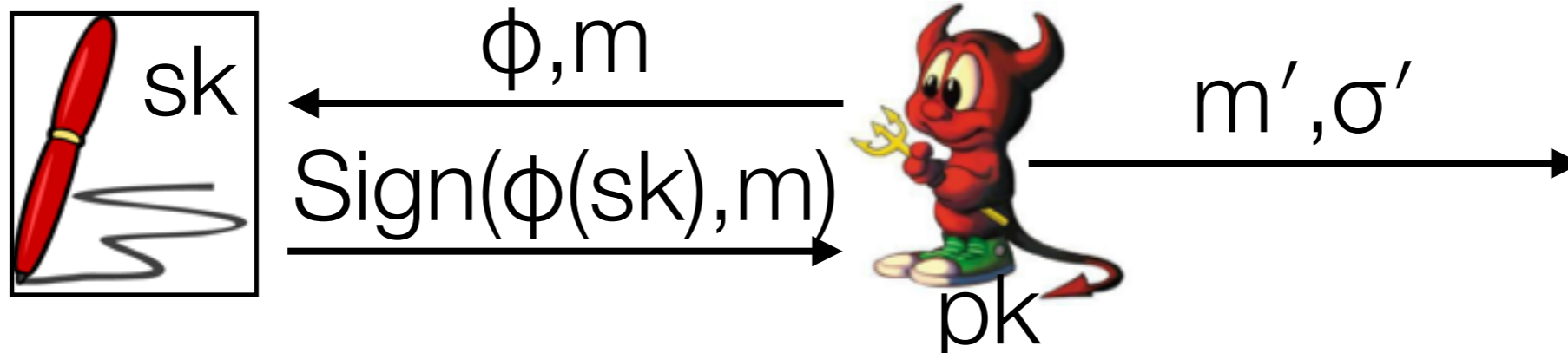
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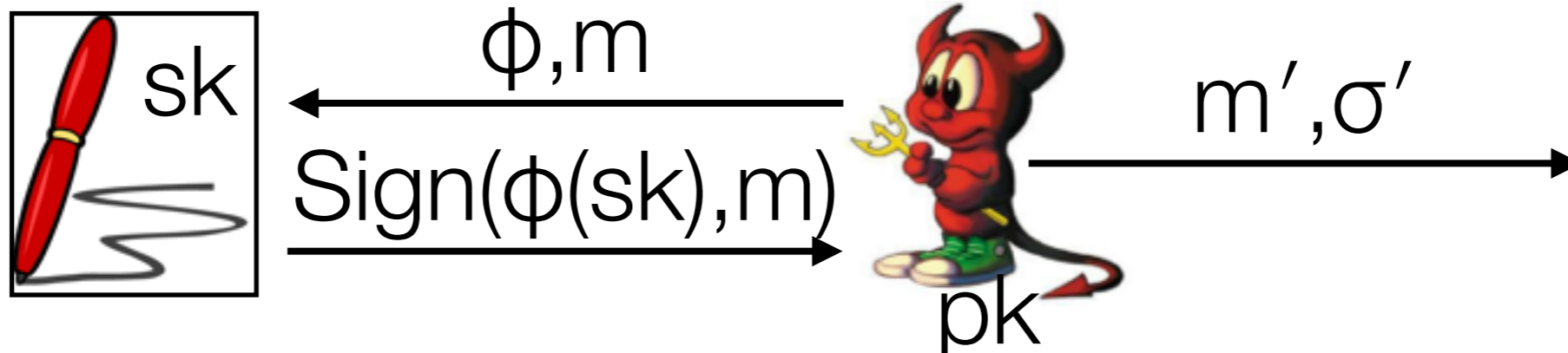
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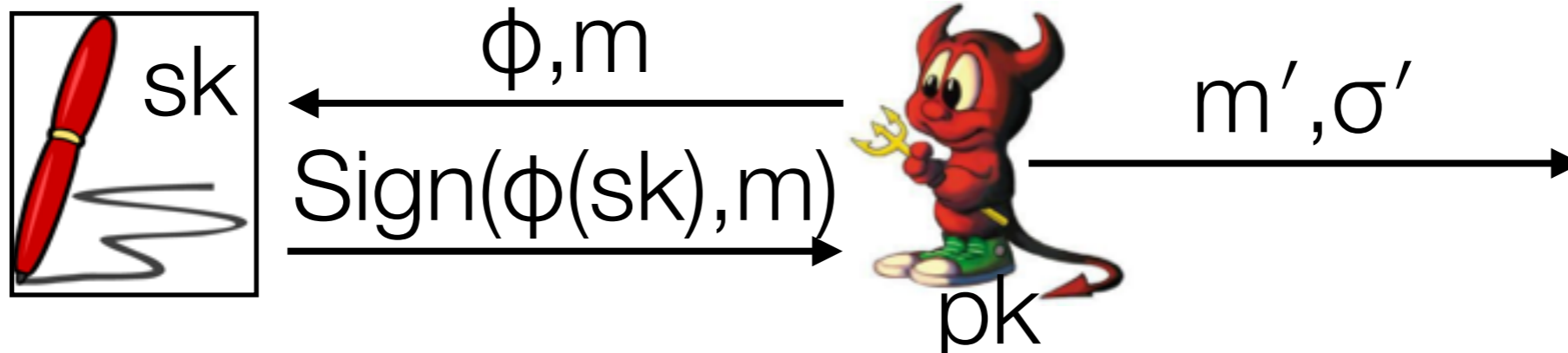
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$\Phi=\{id\}$  gives standard unforgeability

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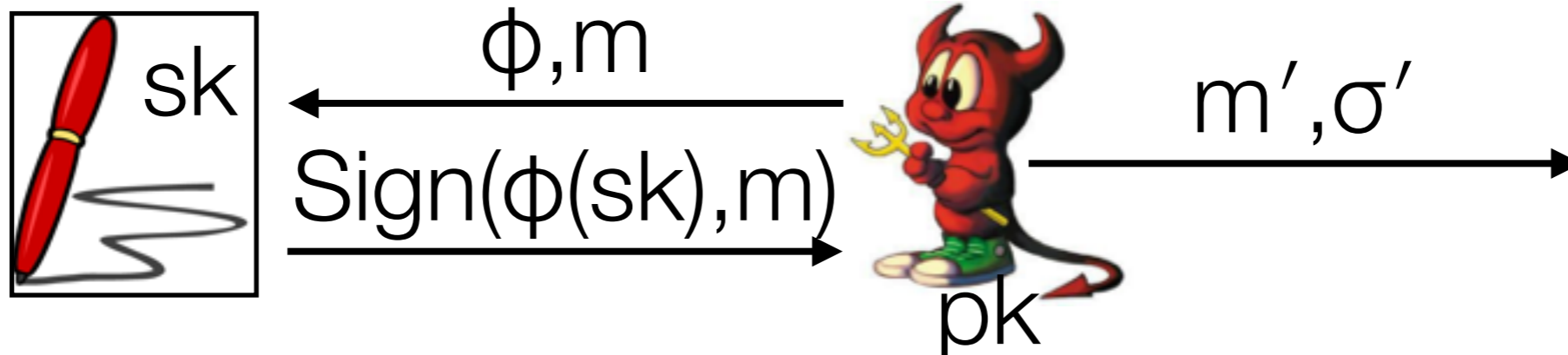


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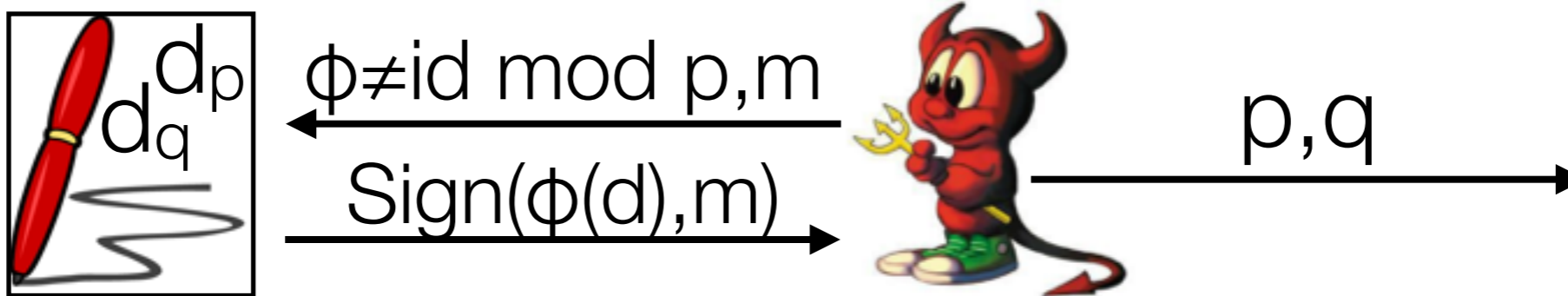
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$\Phi=\{all\ functions\}$  isn't possible [BK03]

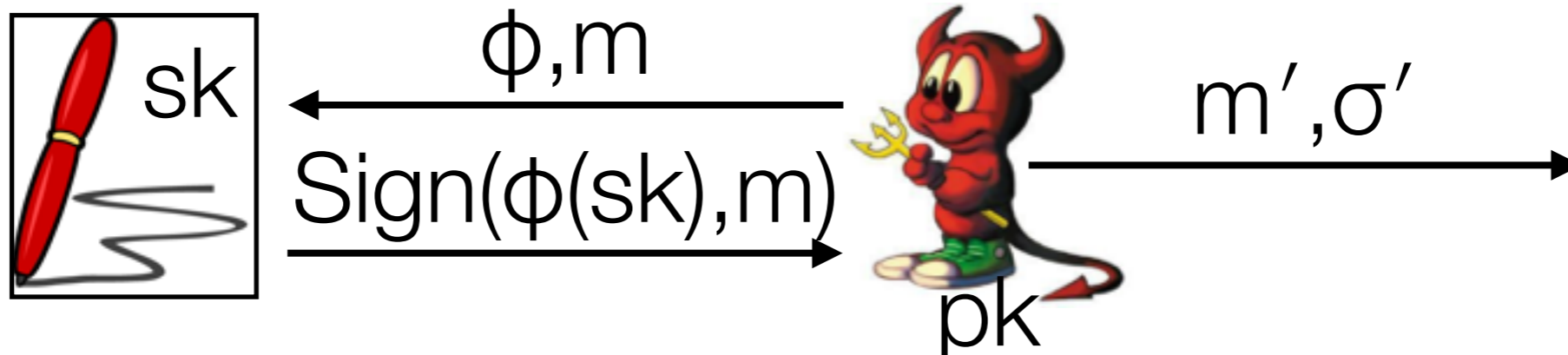
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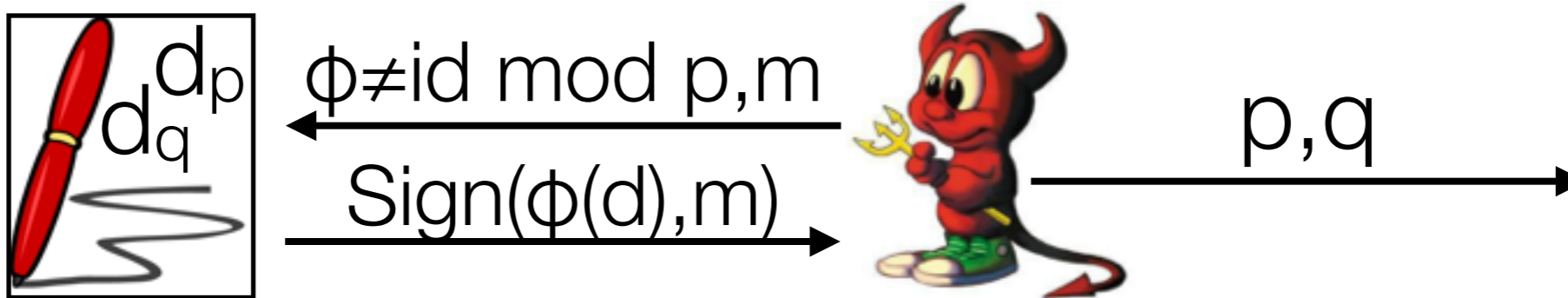
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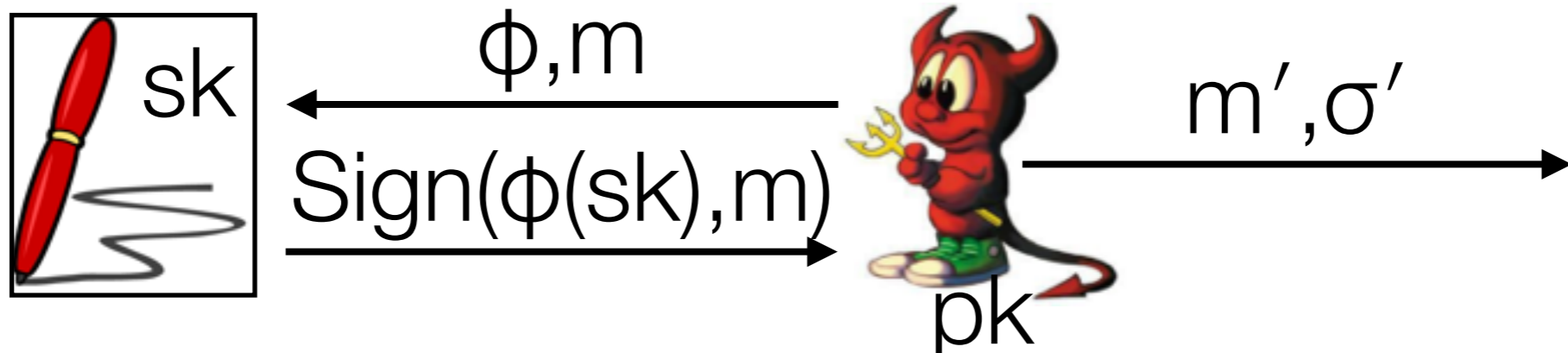


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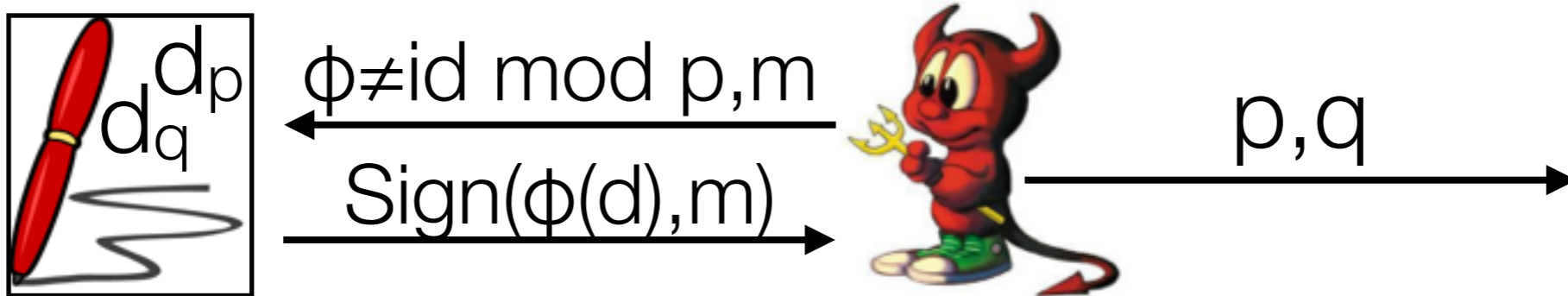


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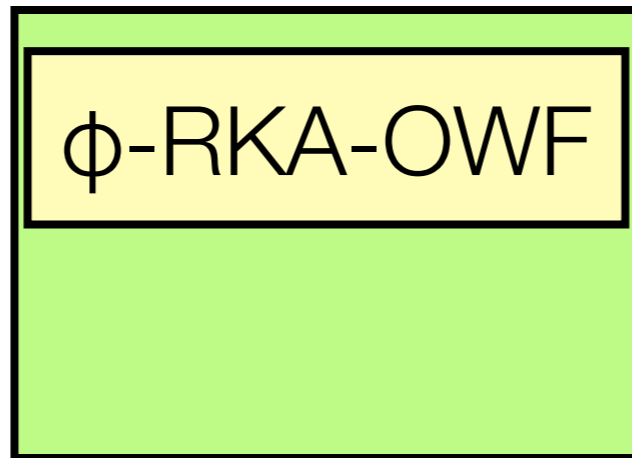
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$\phi$ -RKA-OWF

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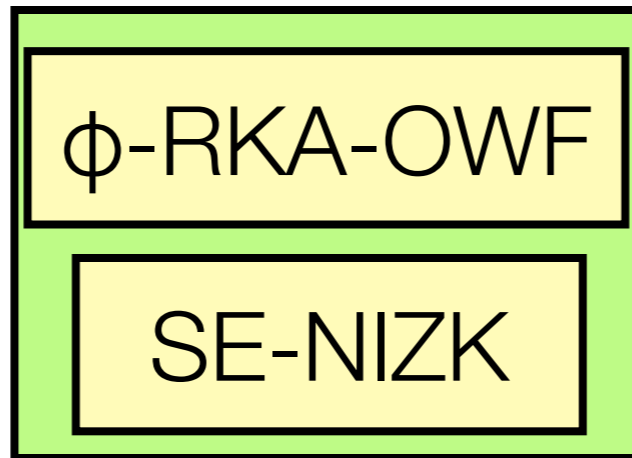
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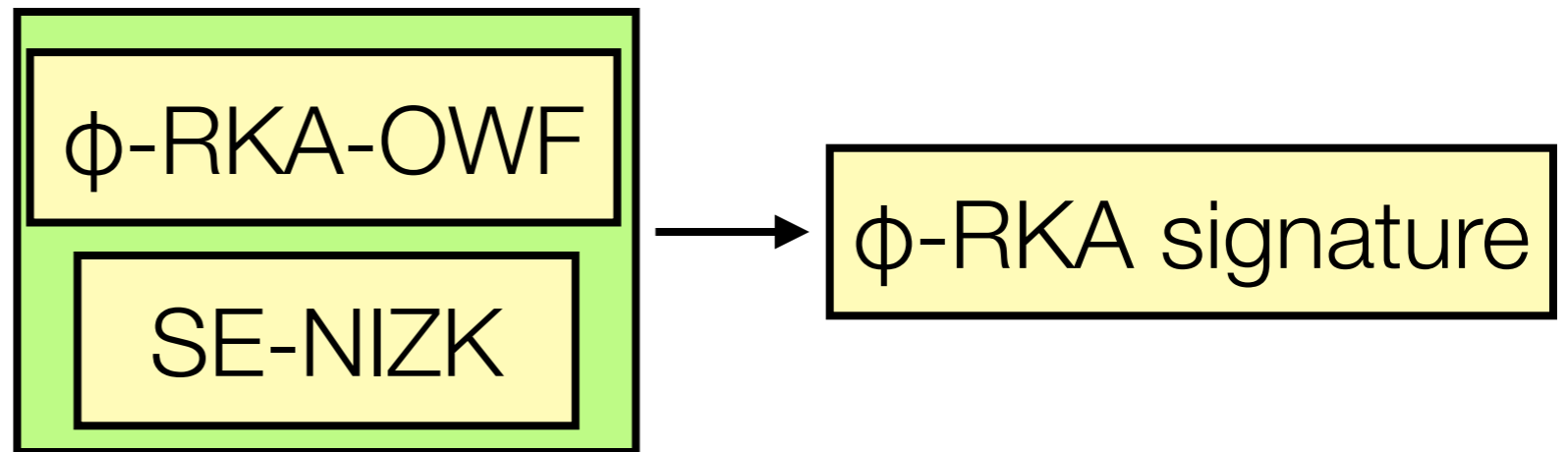
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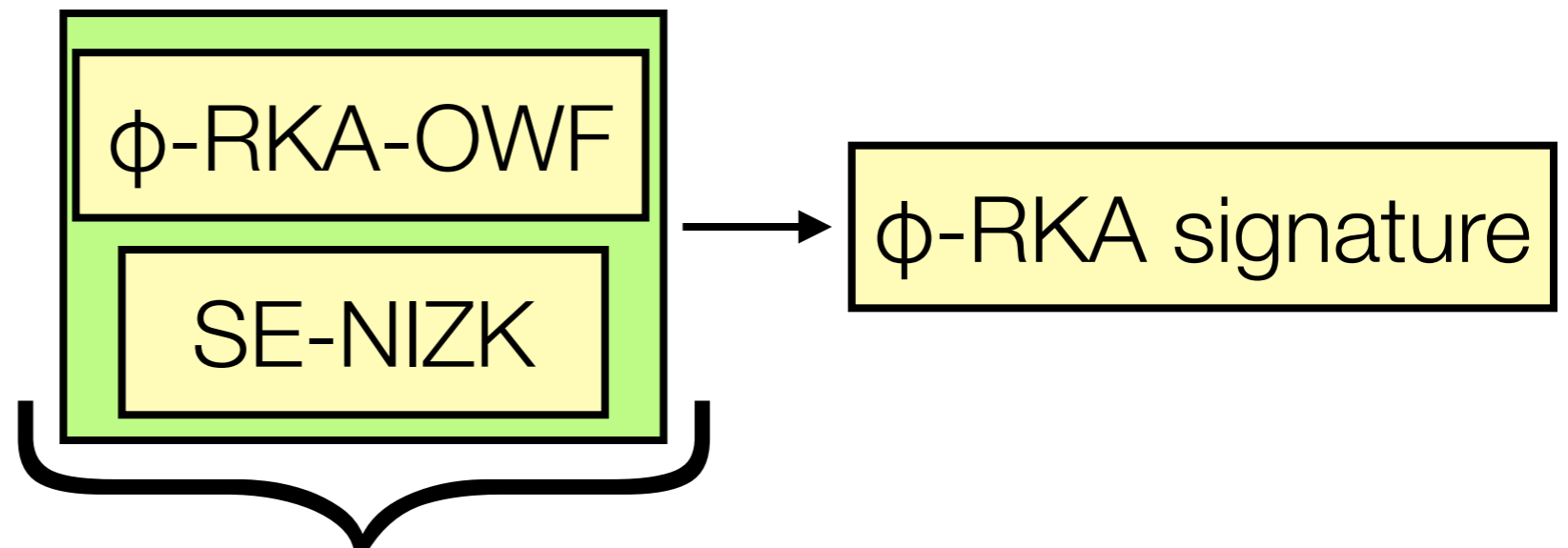
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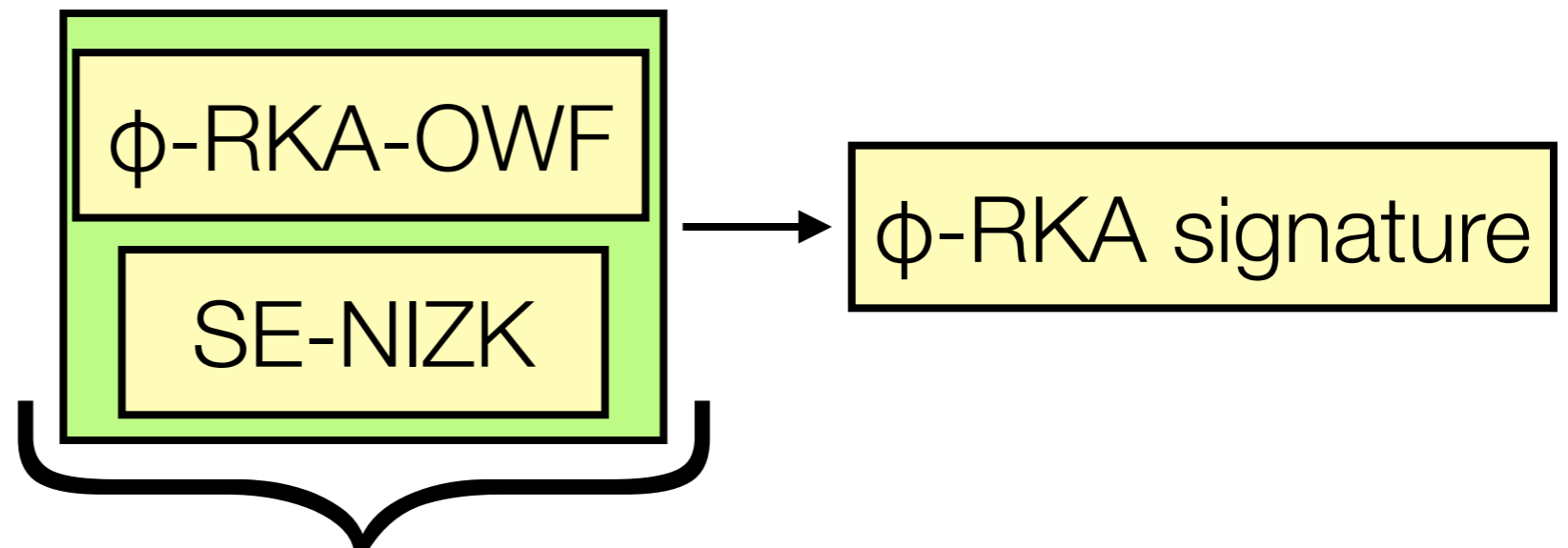


simple construction [DHLW10, CKLM14]

- **KeyGen**:  $\text{crs} \leftarrow \text{CRSGen}; x \leftarrow \text{Dom}(f); y \leftarrow f(x)$   
return  $(\text{pk}=(\text{crs}, y), \text{sk}=x)$
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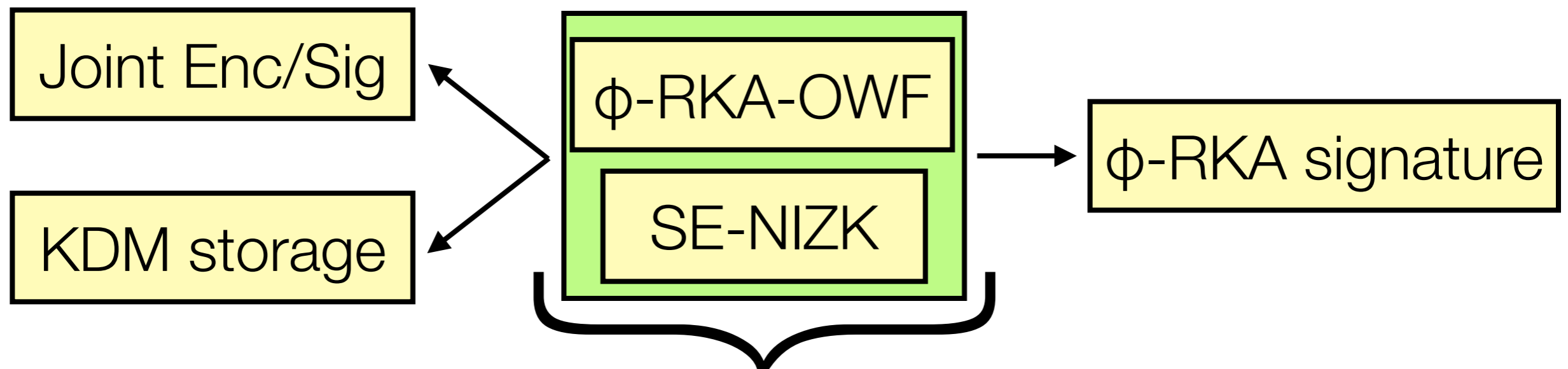


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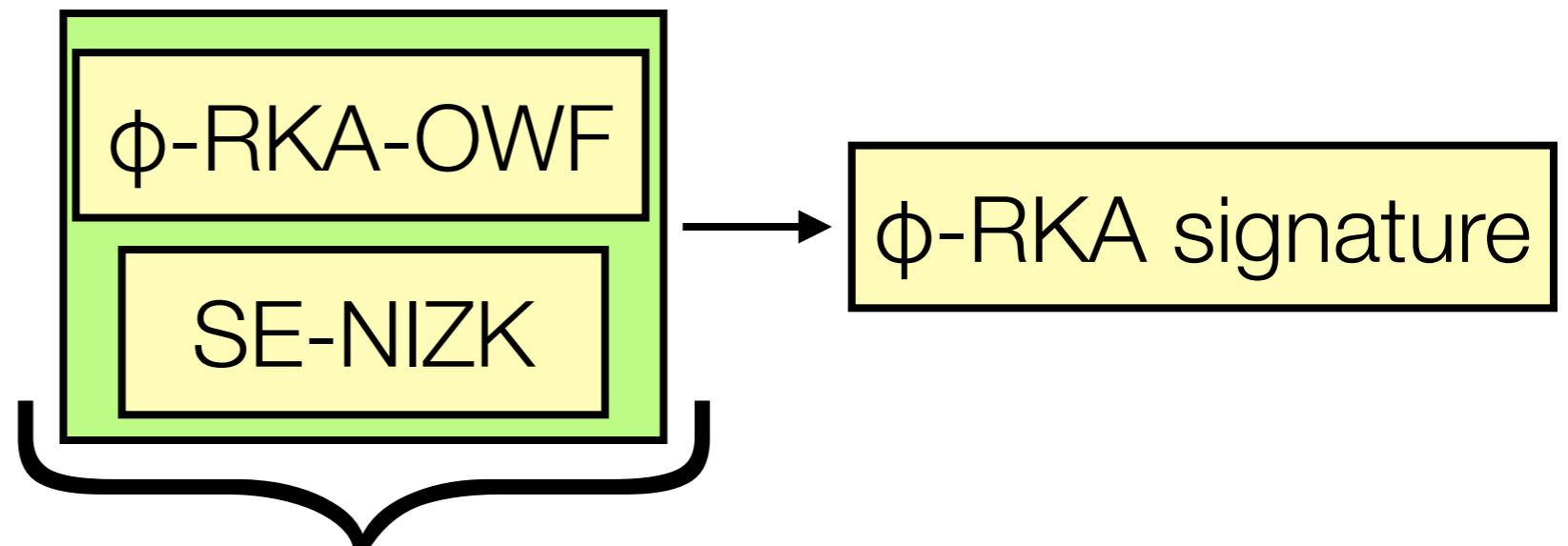
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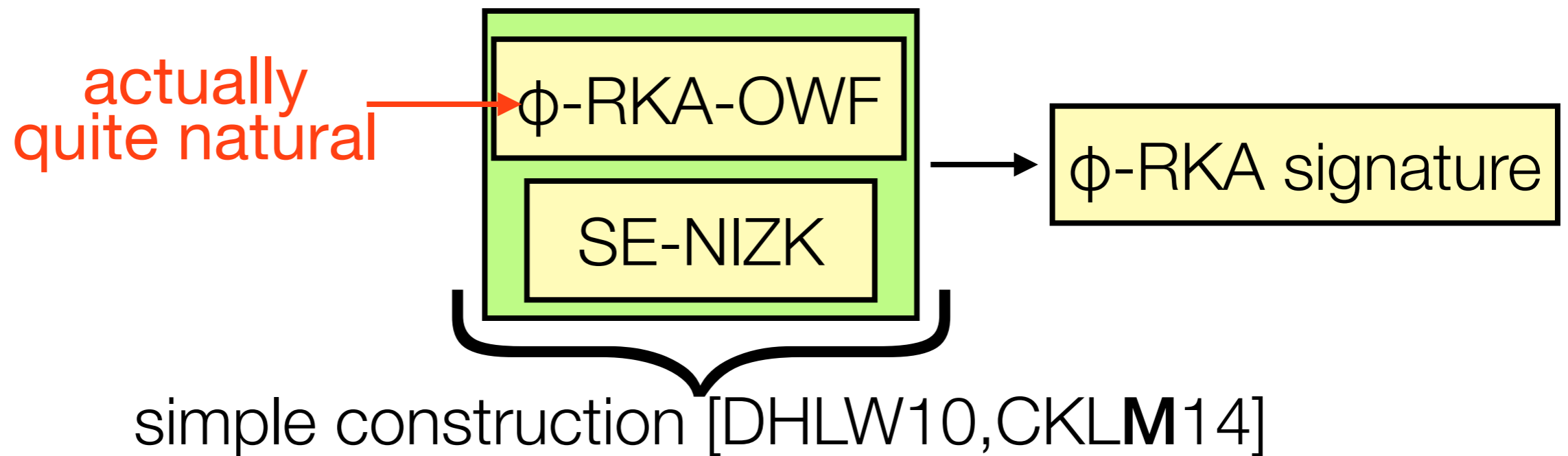


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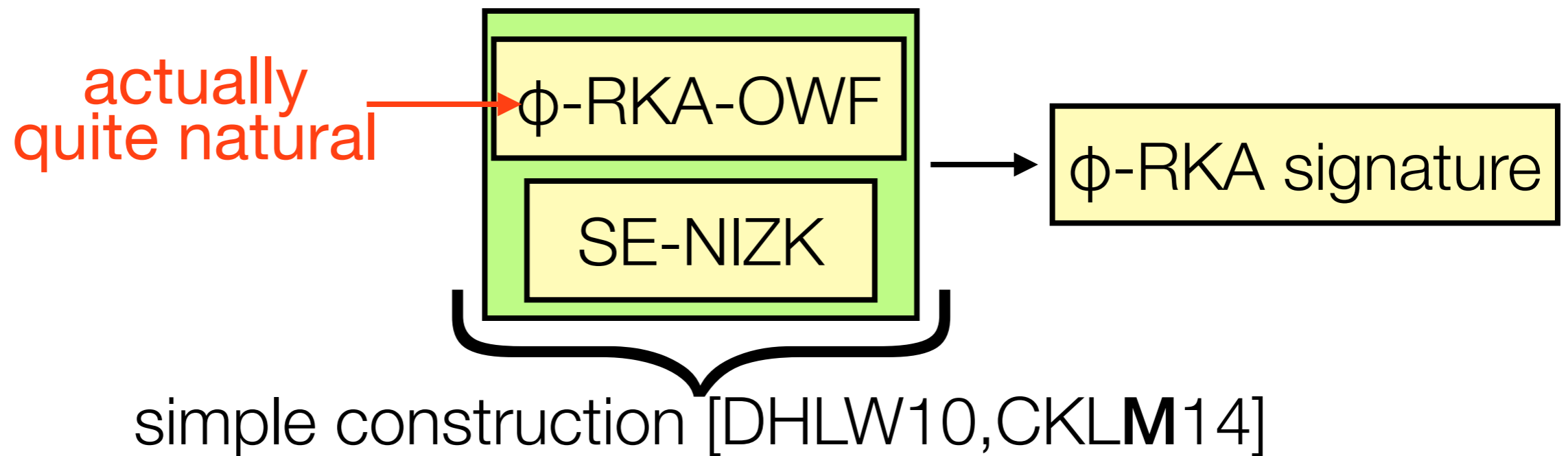
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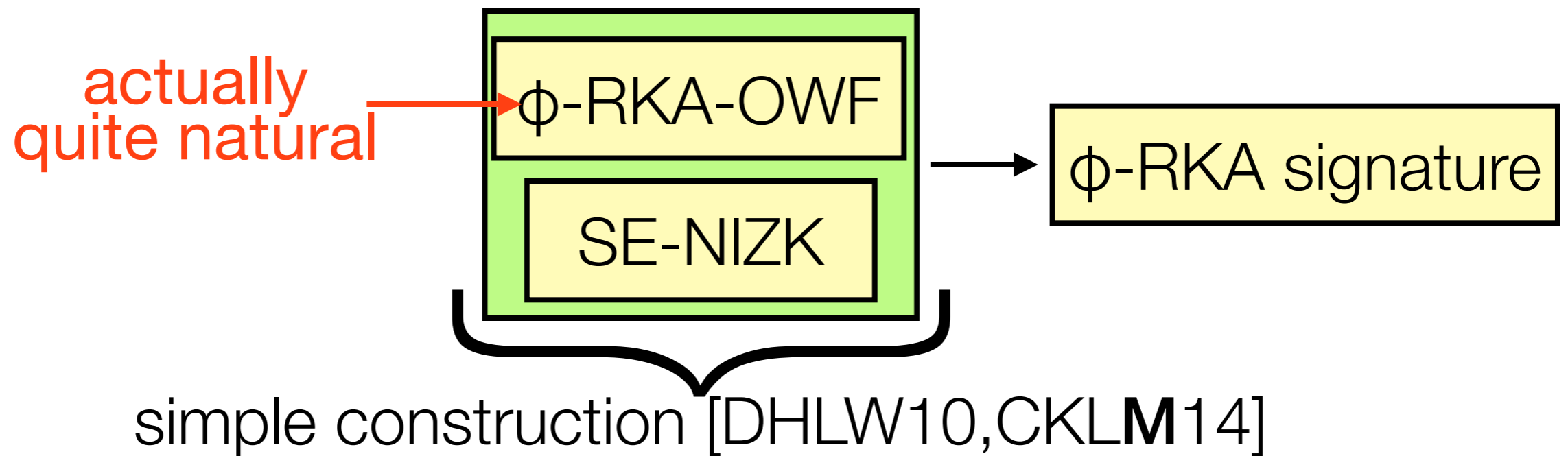
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Creating new RKA-secure signatures is easier!

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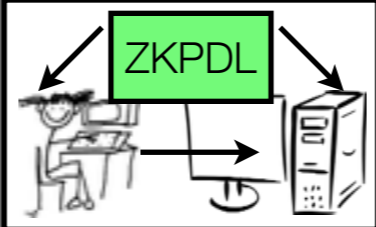

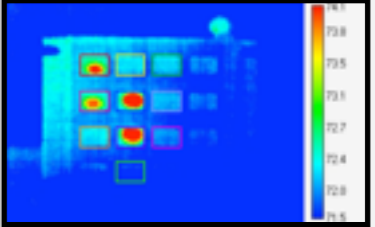
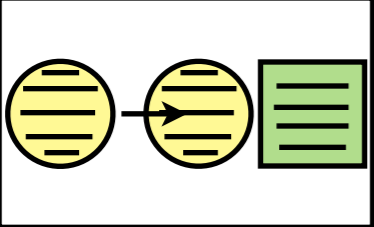
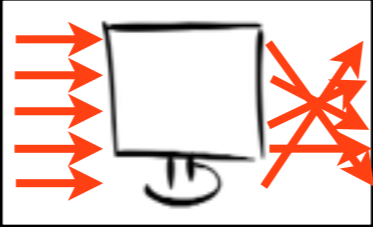


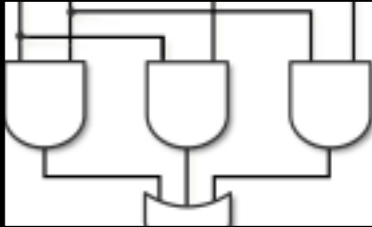
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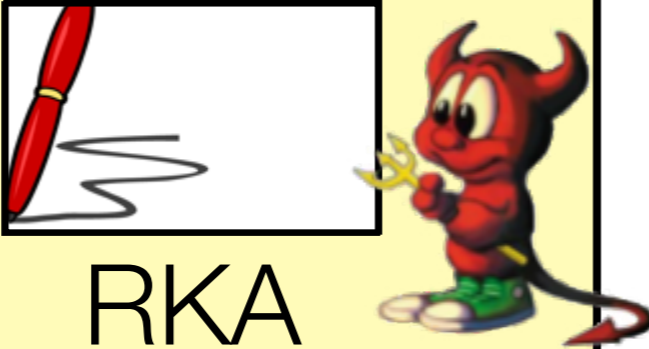
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Our result can pave the way for **easier RKA constructions**

# My research

 [MSF10,LM13]	 [BMT14]	 [MEKHL10]	 [MMCS11]	 [MMS11]
 [CM14]	 [CKLM12,13a,13b]	 [CMZ13]	 [MP+13,HDM+14]	 [OMSK13]





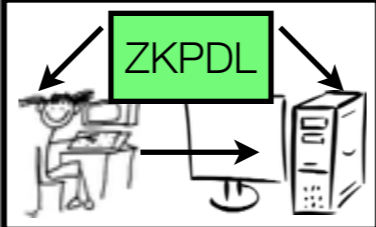

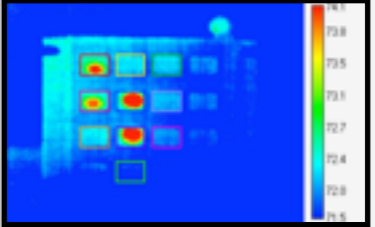
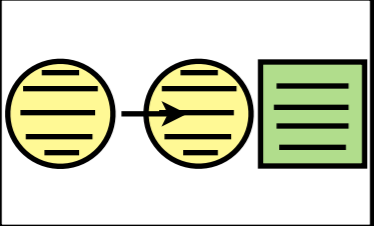
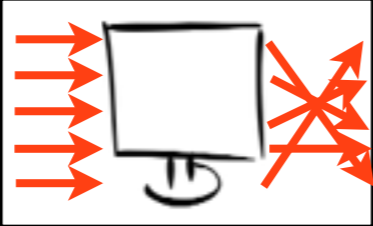


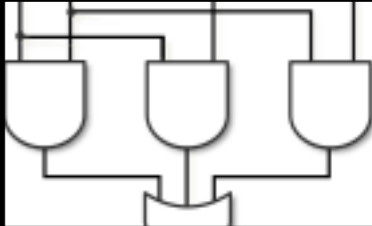
RKA



Bitcoin



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RKA



Bitcoin

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**Centralized**



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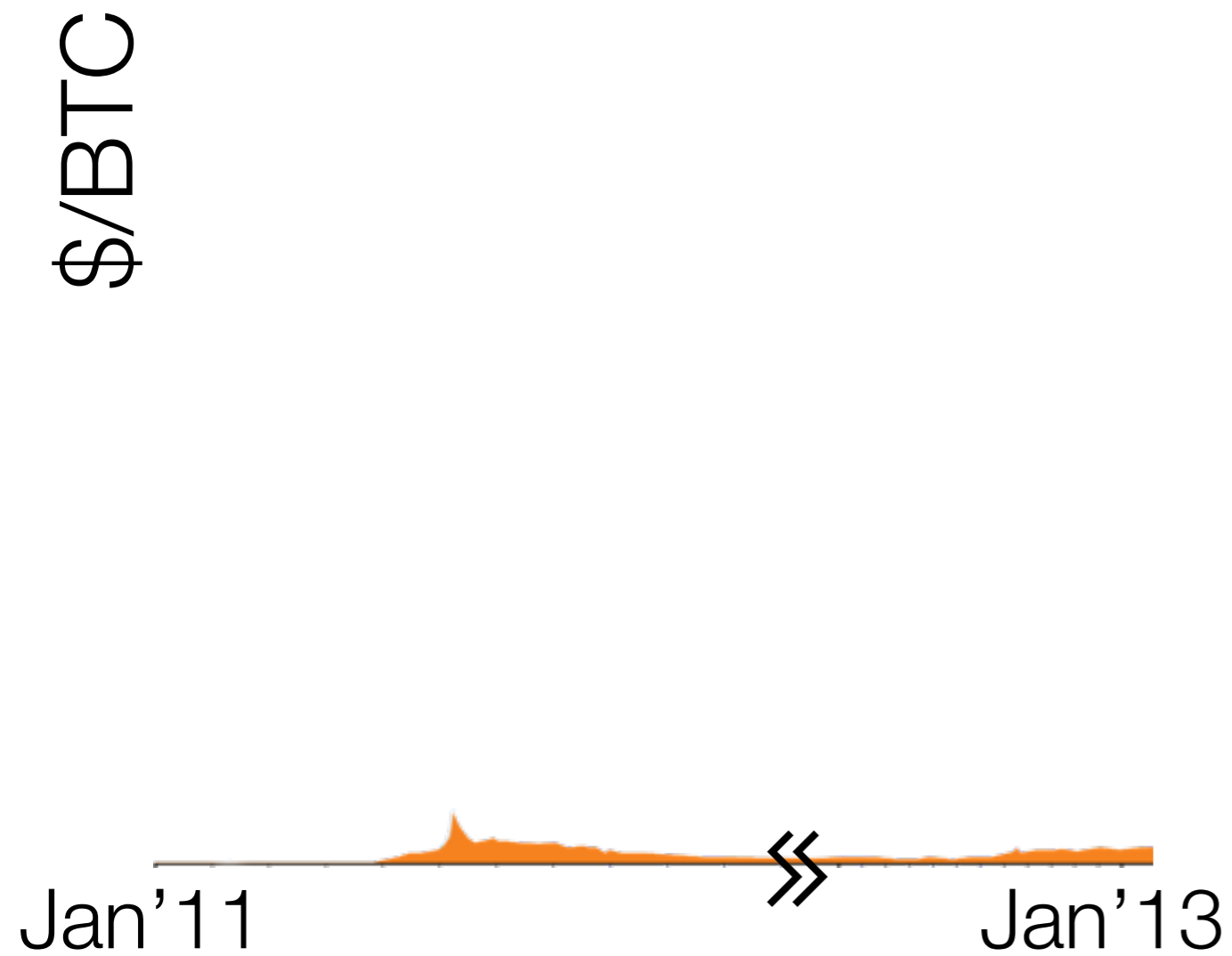
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**How much anonymity does Bitcoin really provide?**

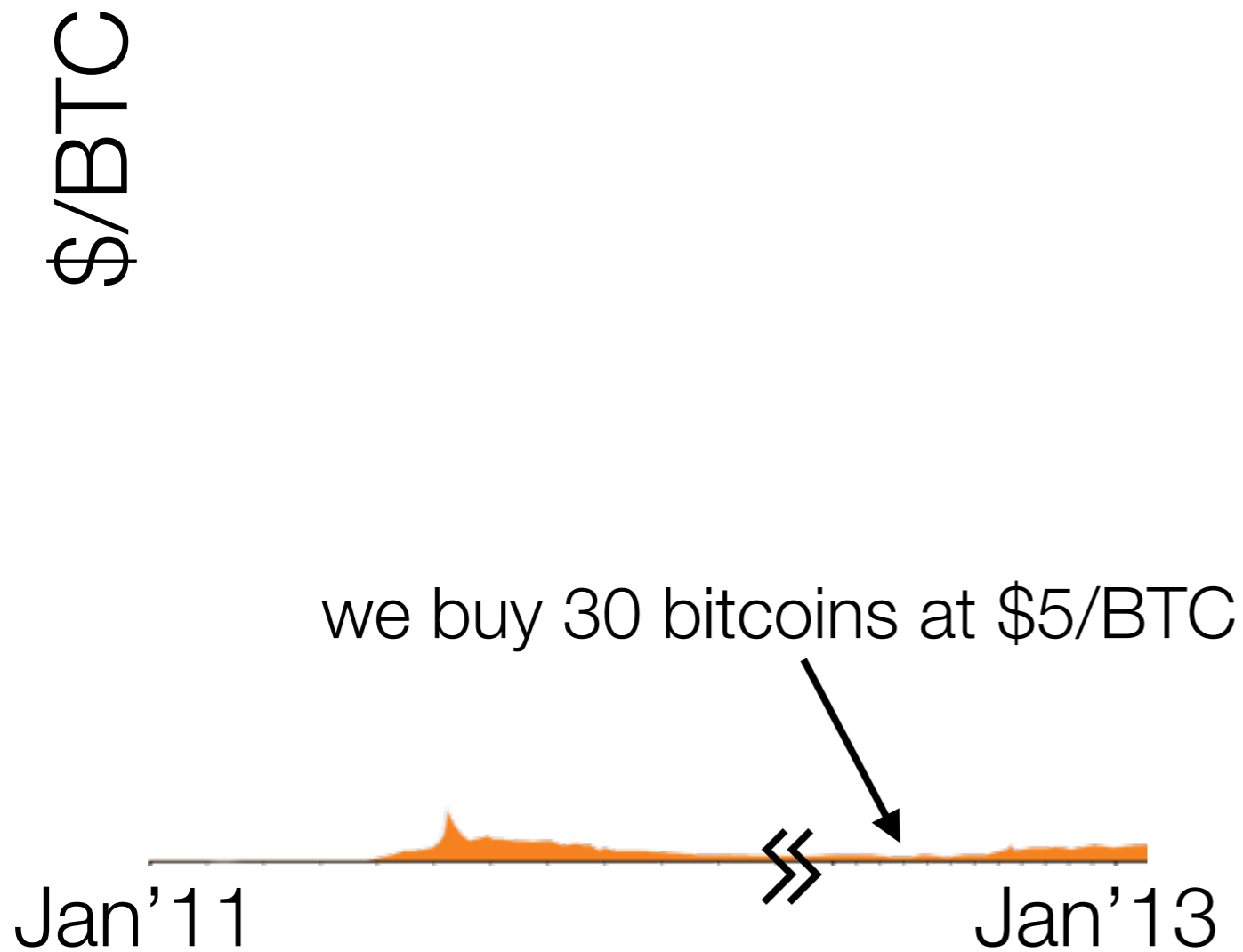
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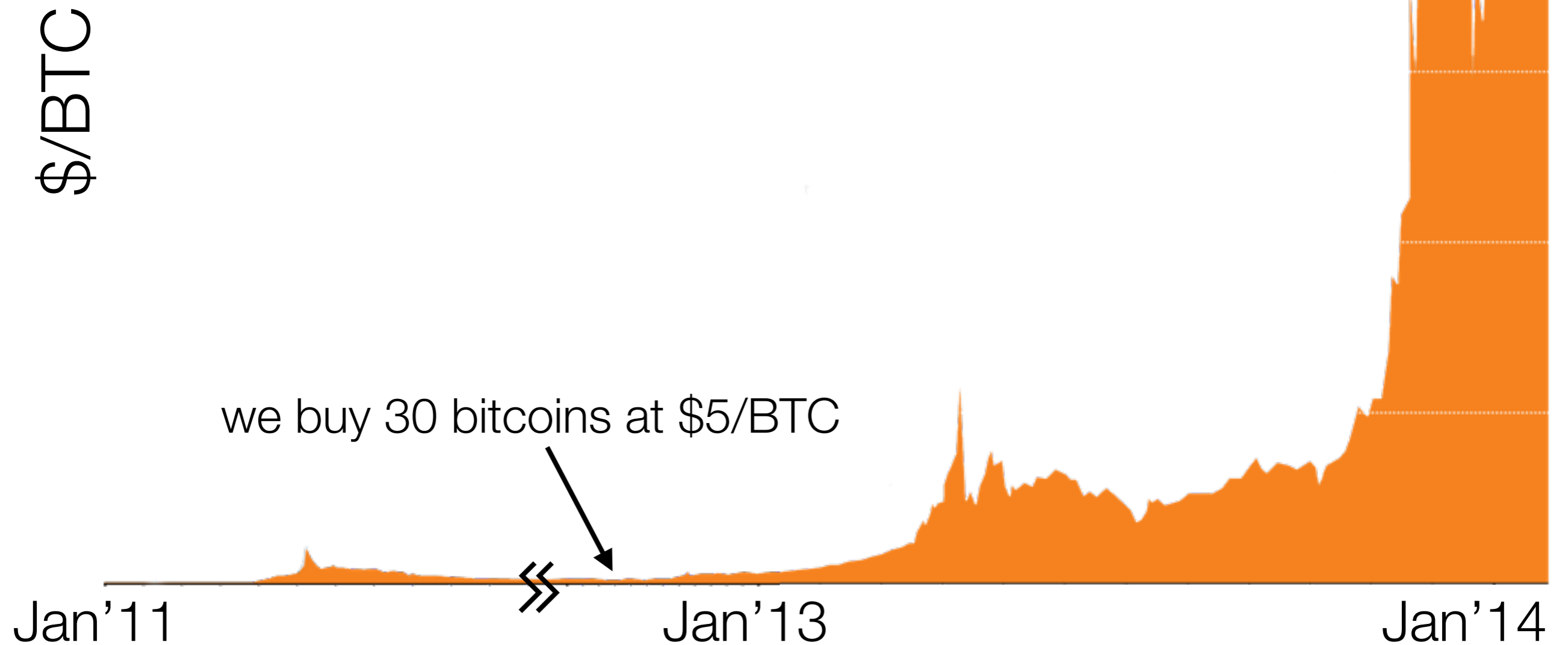
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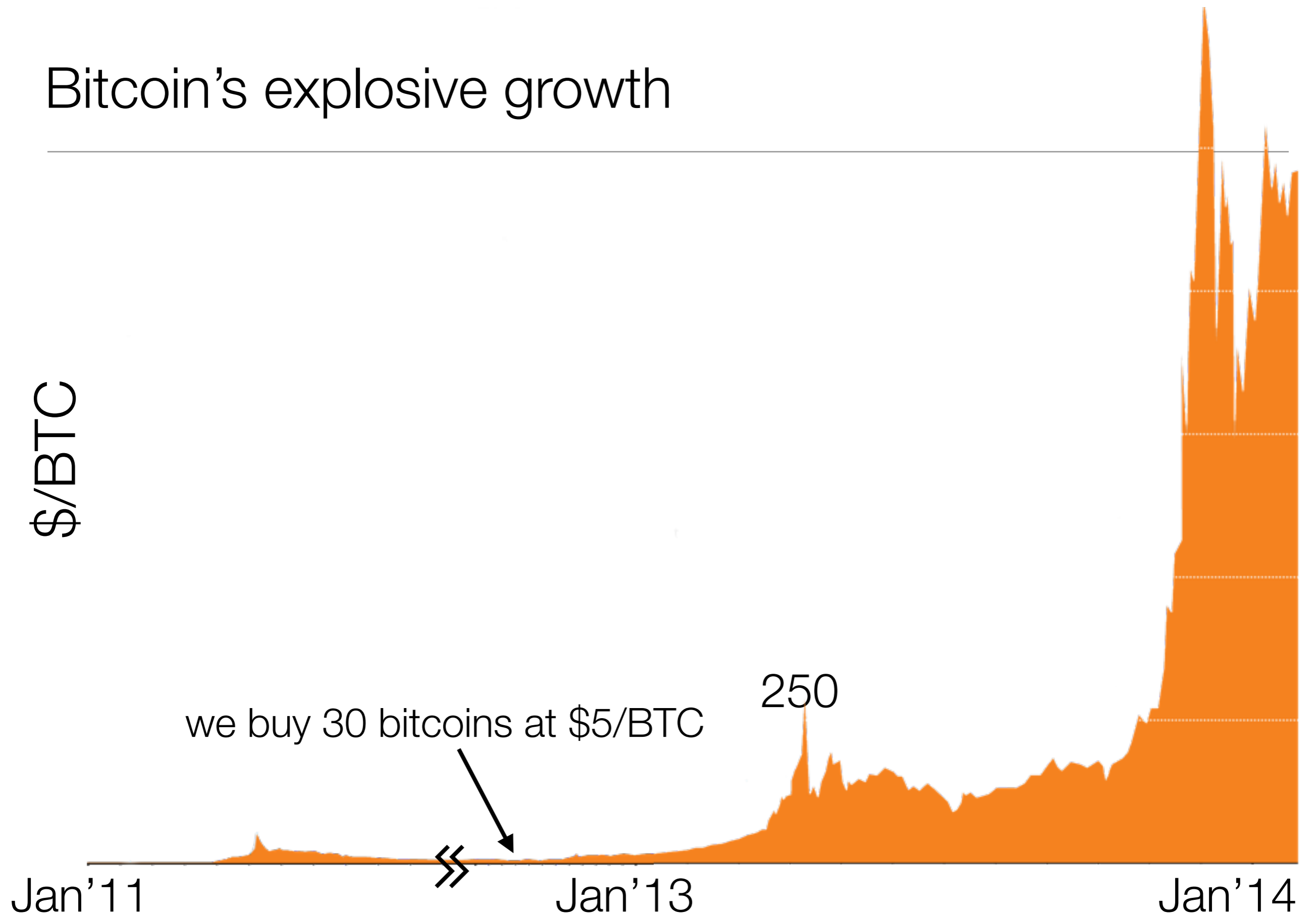


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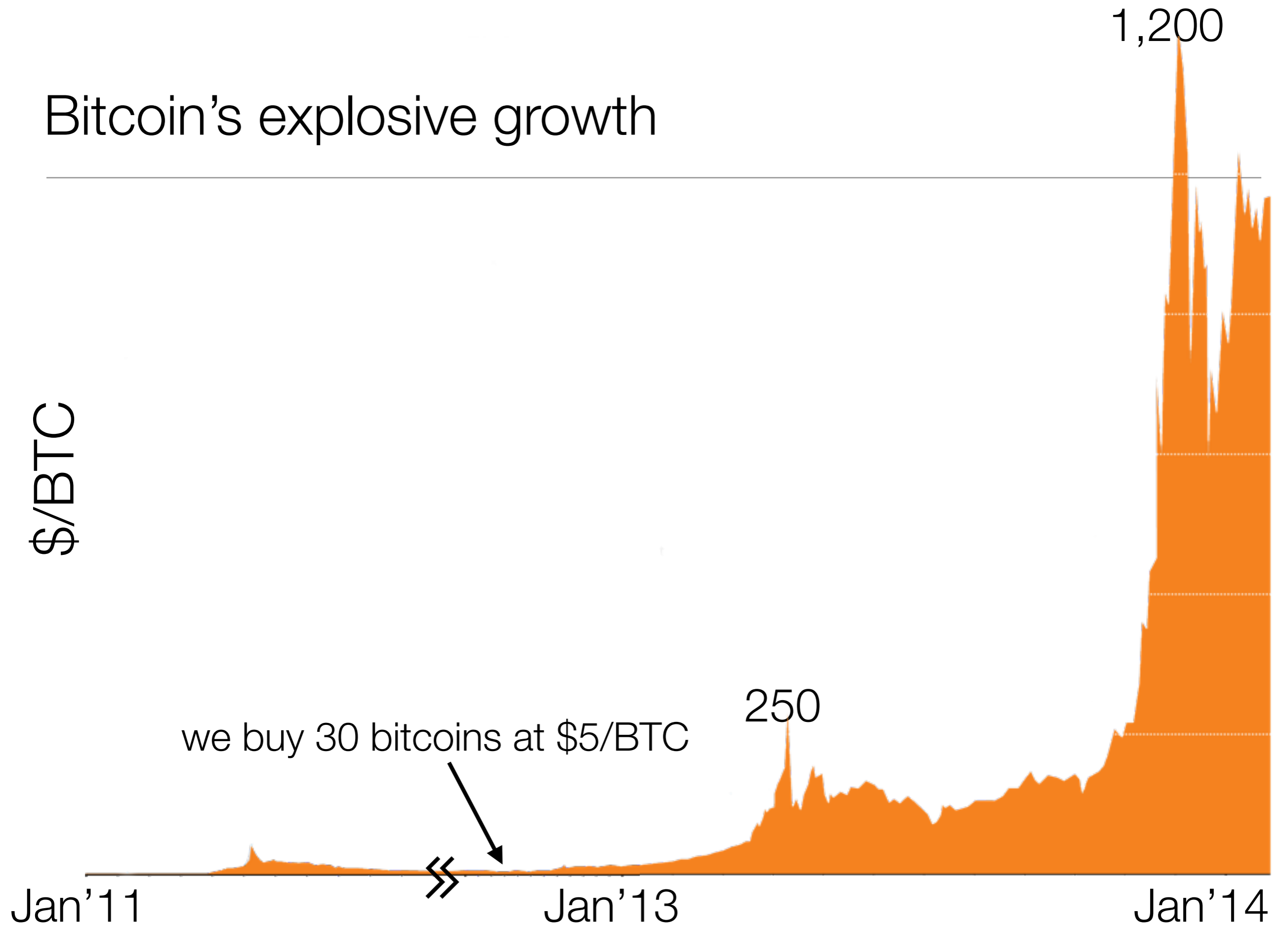
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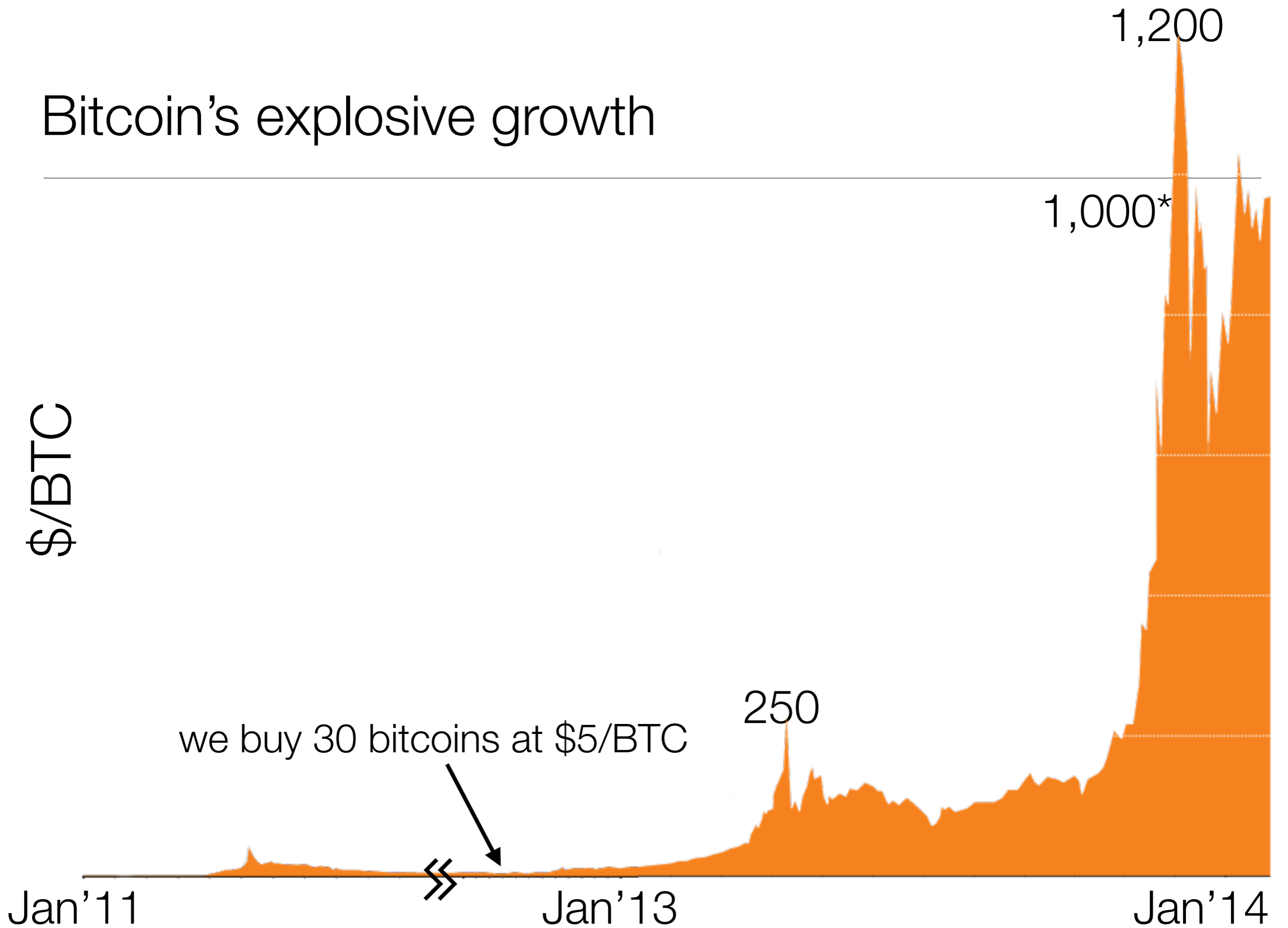
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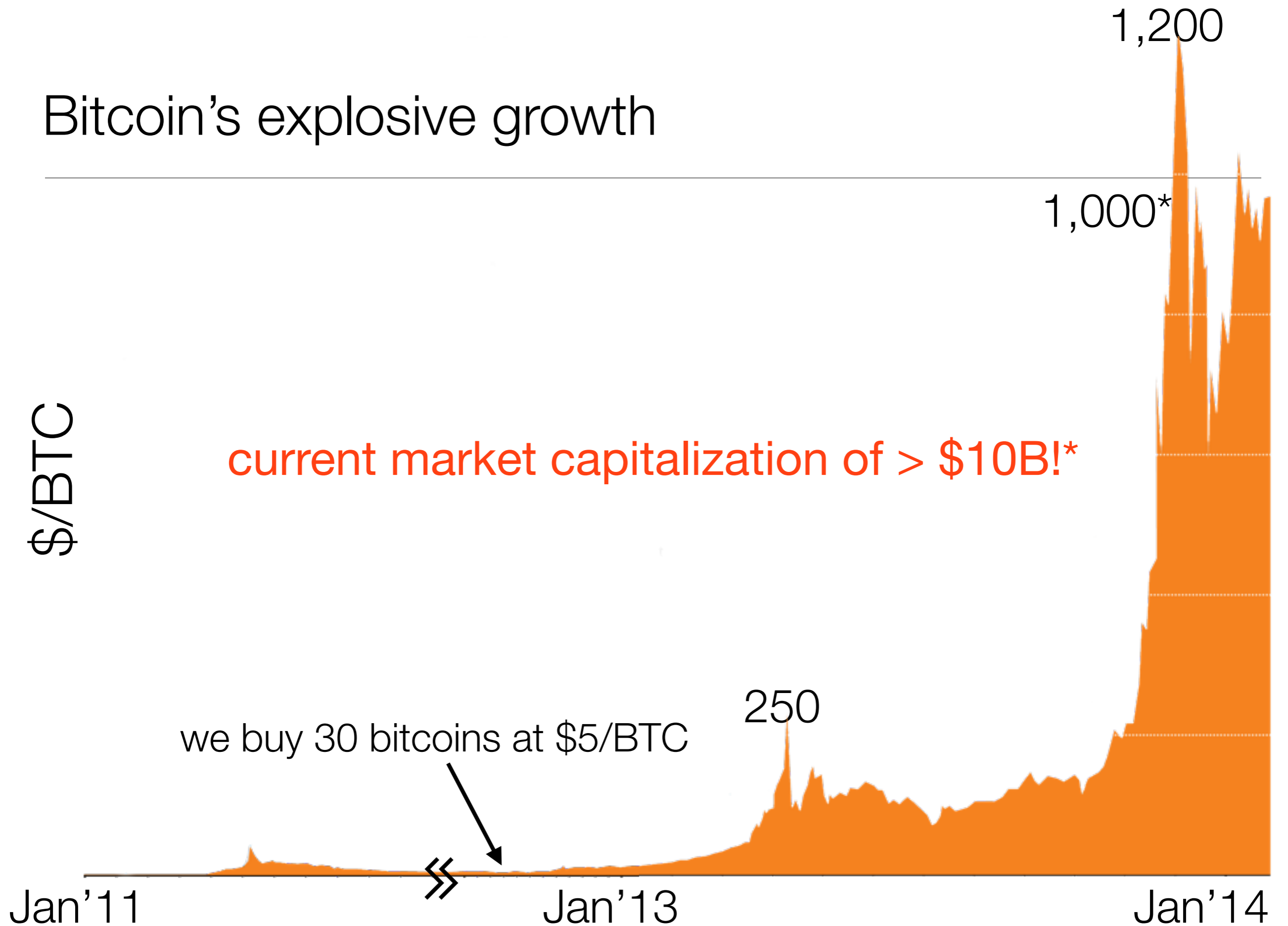


# Bitcoin's explosive growth





# Bitcoin's explosive growth



# How does Bitcoin work?

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# How does Bitcoin work?

- decentralized



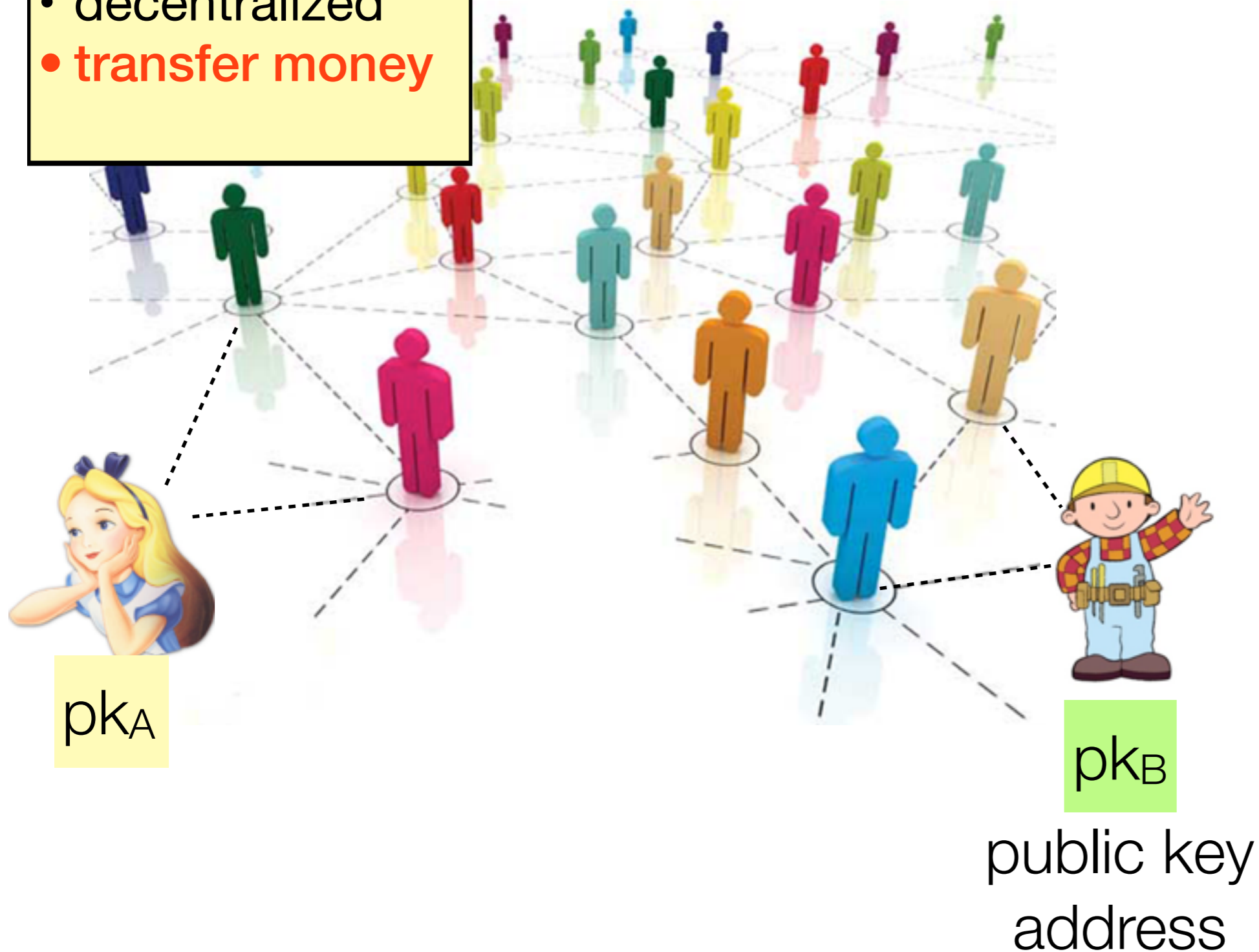
# How does Bitcoin work?

- decentralized
- **transfer money**



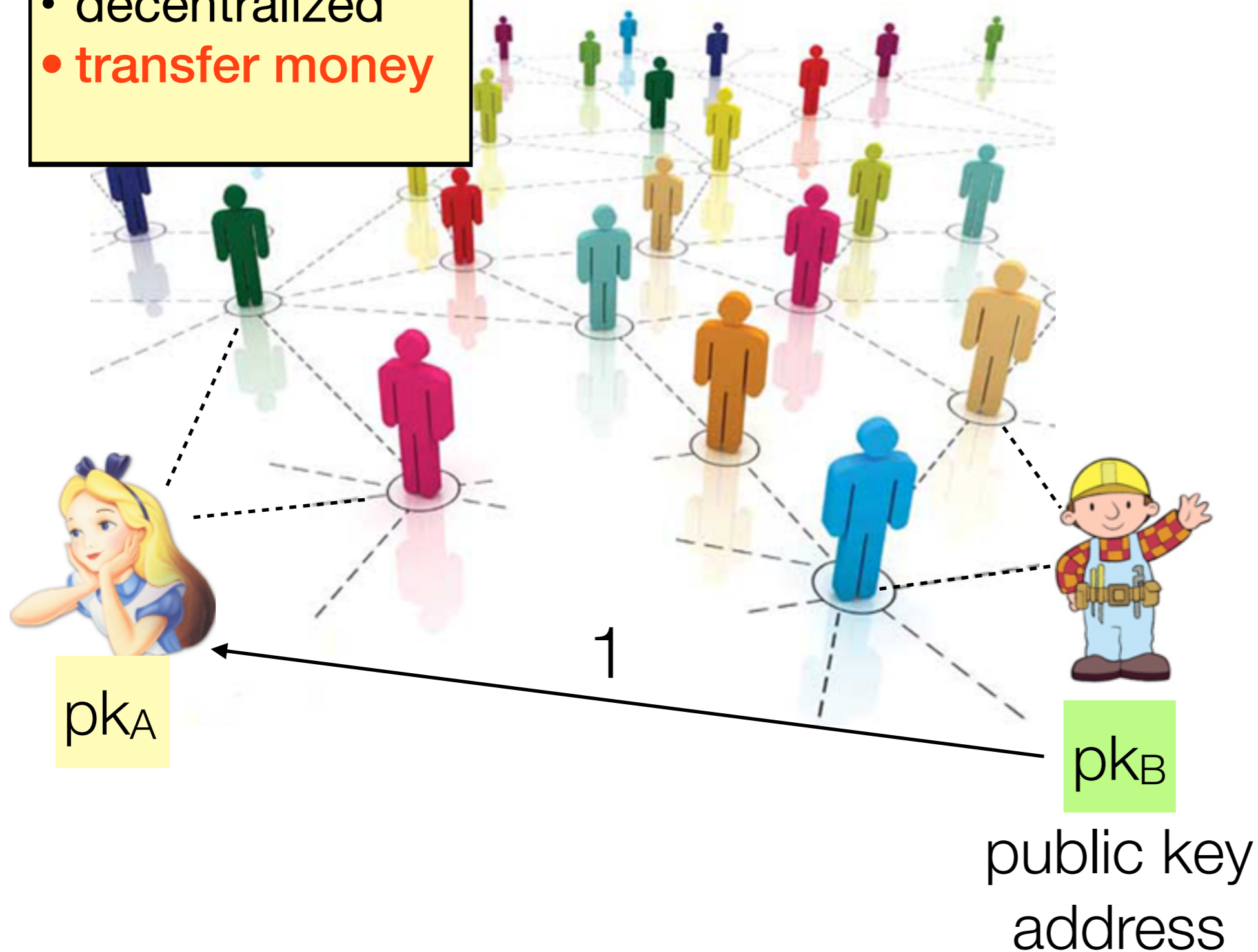
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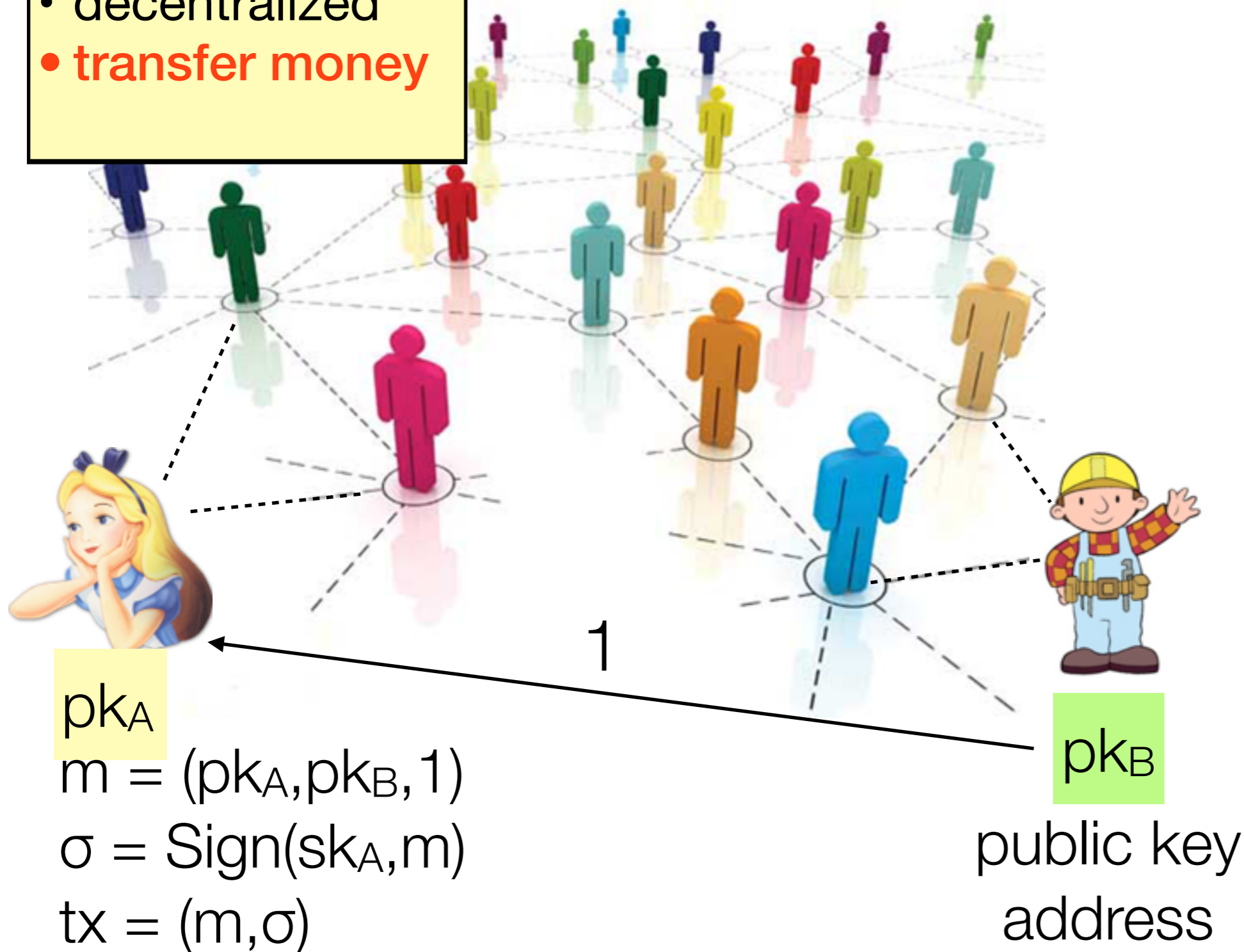
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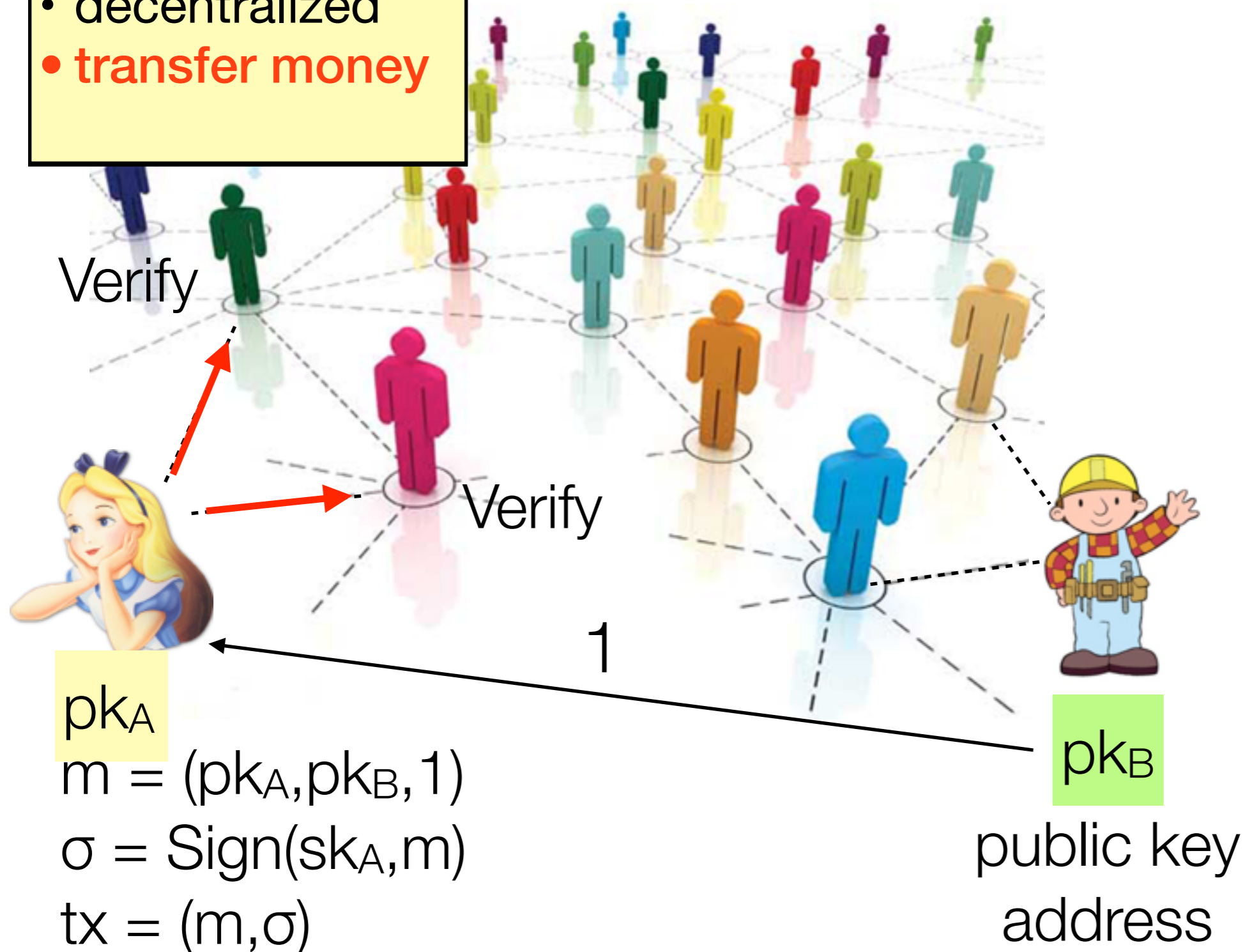
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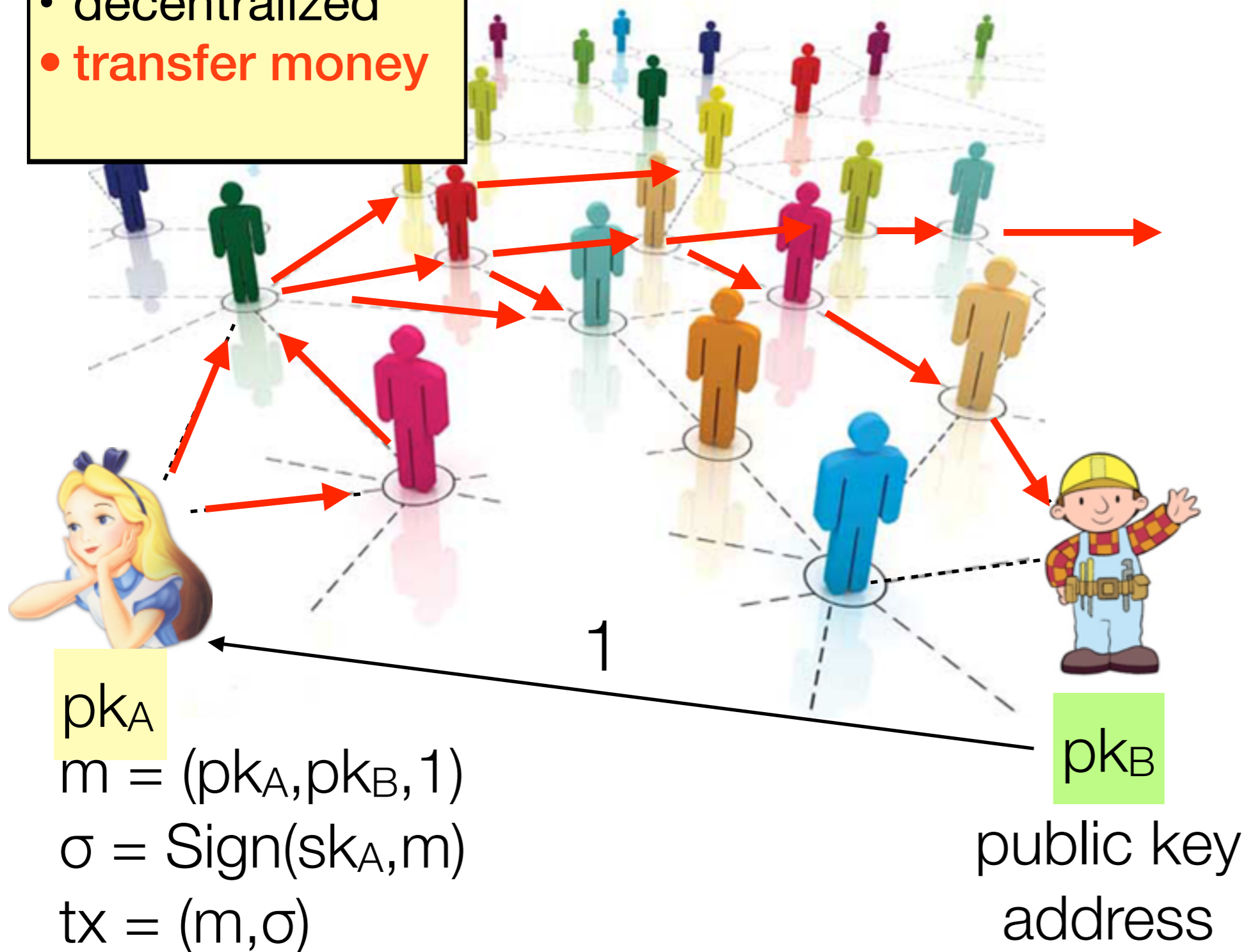
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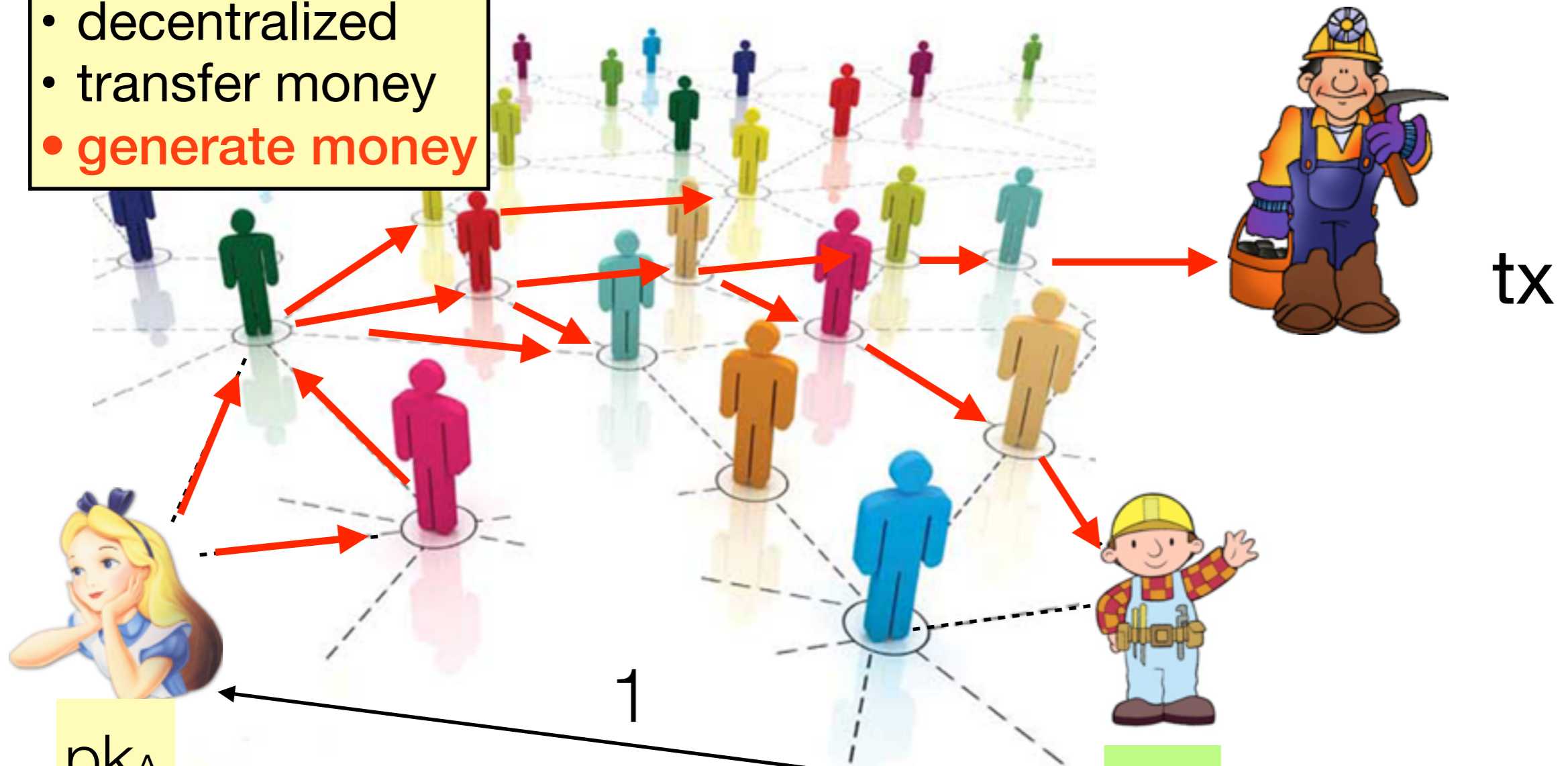
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- decentralized
- transfer money



# How does Bitcoin work?

- decentralized
- transfer money
- generate money



$pk_A$

$$m = (pk_A, pk_B, 1)$$

$$\sigma = \text{Sign}(sk_A, m)$$

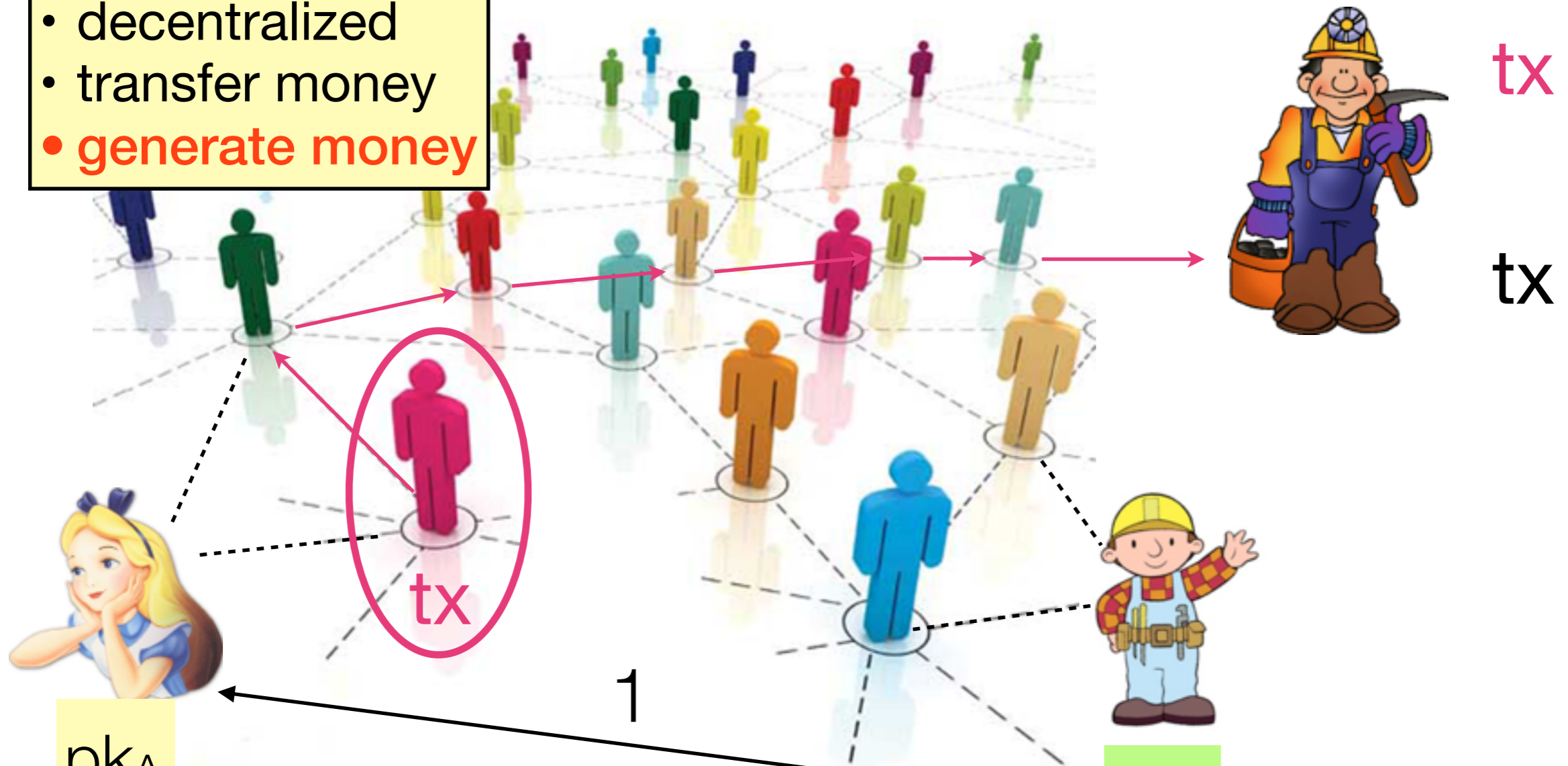
$$tx = (m, \sigma)$$

$pk_B$

public key  
address

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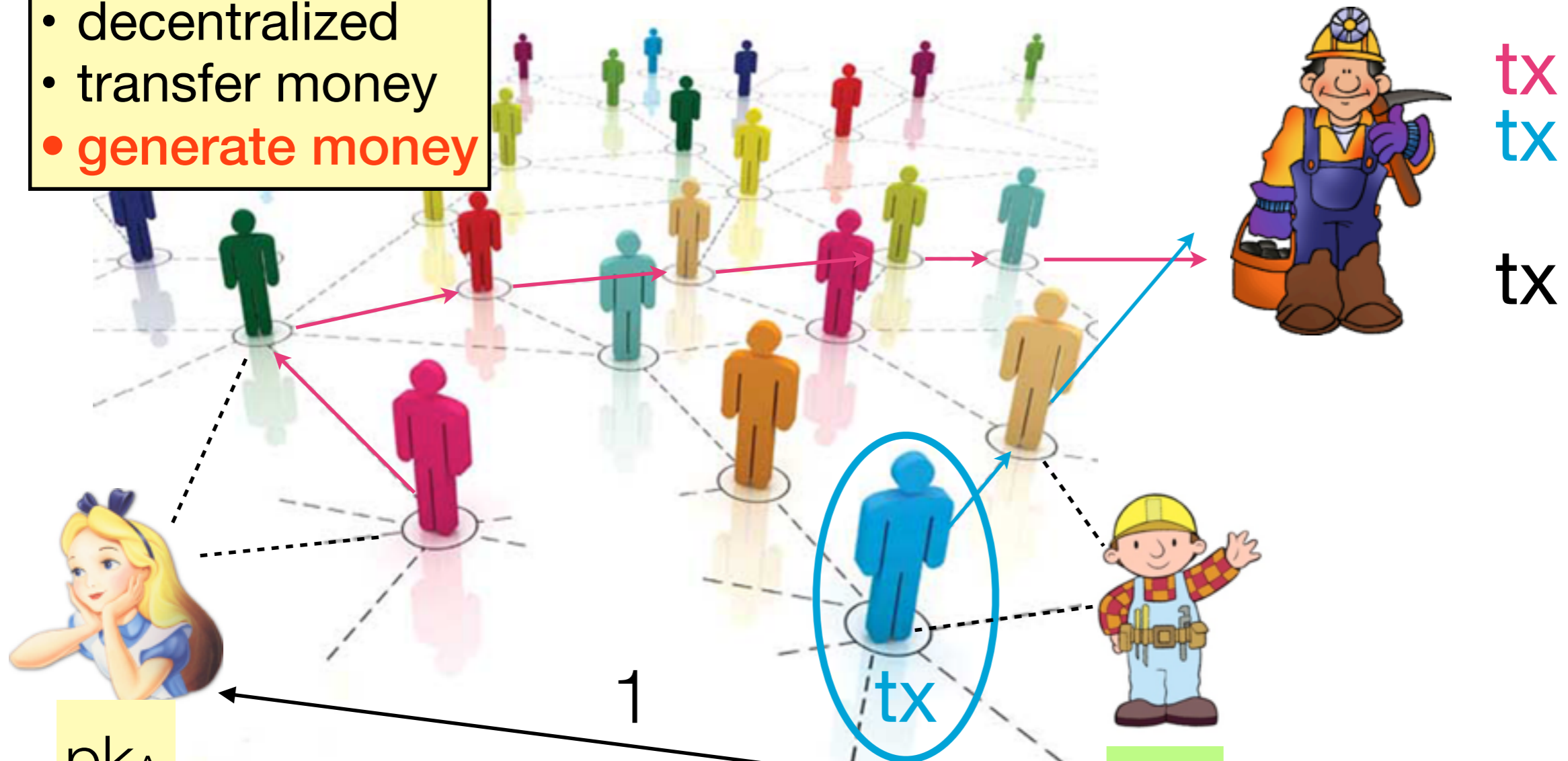
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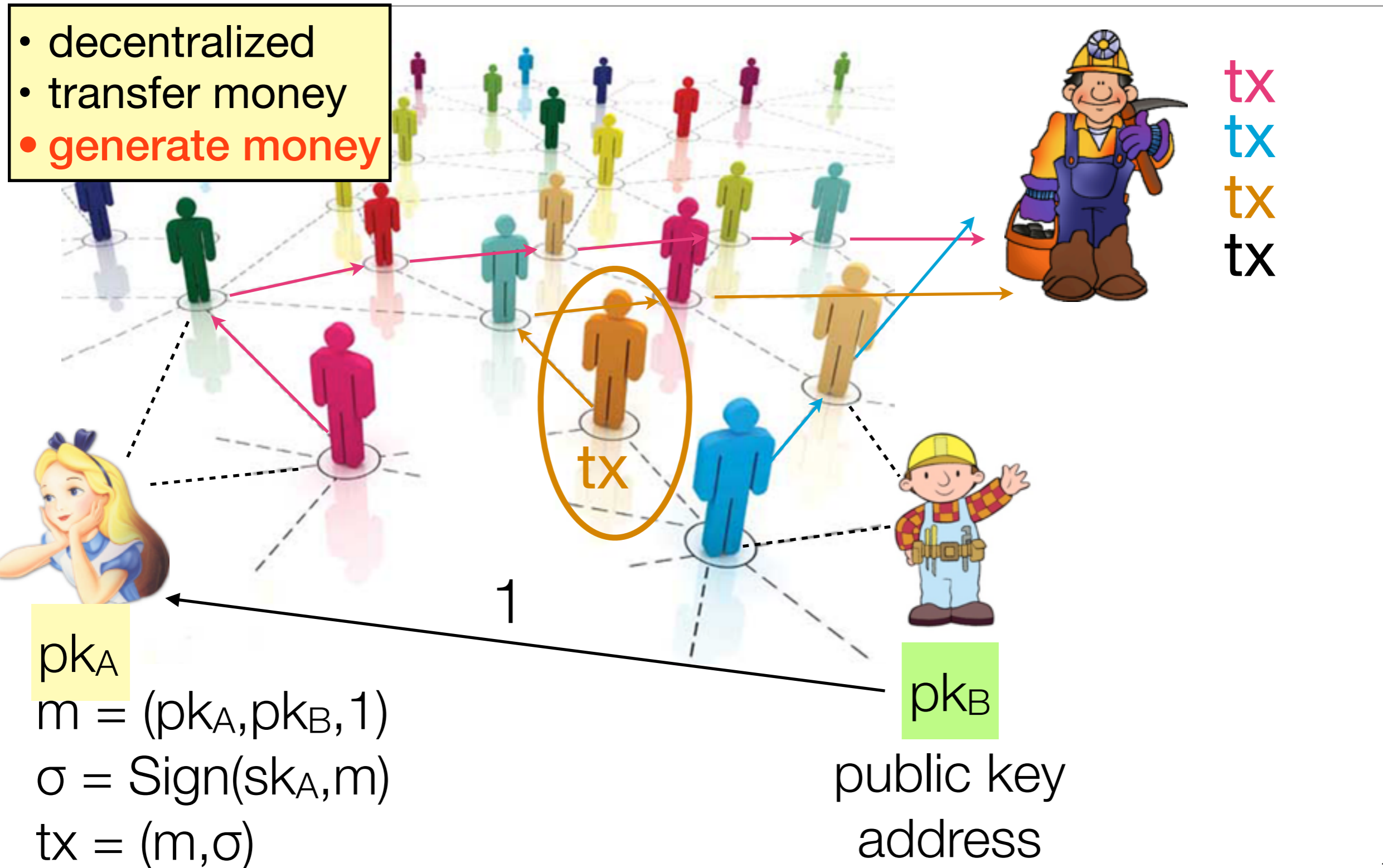
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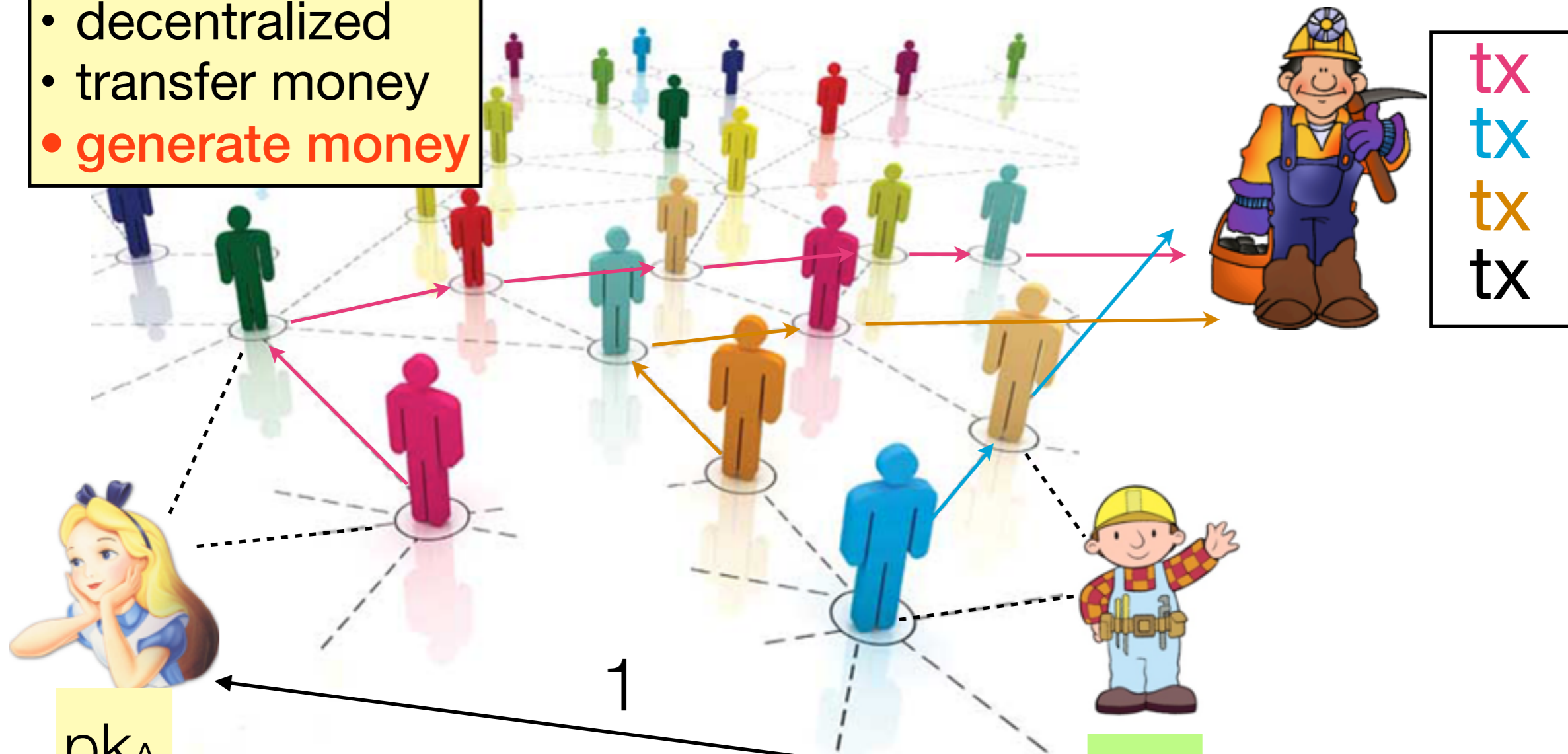
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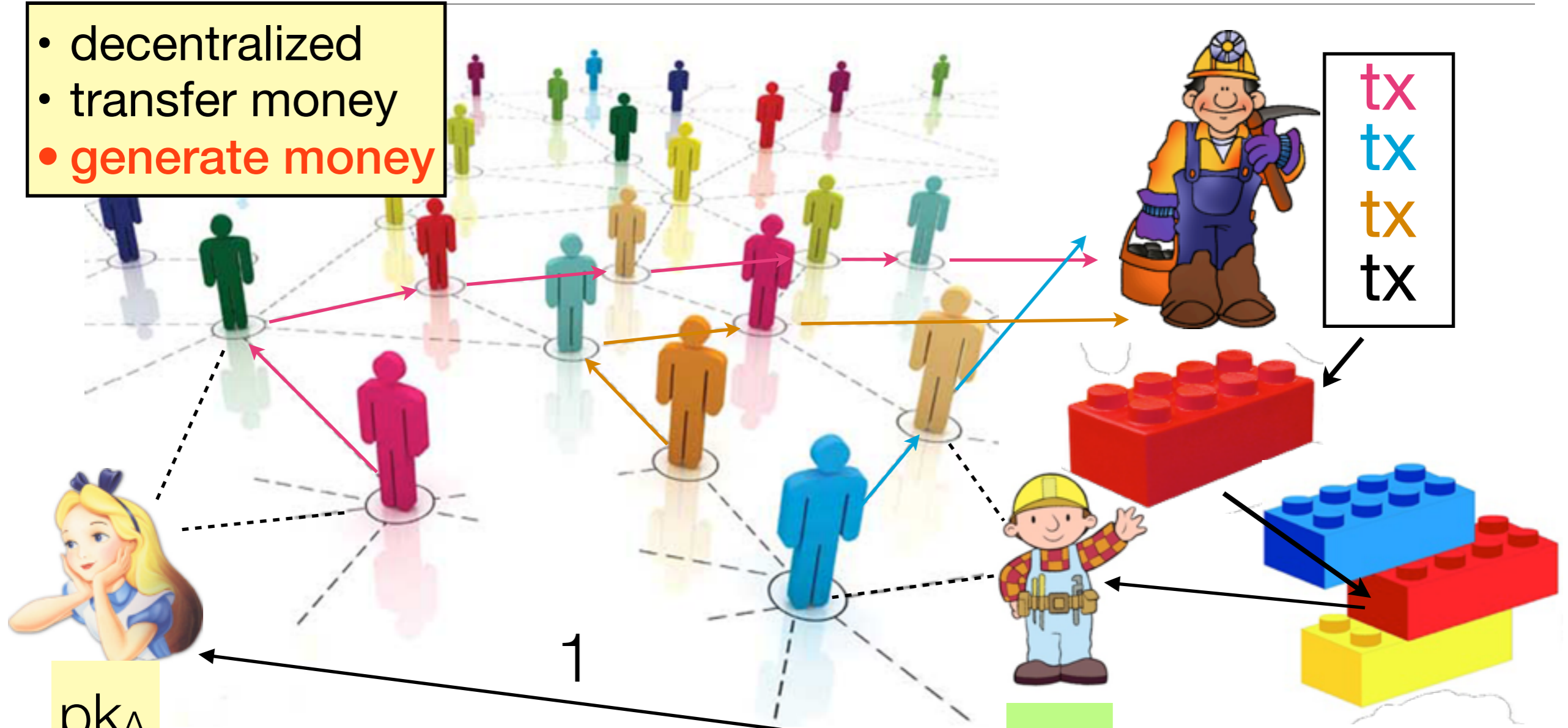
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$tx = (m, \sigma)$

$pk_B$

public key  
address

# How do bitcoins get spent?

---

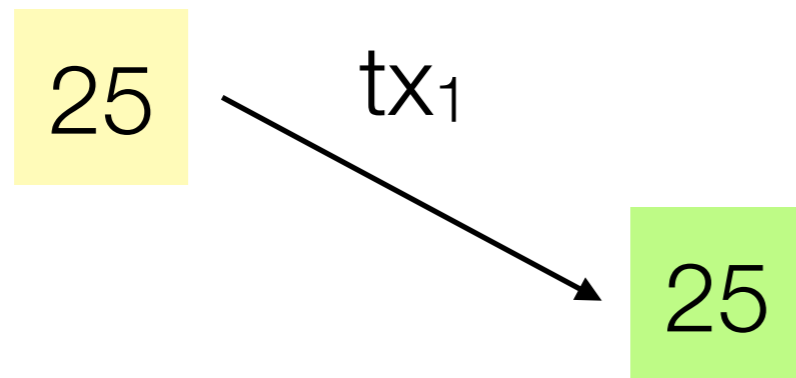
- decentralized
- transfer money
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- **prevent double-spending**



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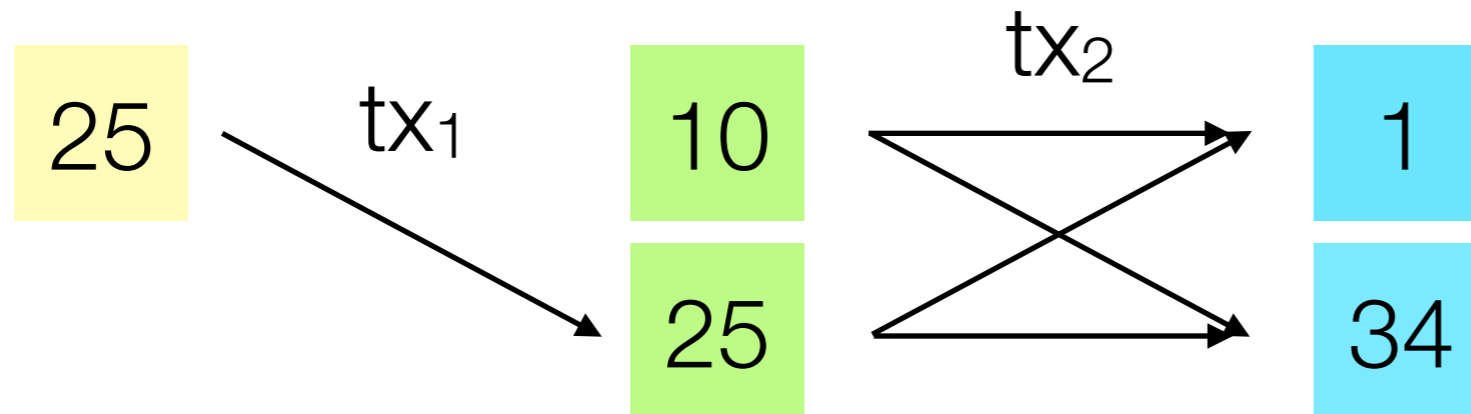
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- decentralized
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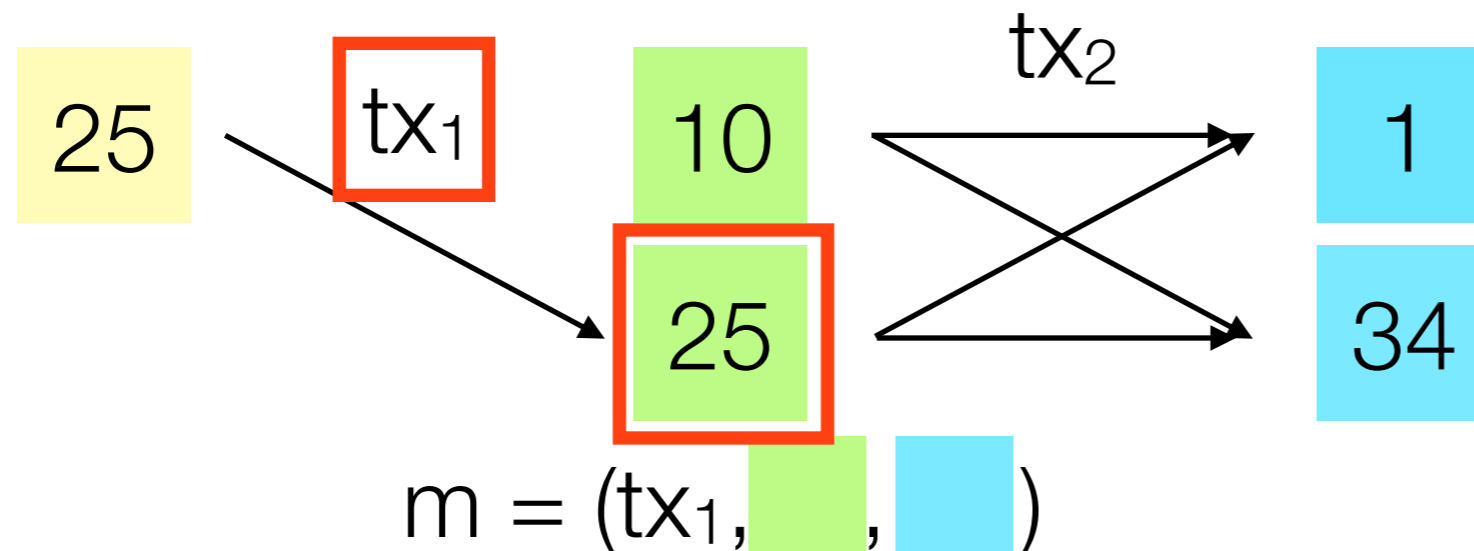
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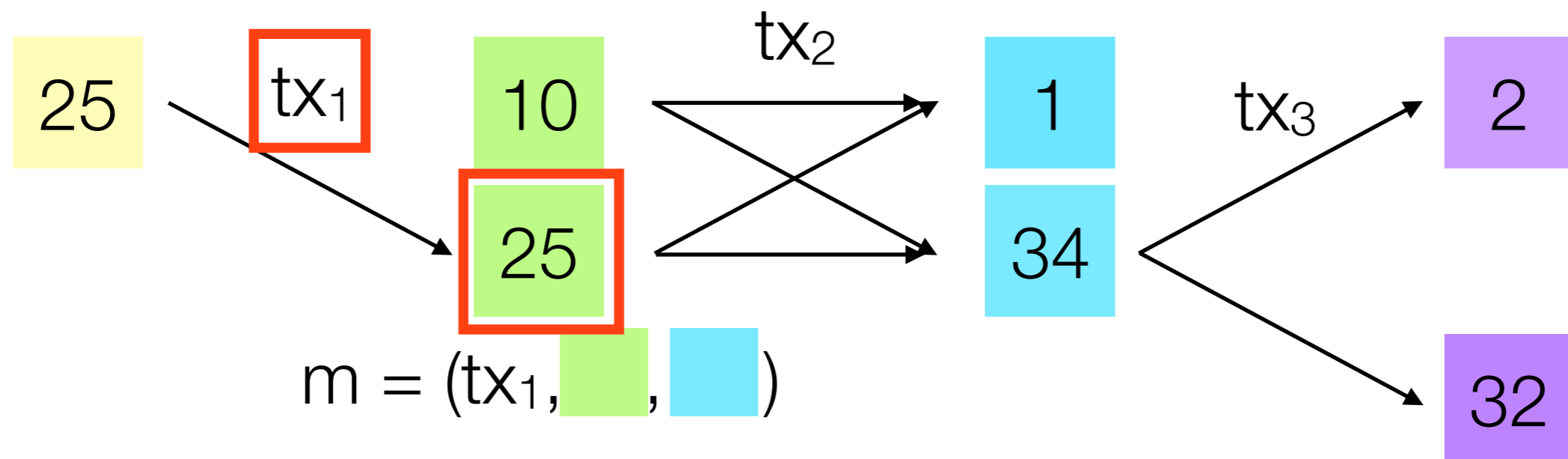
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To **spend bitcoins**, a user must indicate the **previous transaction**

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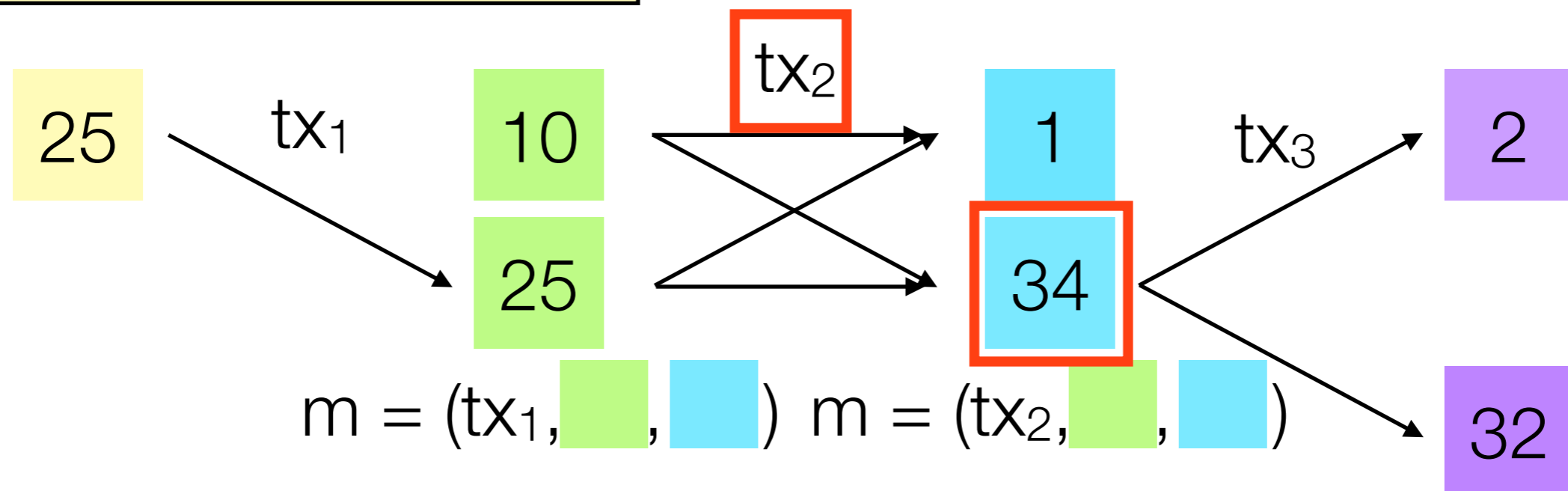
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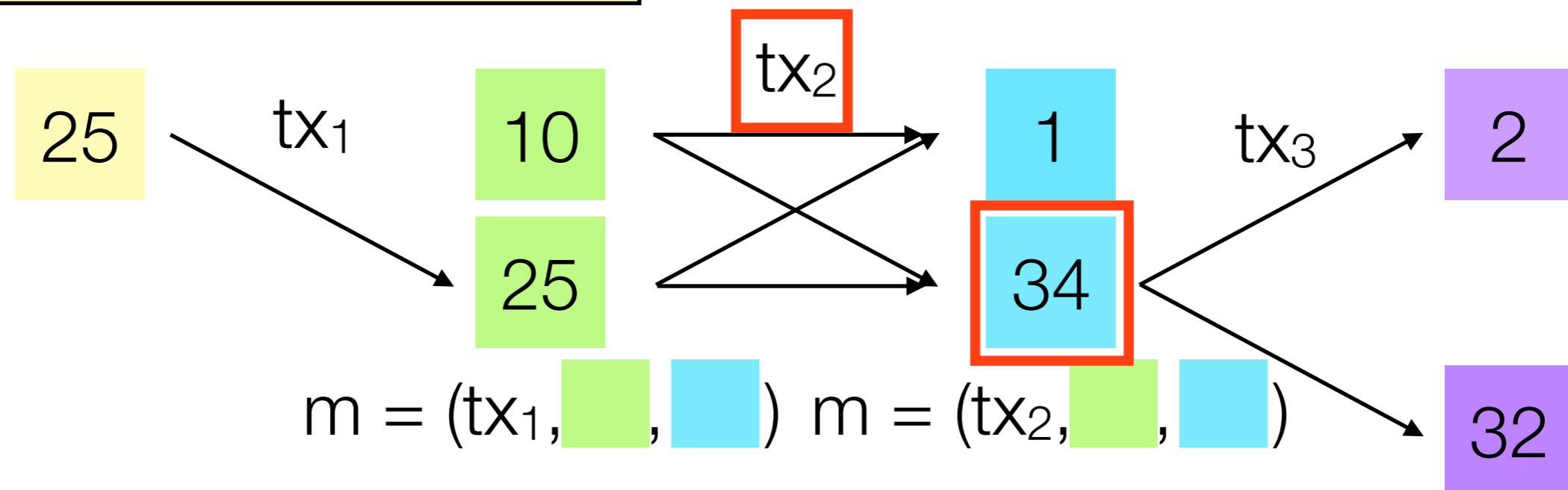
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# How do bitcoins get spent?

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- transfer money
- generate money
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To **spend bitcoins**, a user must indicate the **previous transaction**

All bitcoins received in a transaction **must be spent all at once**

# How to identify users? [MPGLMVS IMC13]

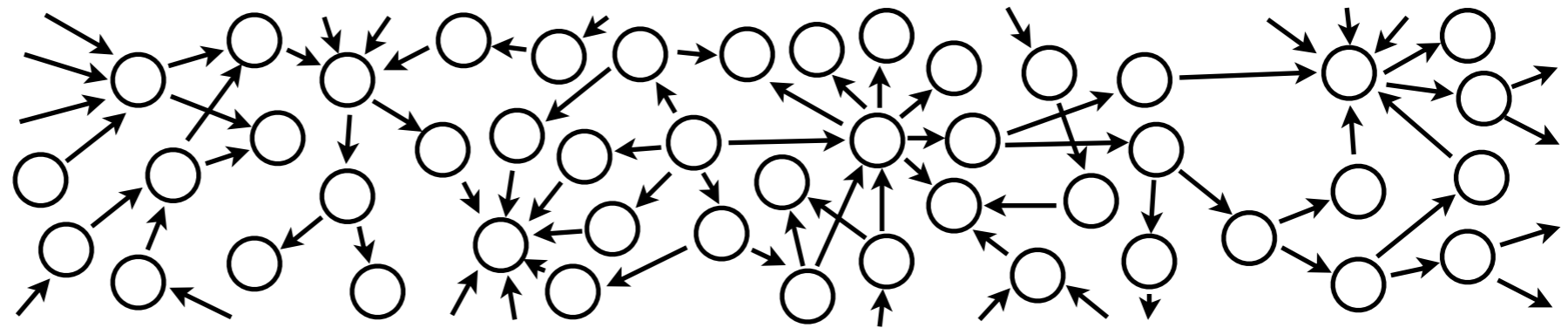
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Users can use **arbitrarily many public keys** (pseudonyms); as a result the Bitcoin graph is complicated and has **12 million public keys**

# How to identify users? [MPGLMVS IMC13]

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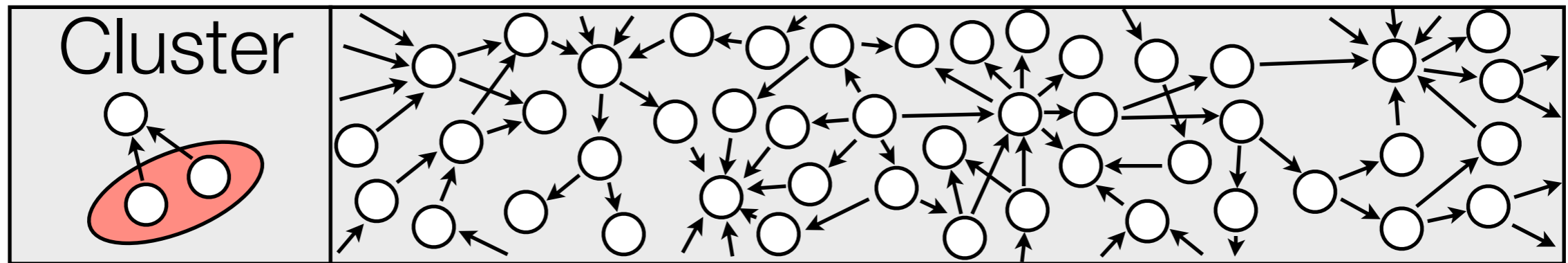
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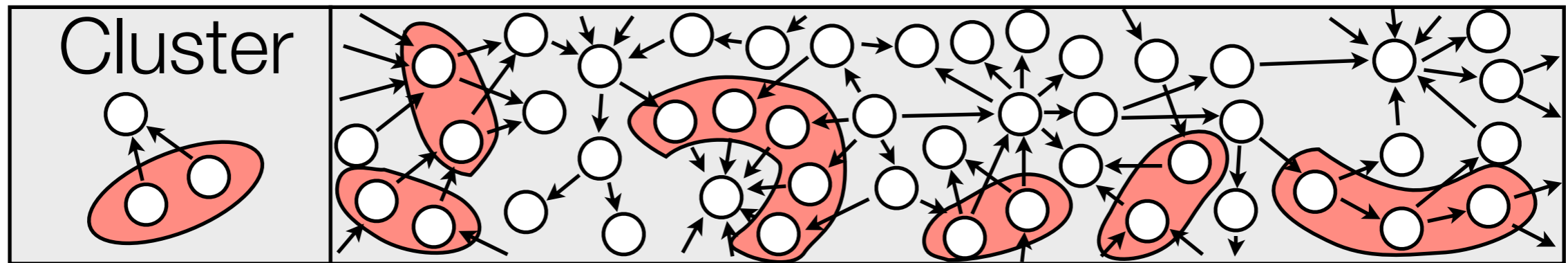
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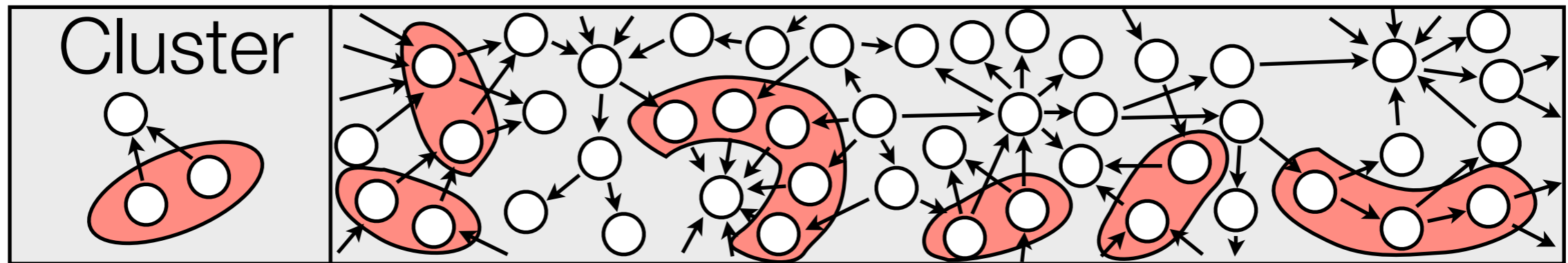
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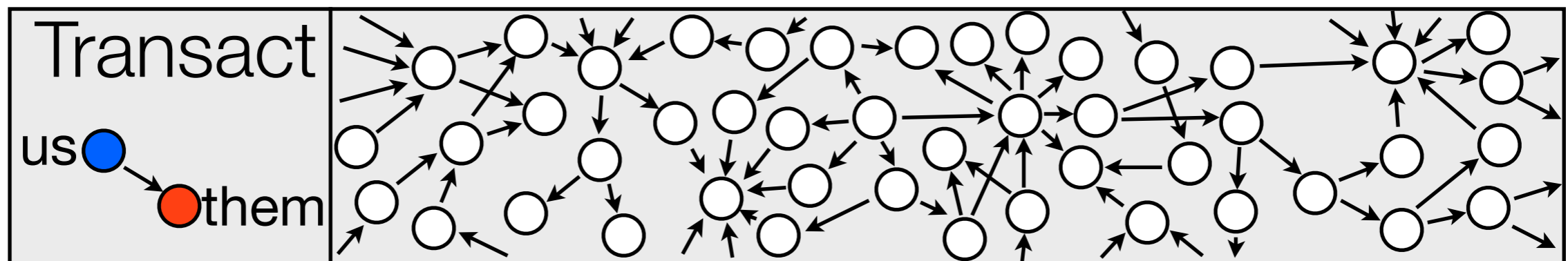
Collapse into a more manageable graph of **clusters of public keys** representing distinct entities

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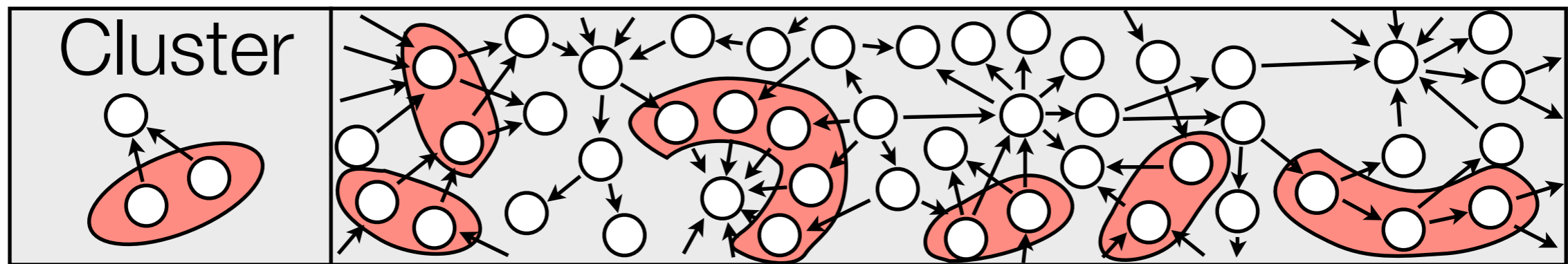


Collapse into a more manageable graph of **clusters of public keys** representing distinct entities

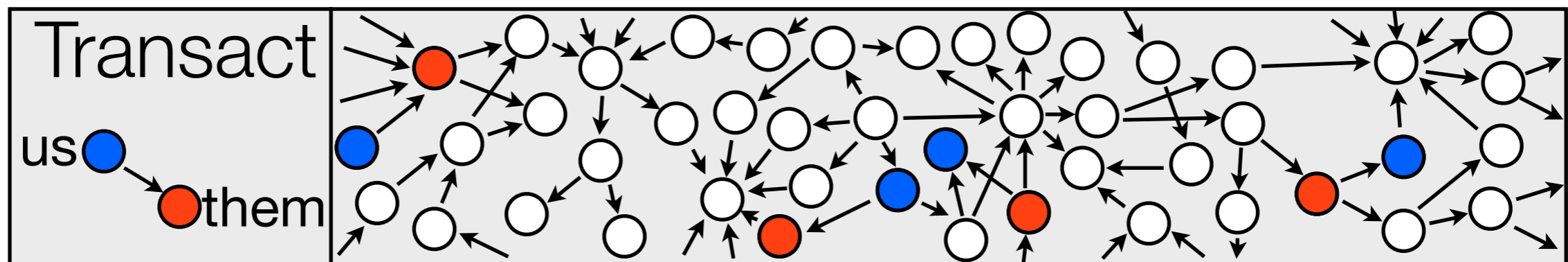


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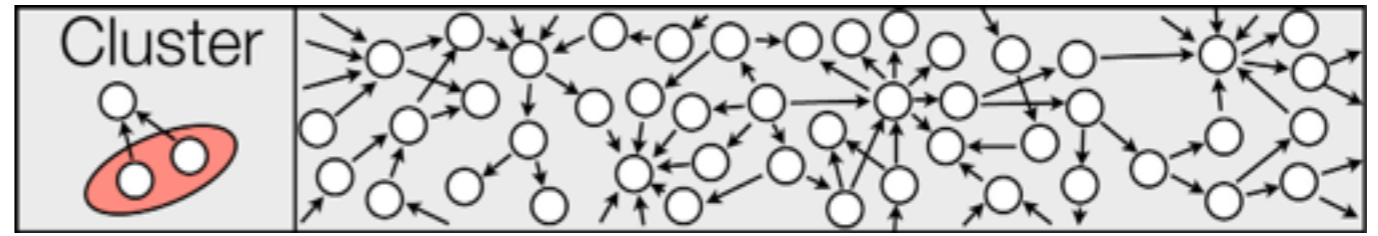
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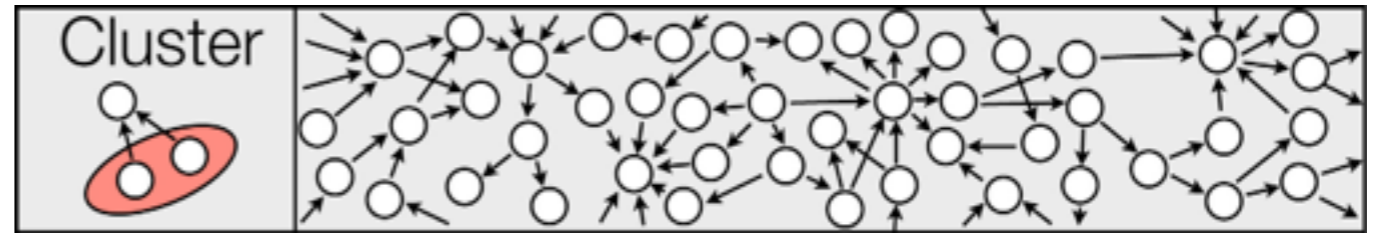
Collect **ground truth data** by participating in transactions

# Clustering by inputs

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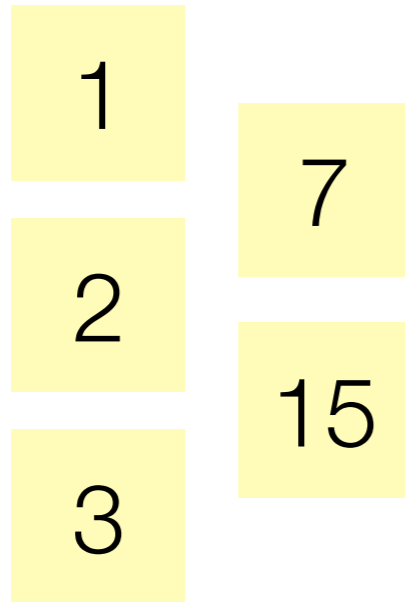
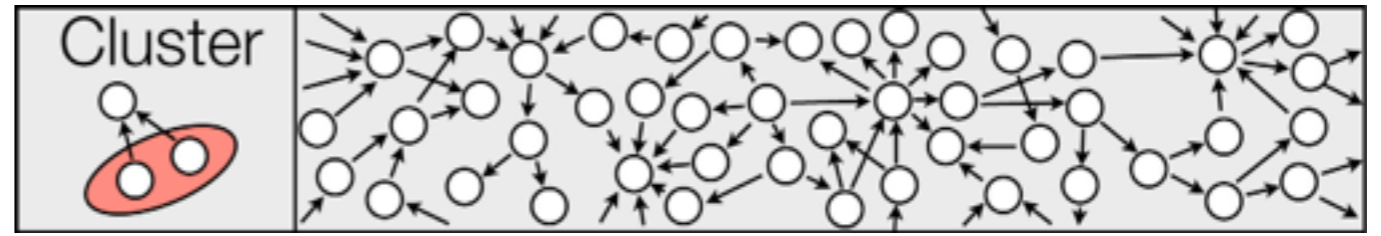
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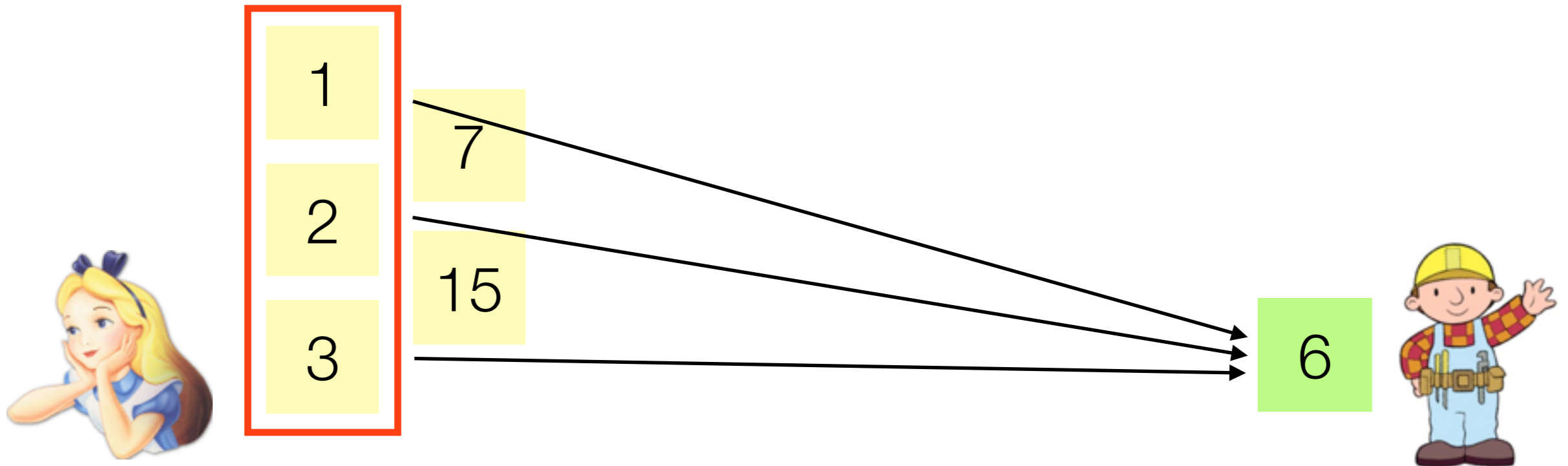
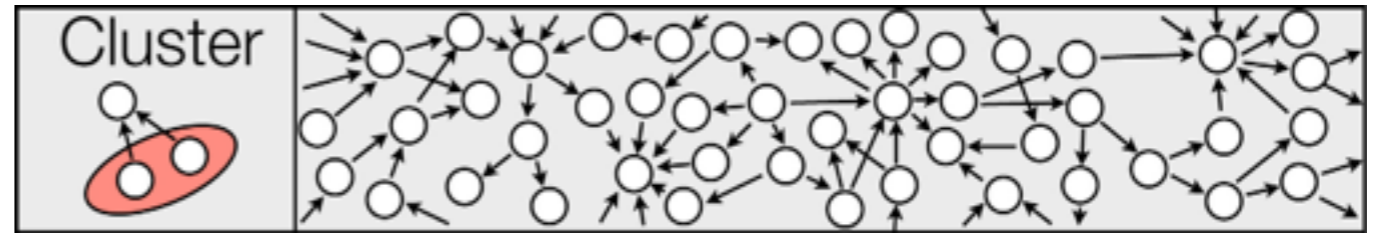
1	7
2	
3	15



# Clustering by inputs

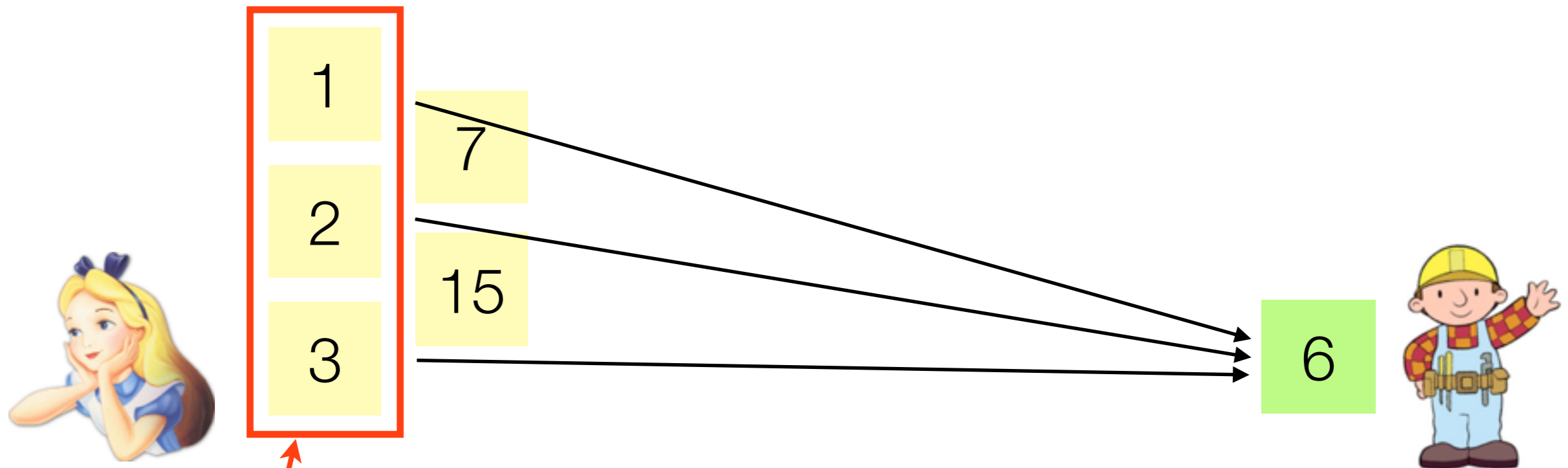
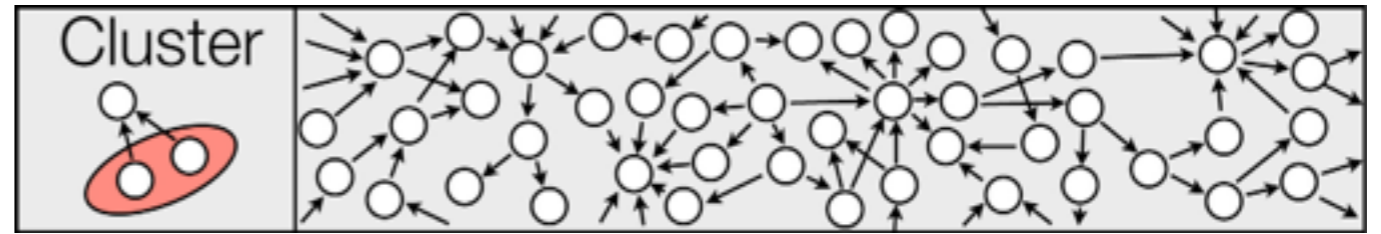


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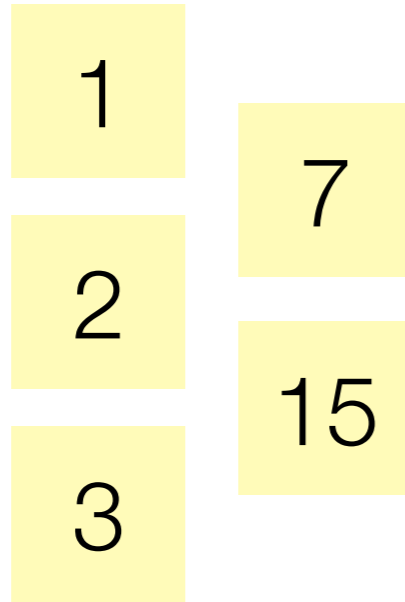
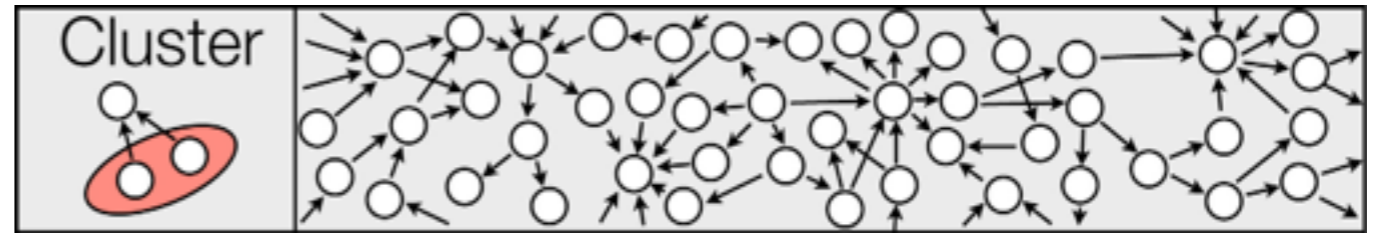


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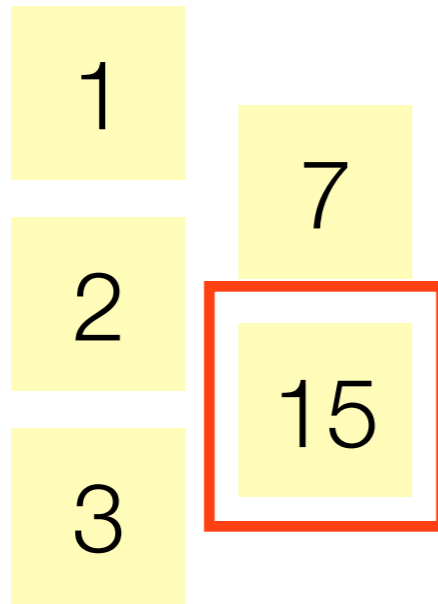
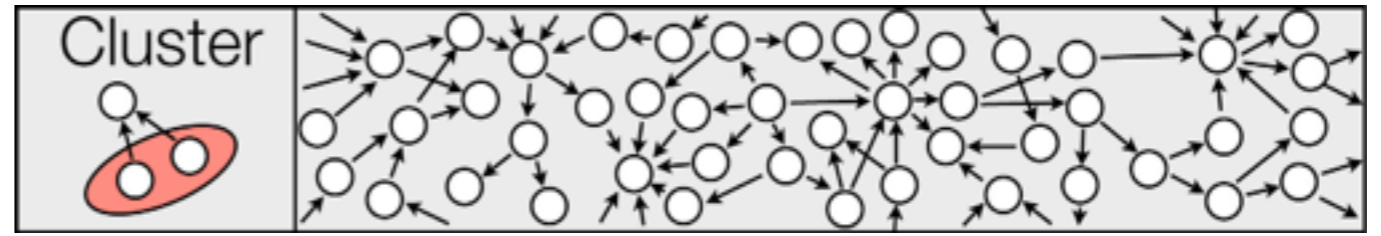


Heuristic #1: the same user controls these addresses  
[N08,RH11,RS13,A+13]

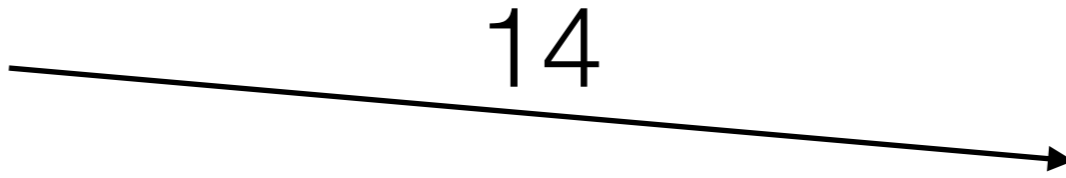
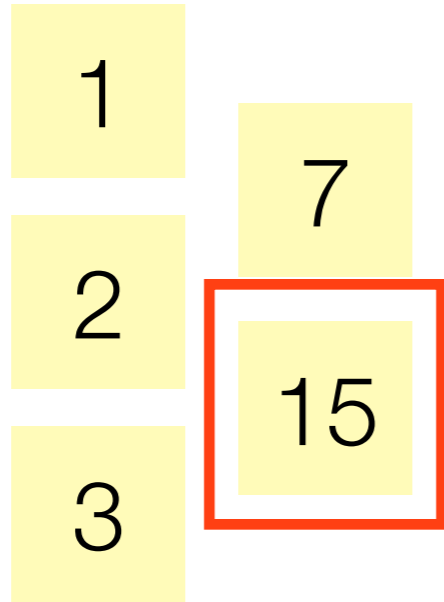
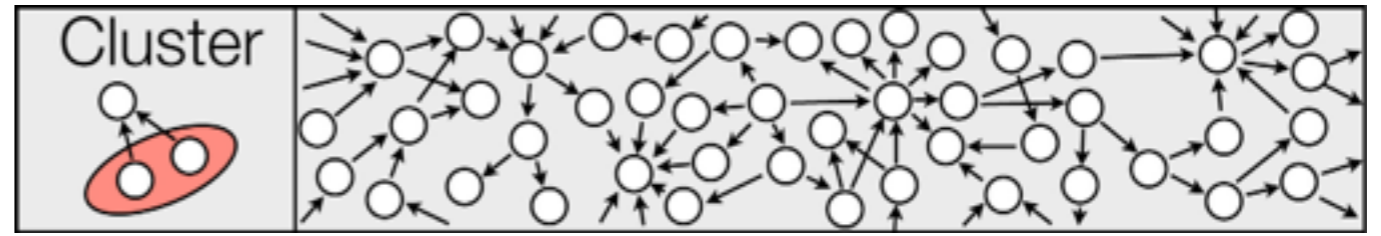
# Change addresses



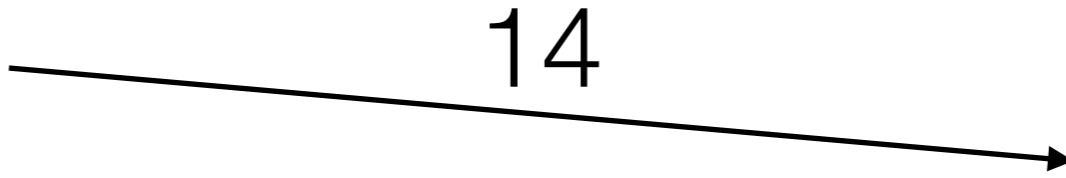
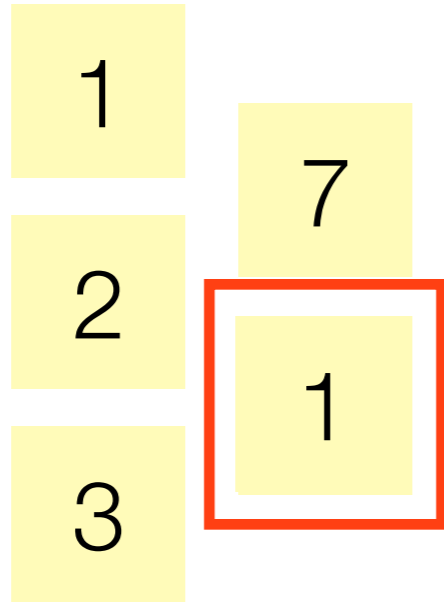
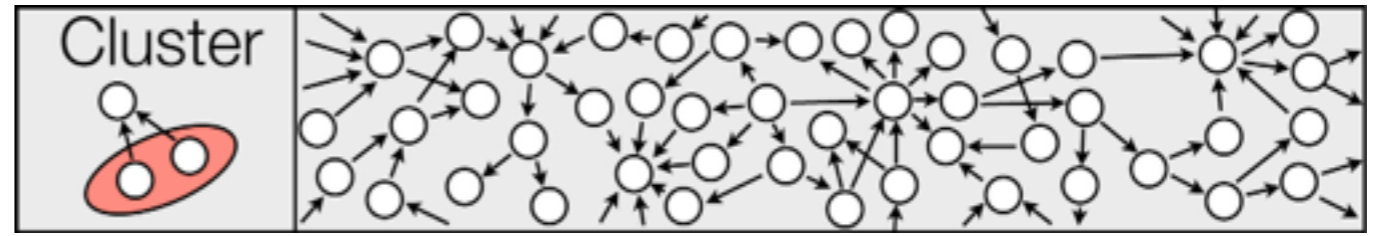
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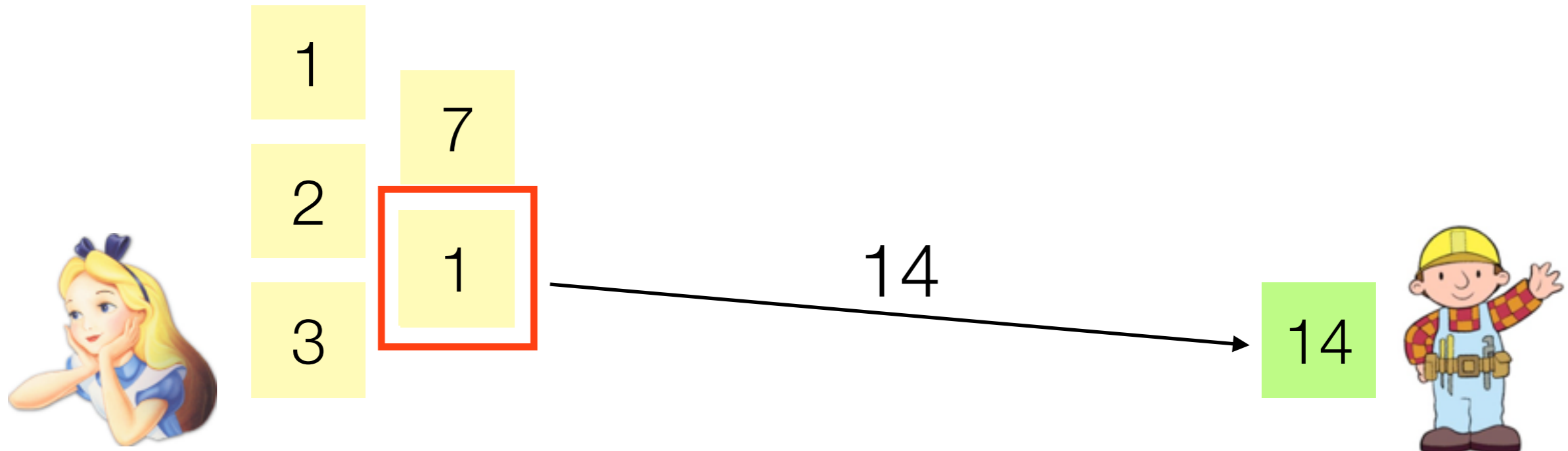
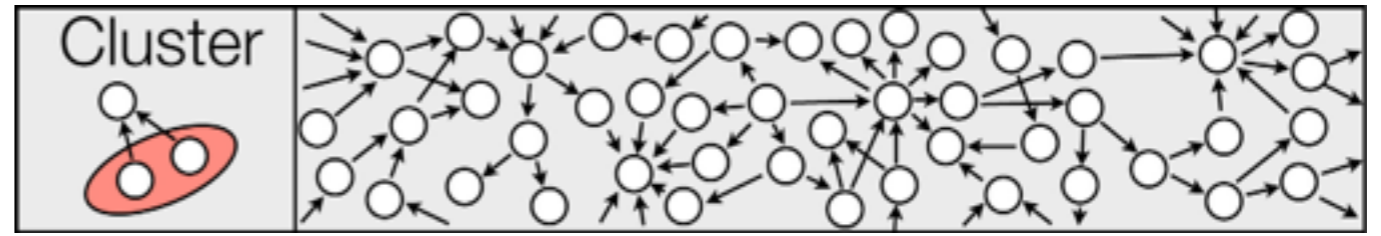
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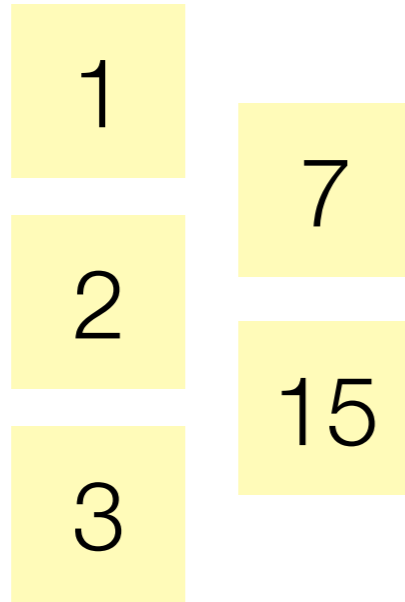
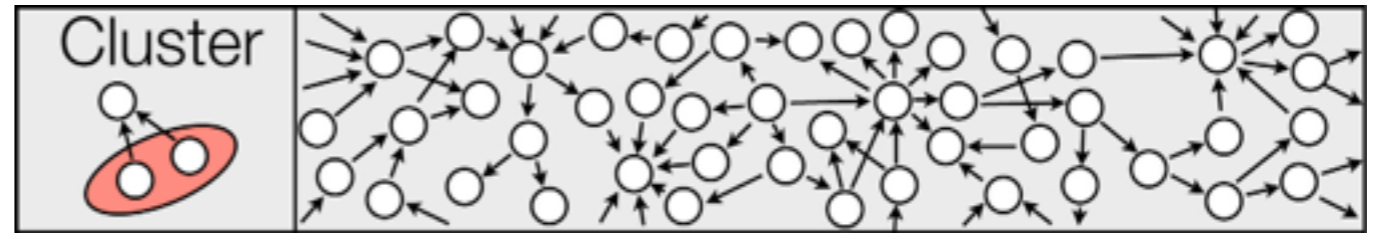


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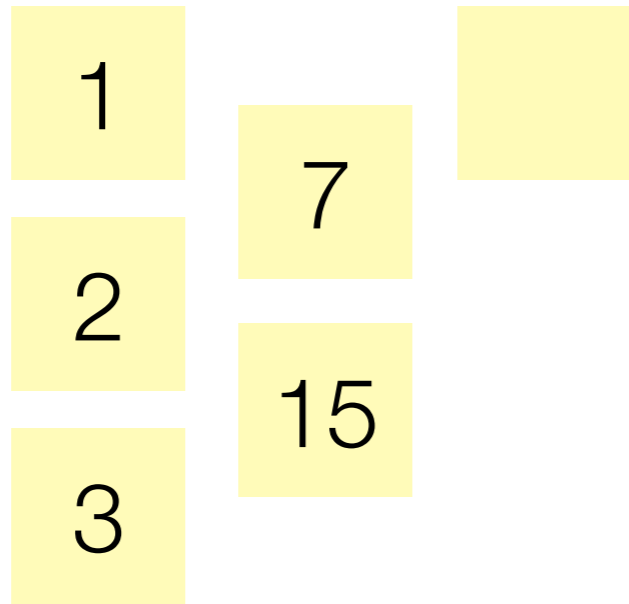
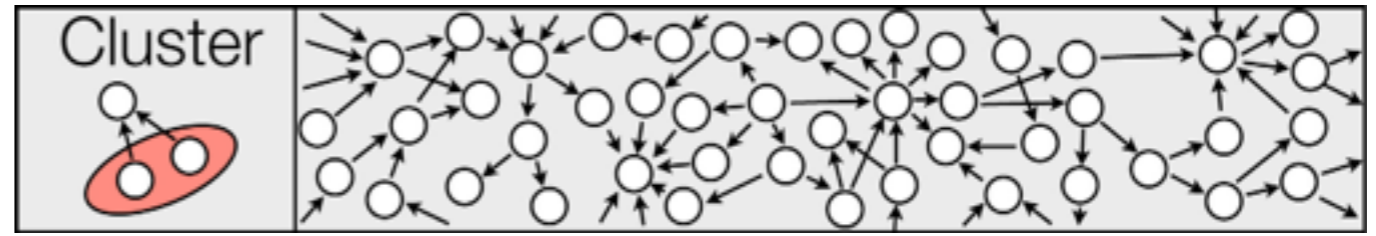
All bitcoins received in a transaction **must be spent all at once**

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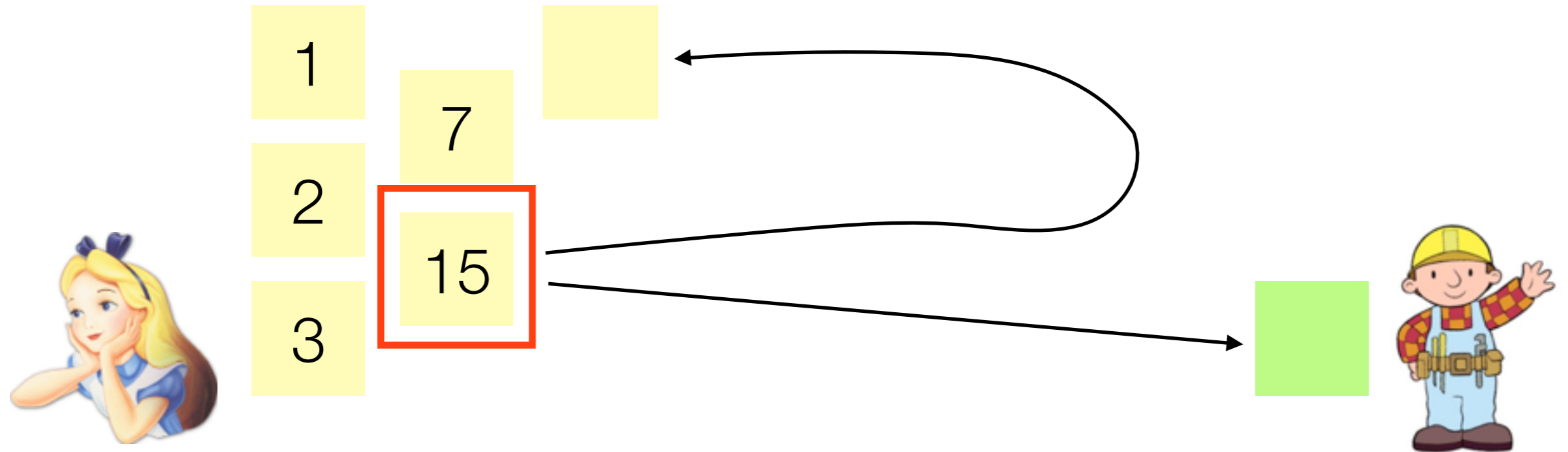
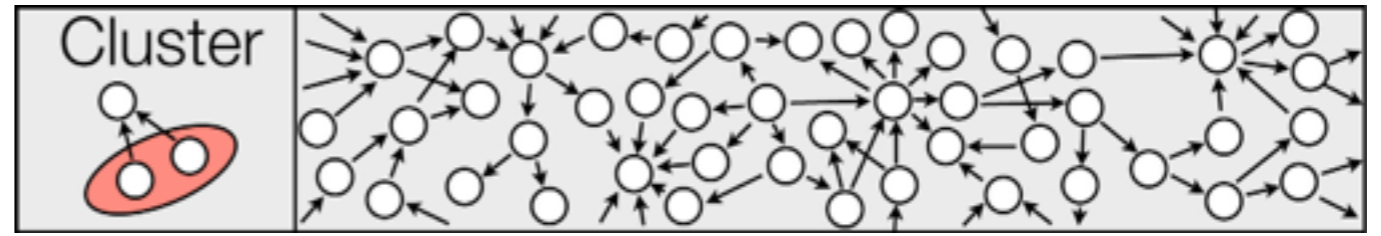
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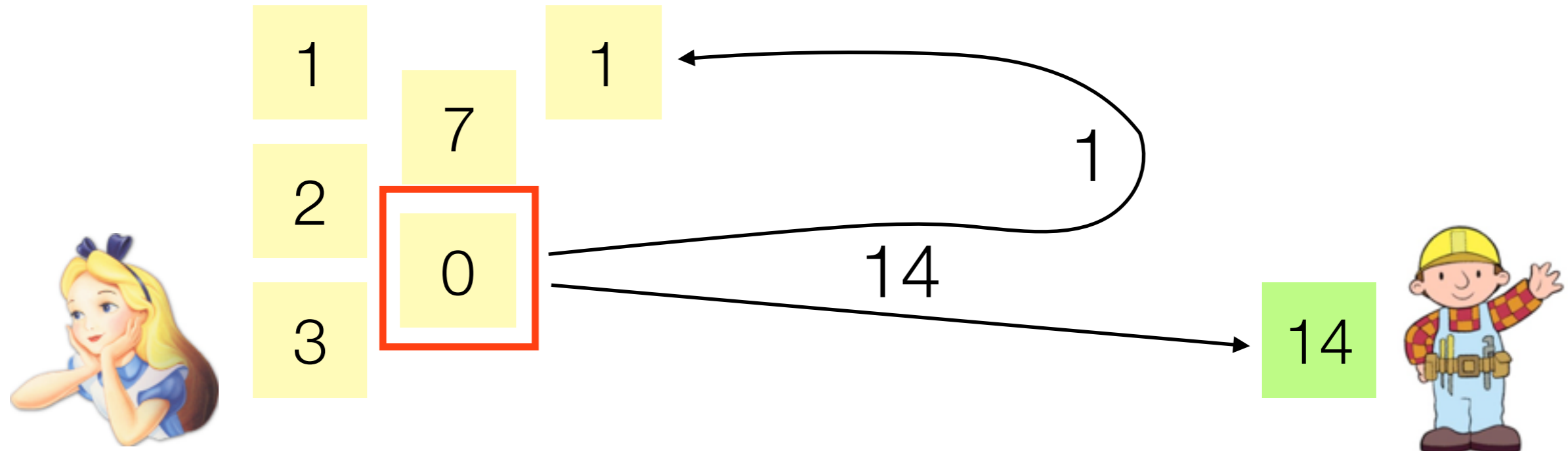
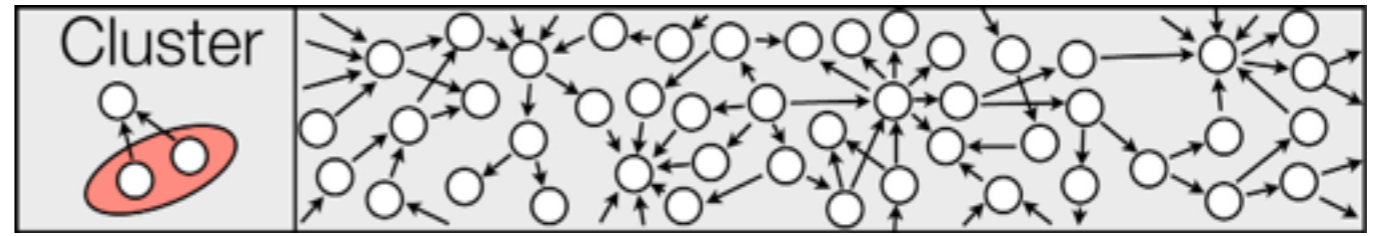


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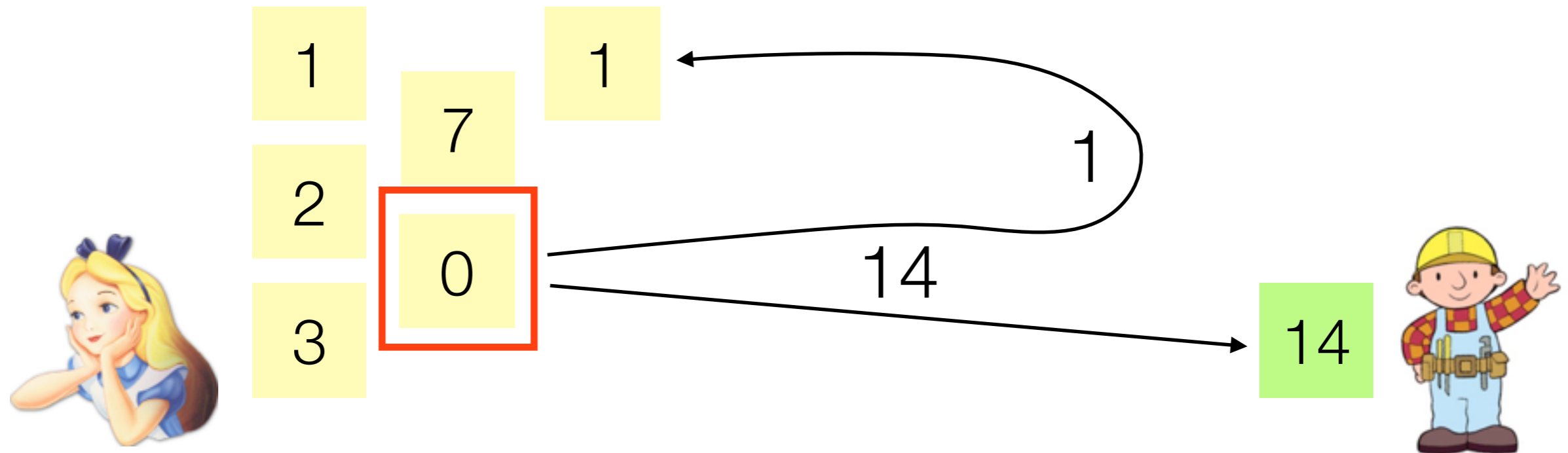
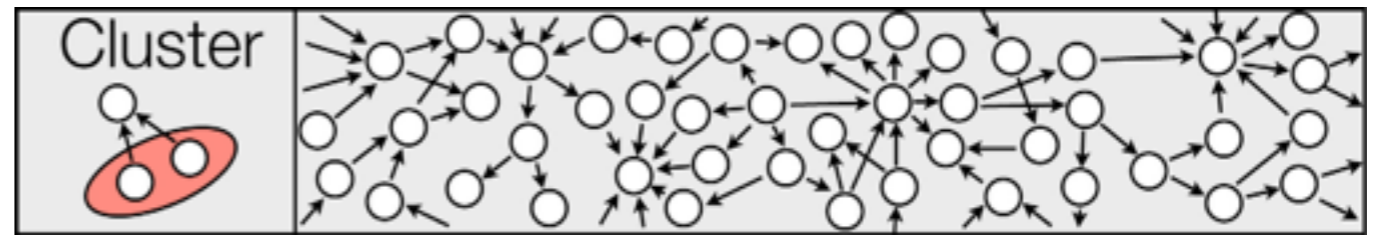
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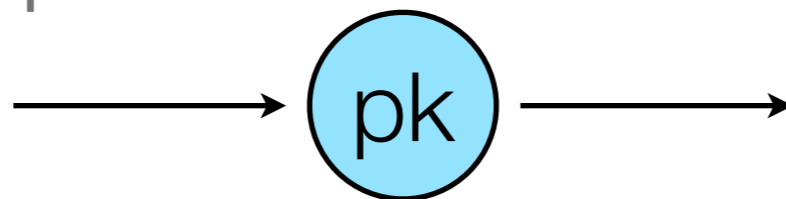
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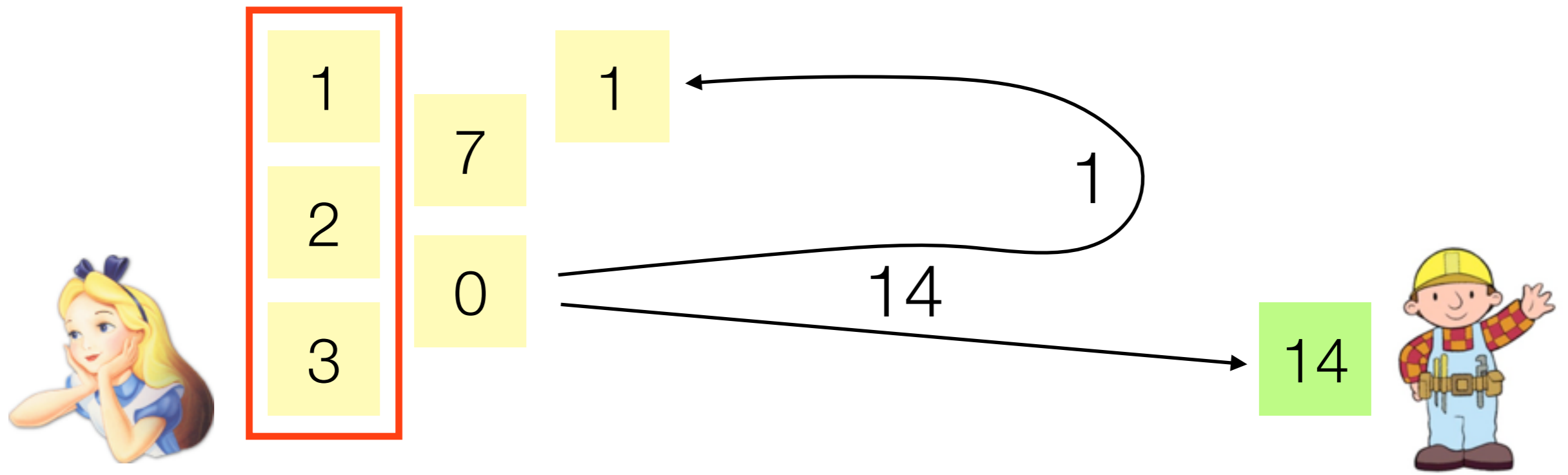
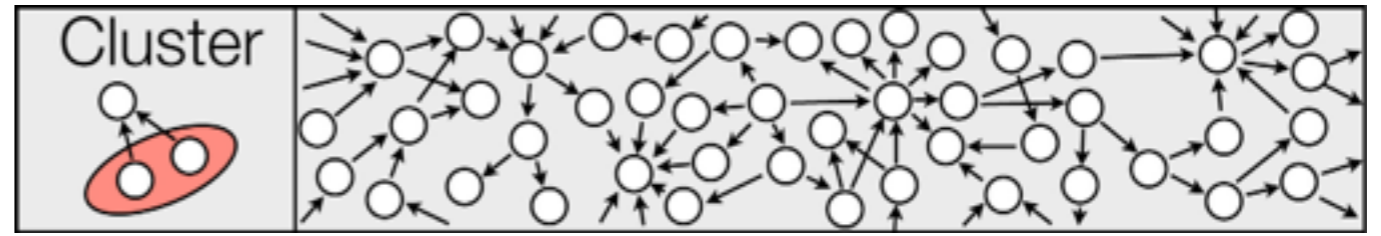


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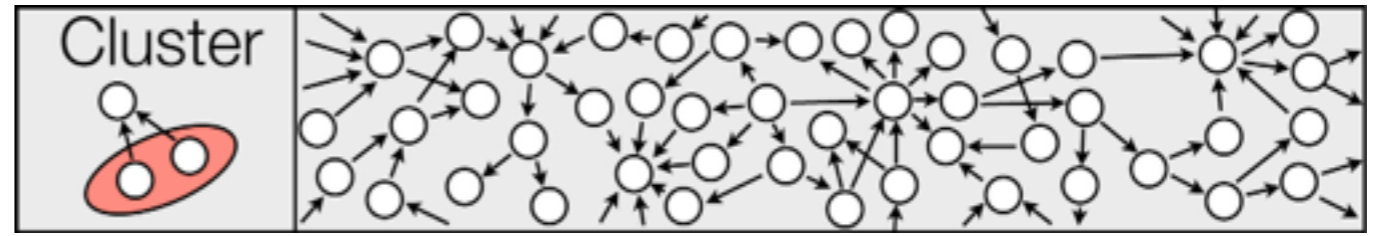
In the standard idiom, change addresses are **used at most twice**: to receive change and to spend it



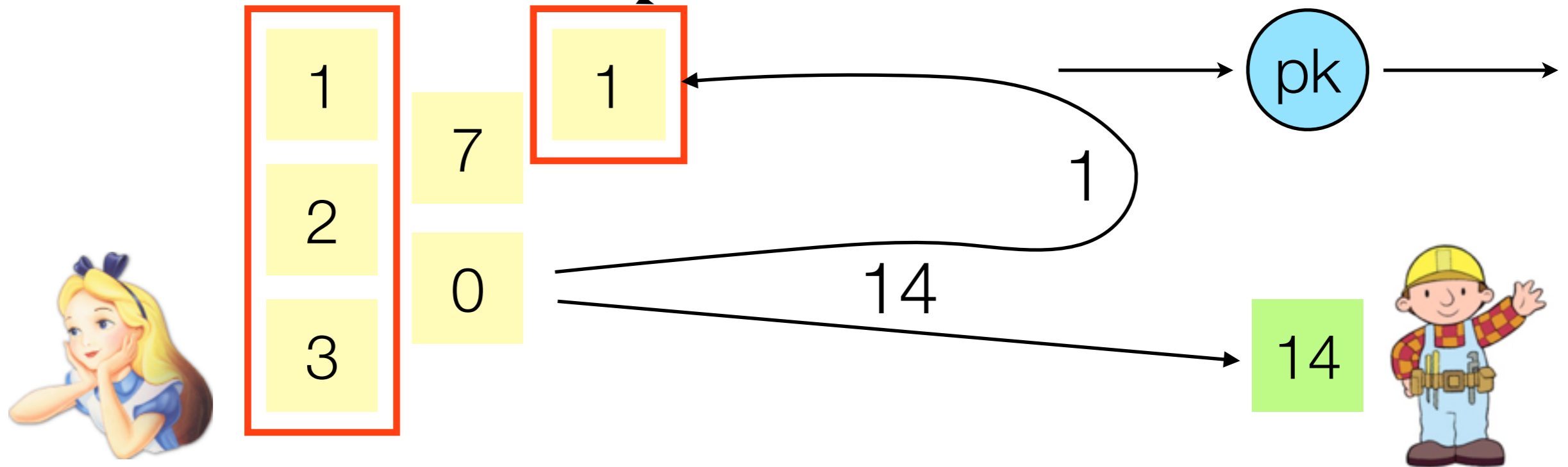
# Clustering by change



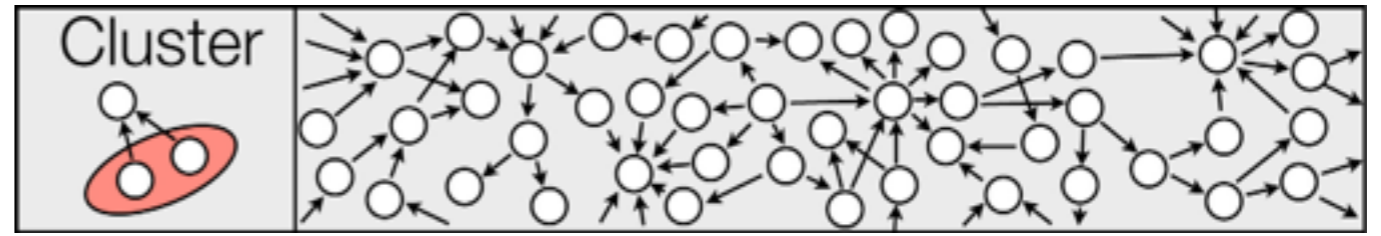
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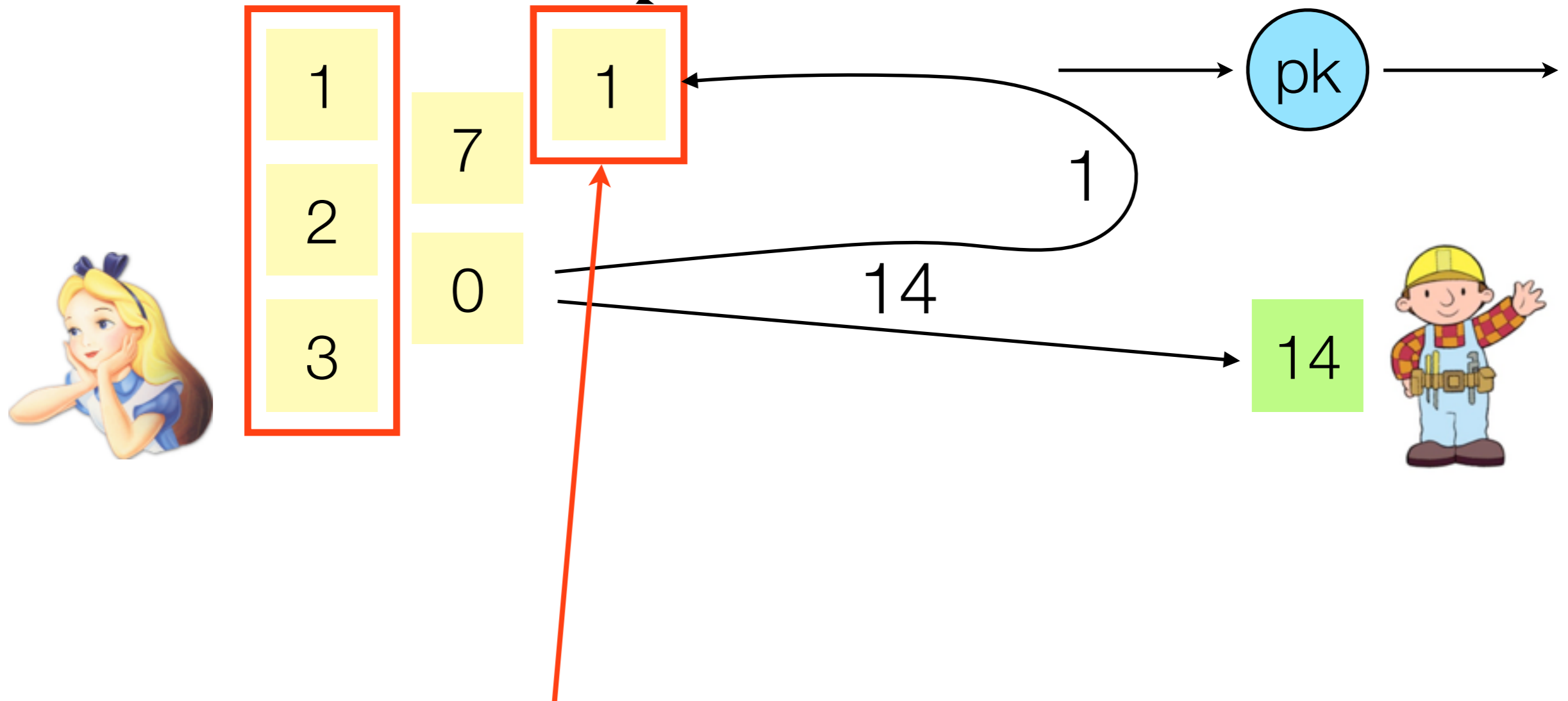
identify using one-time behavior



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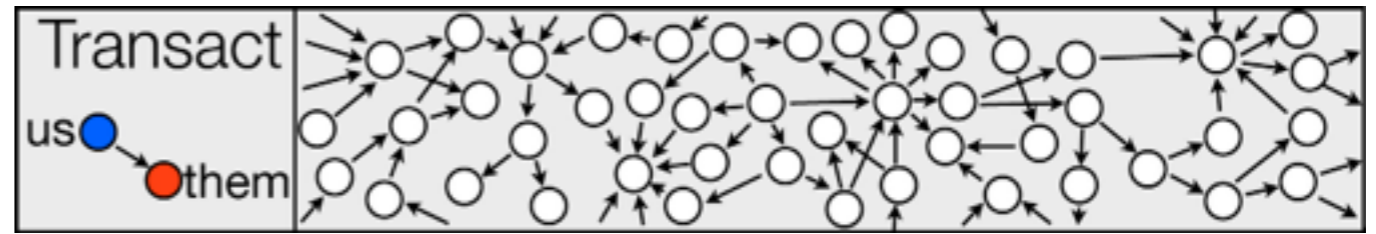
identify using one-time behavior



Heuristic #2: the same user also controls this address

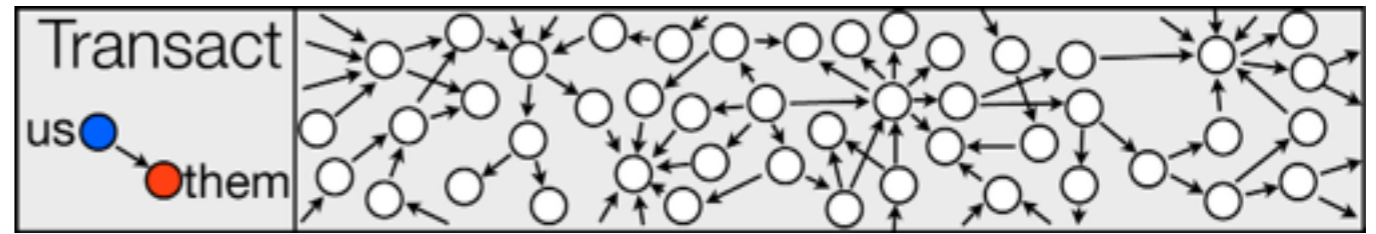
# Data collection

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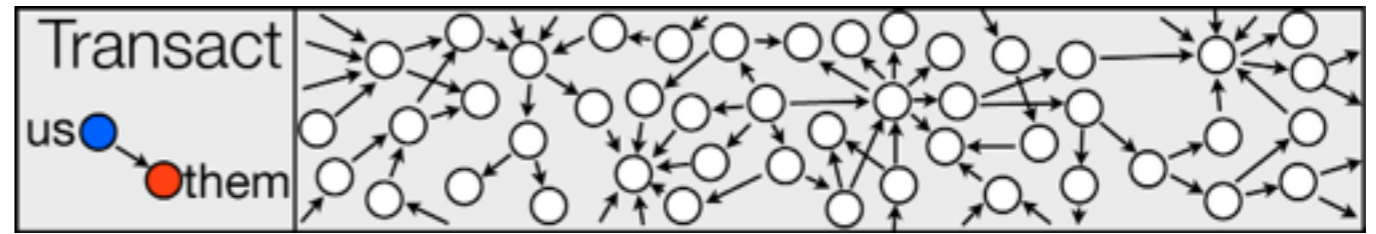
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**Engaged** in transactions with:



# Data collection

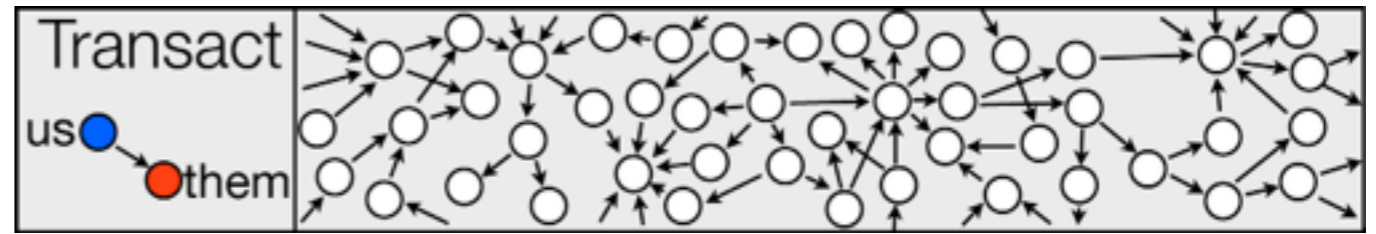


**Engaged** in transactions with:

- Exchanges



# Data collection



Engaged in transactions with:

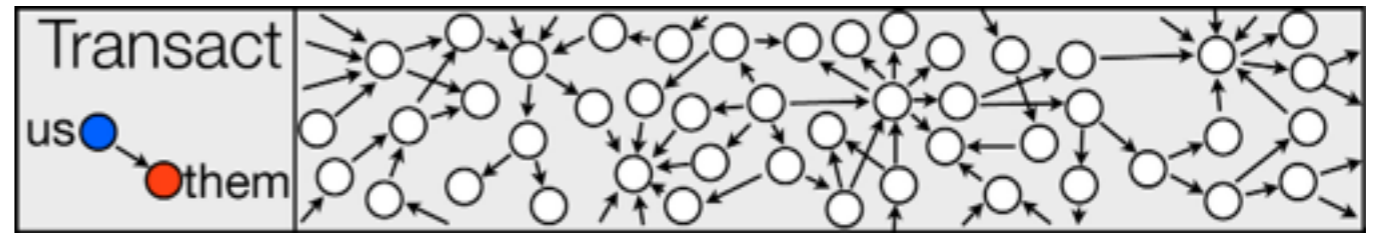
- Exchanges



- Vendors



# Data collection



Engaged in transactions with:

- Exchanges



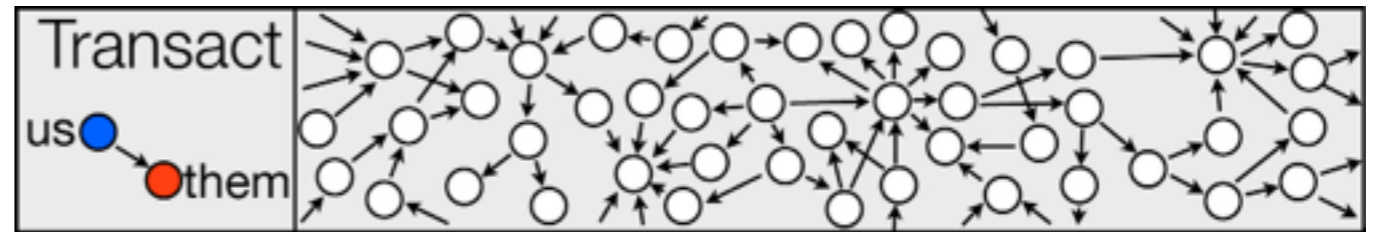
- Vendors



- Mining pools



# Data collection



Engaged in transactions with:

- Exchanges



- Vendors



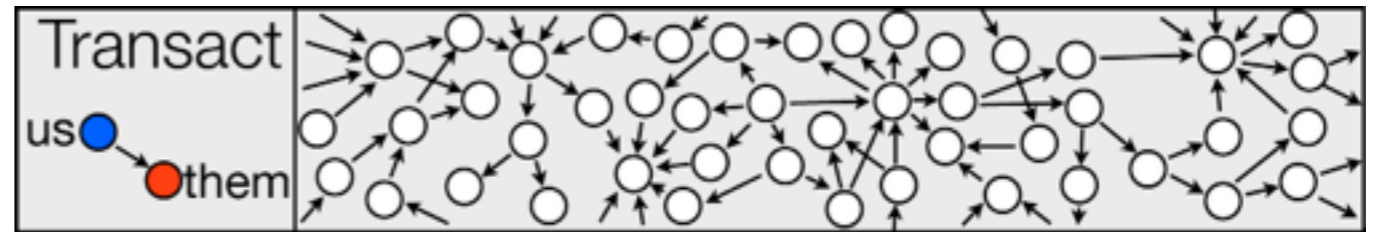
- Mining pools



- Gambling sites



# Data collection



Engaged in transactions with:

- Exchanges



- Mining pools



- Wallet services



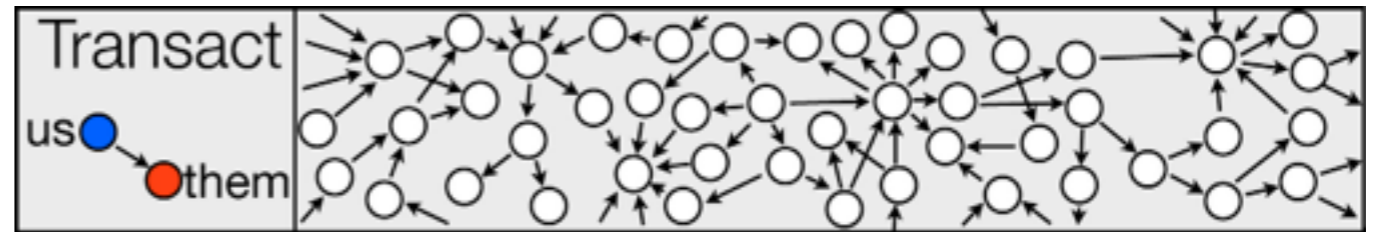
- Vendors



- Gambling sites



# Data collection



Engaged in transactions with:

- Exchanges



- Mining pools



- Wallet services



- Vendors



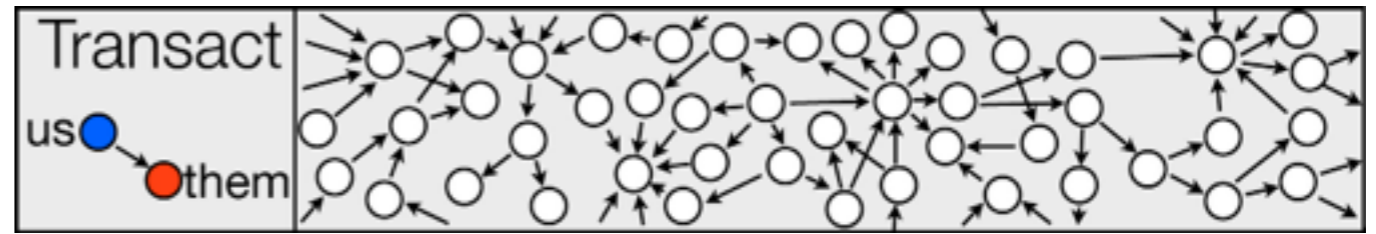
- Gambling sites



- Mix services



# Data collection



Engaged in transactions with:

- Exchanges



- Mining pools



- Wallet services



- Vendors



- Gambling sites

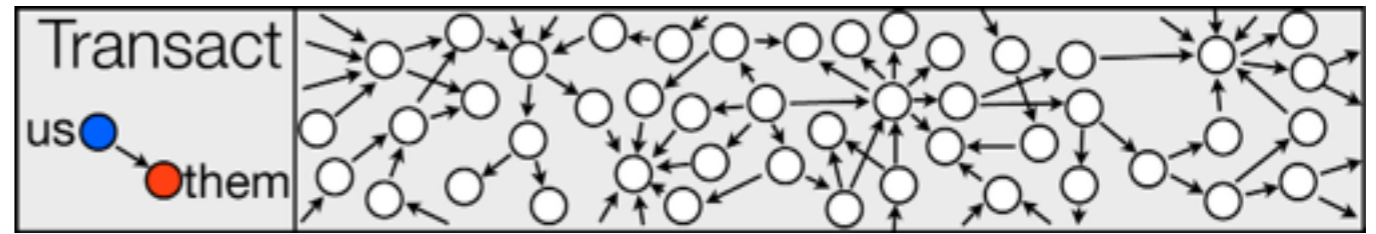


- Mix services



Scraped published tags

# Data collection



**Engaged** in transactions with:

- Exchanges



- Vendors



- Mining pools



- Gambling sites



- Wallet services



- Mix services

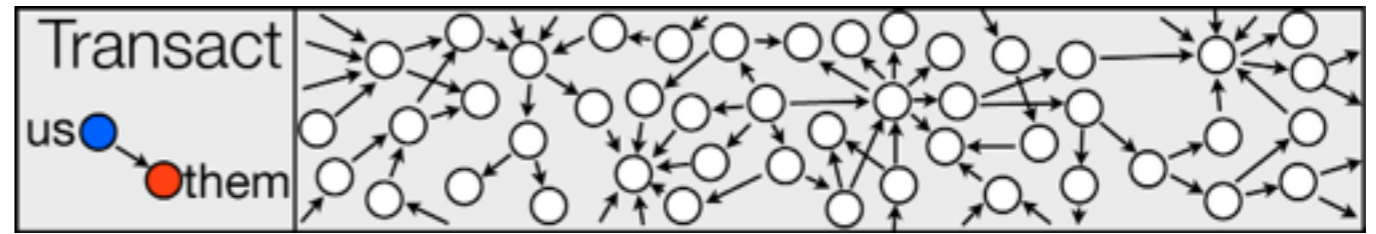


**Scraped** published tags

**Found** addresses discussed on forums



# Exchanges



Bitcoin-24x

Bitcoin-Central

bitcoin.de  
Bitcoin-Marketplace - Made in Germany!

Bitcurex  
The new age of currency.

bitfloor

BitMarket.eu  
YOUR PLACE TO EXCHANGE BITCOINS

BITME

BITSTAMP

Bitcoin China

BTCe

CAMP BX  
BITCOIN TRADING PLATFORM

VirtEx  
Canadian Virtual Exchange

ICBIT  
Bitcoin Exchange

mercadobitcoin

MT.GOX

TRADING LTD.  
THEROCK

Vircurex

VirWOX  
virtual world exchange

aurum



change

BitInstant

BITCOIN NORDIC  
Bitcoins easy. Bitcoins fast.

btcQuick

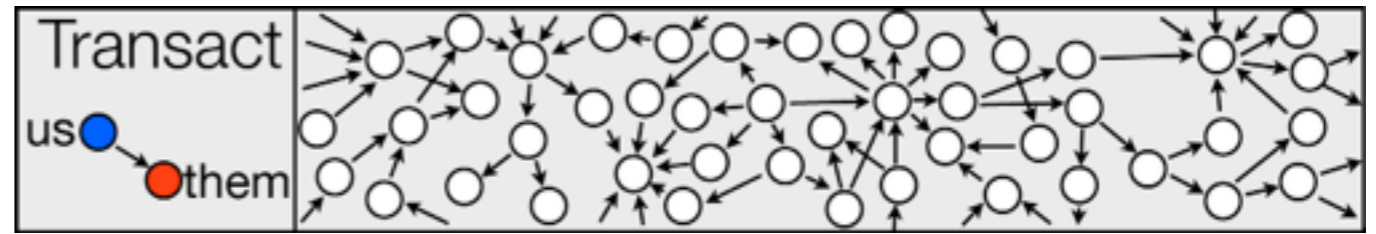
FastCash4Bitcoins

LILION TRANSFER  
Login | Registration

NANAIMO GOLD  
DIGITAL CURRENCY EXCHANGE

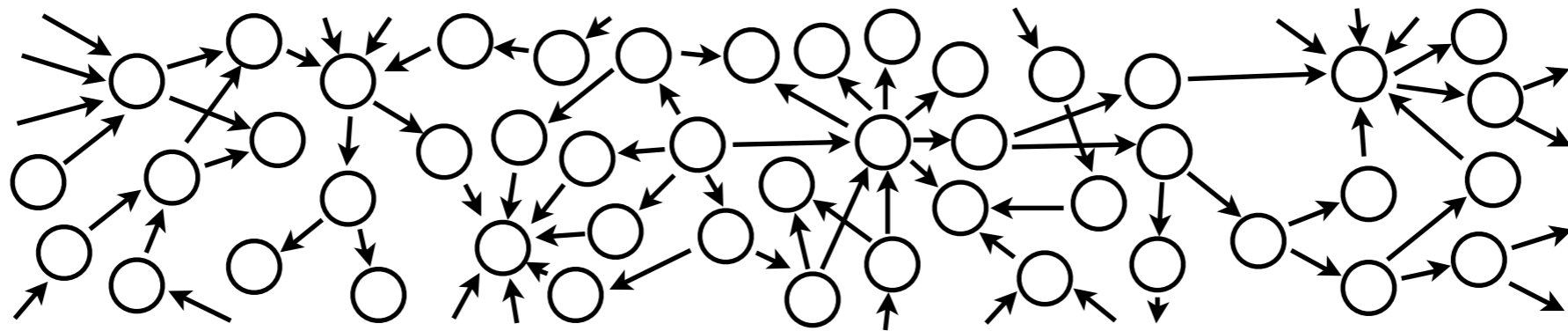
OKPAY payments  
made easy

# Vendors



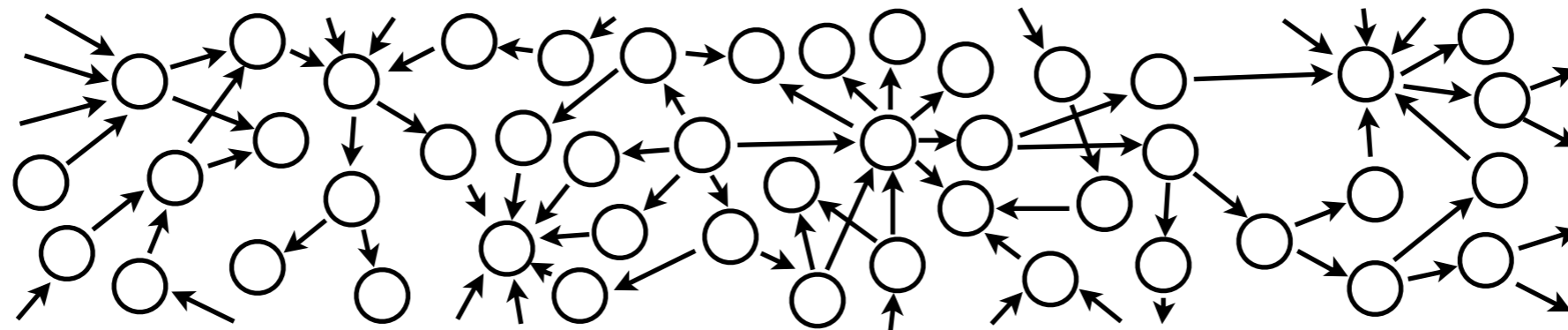
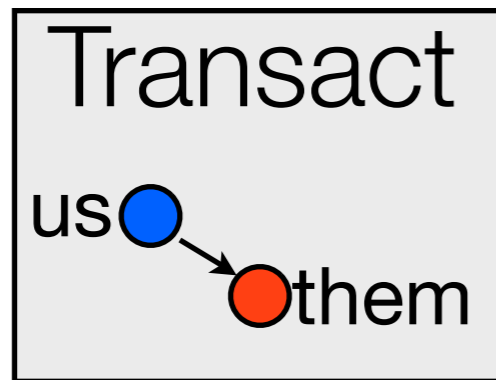
# Putting it all together

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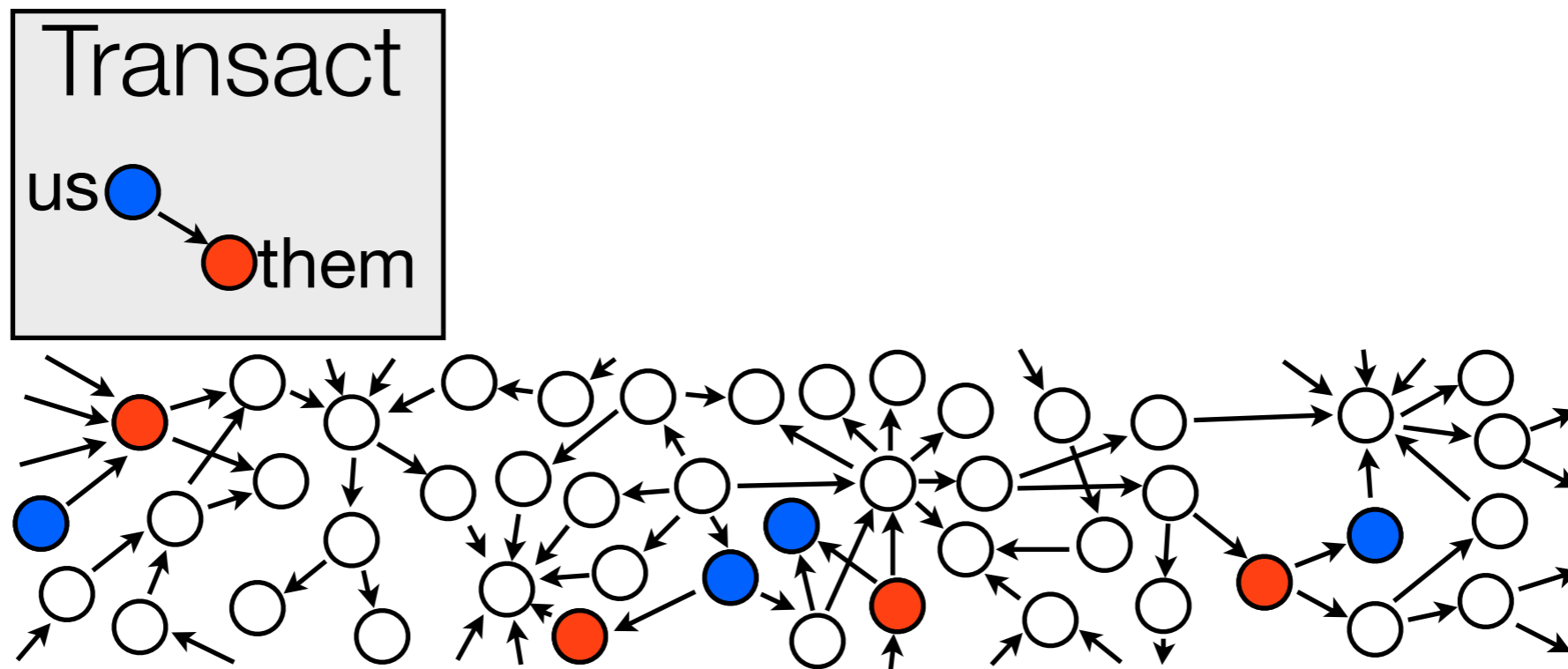
# Putting it all together

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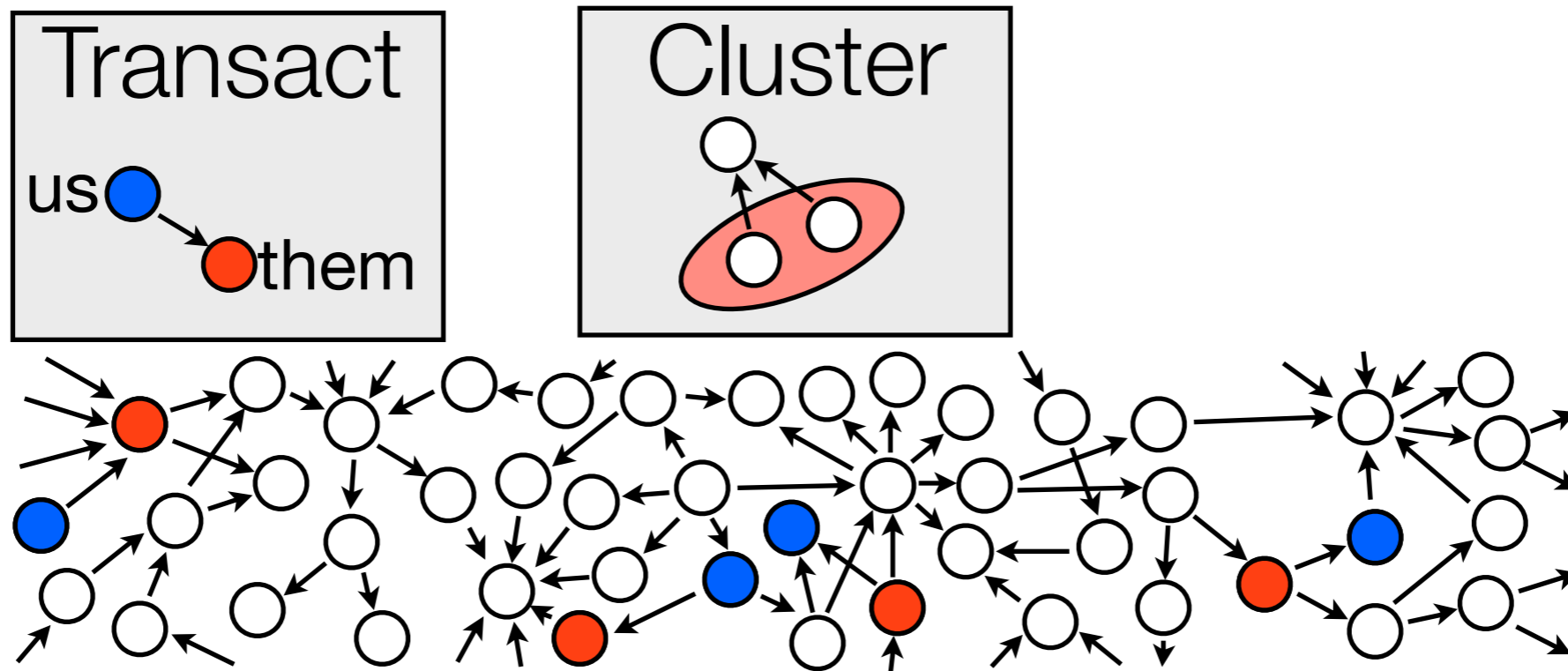
# Putting it all together

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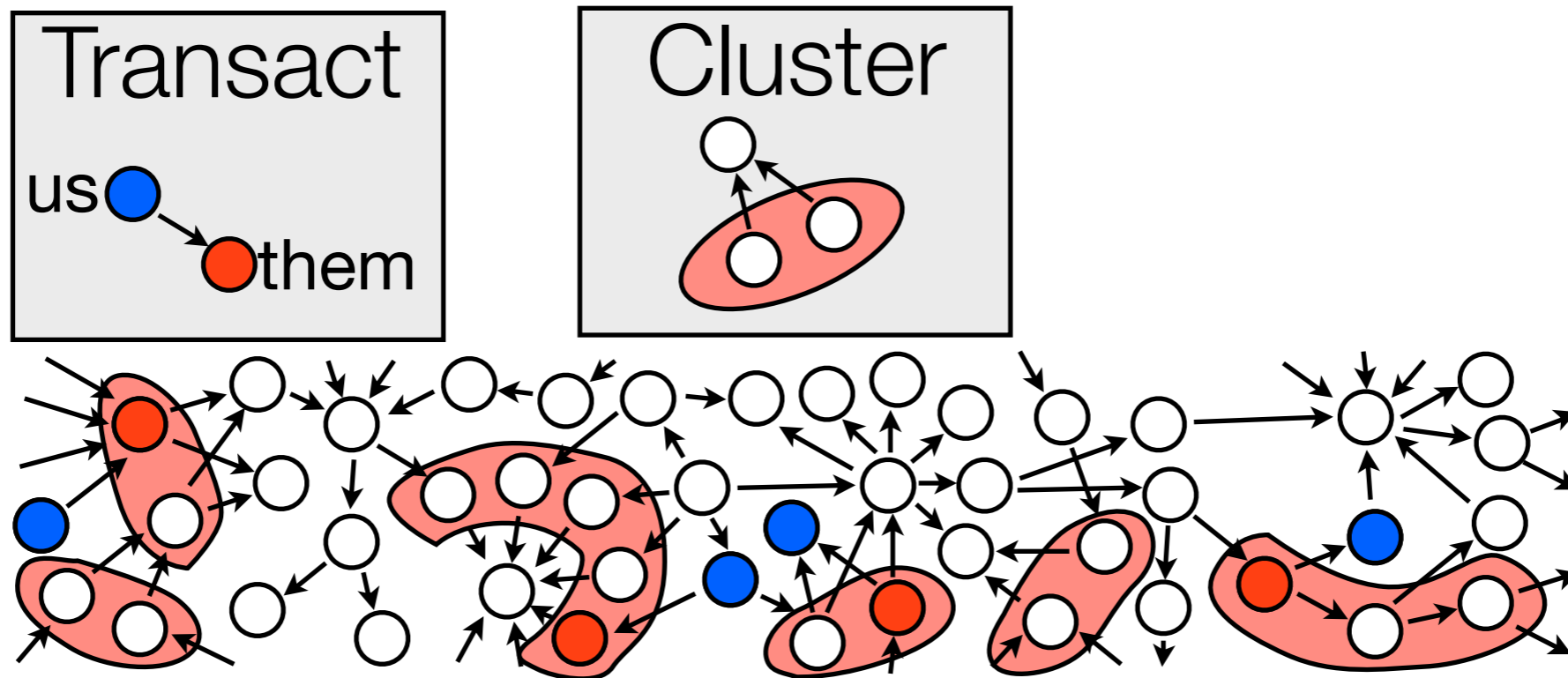
# Putting it all together

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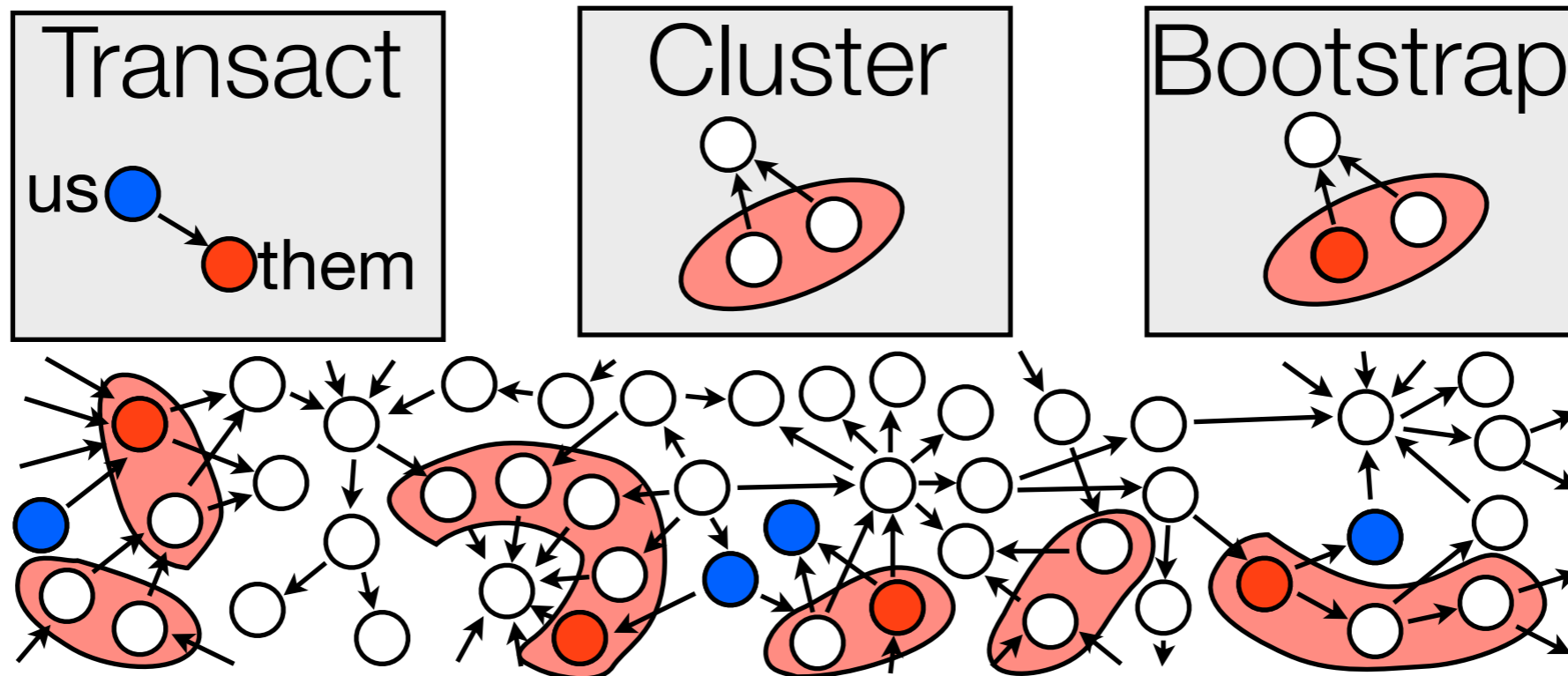
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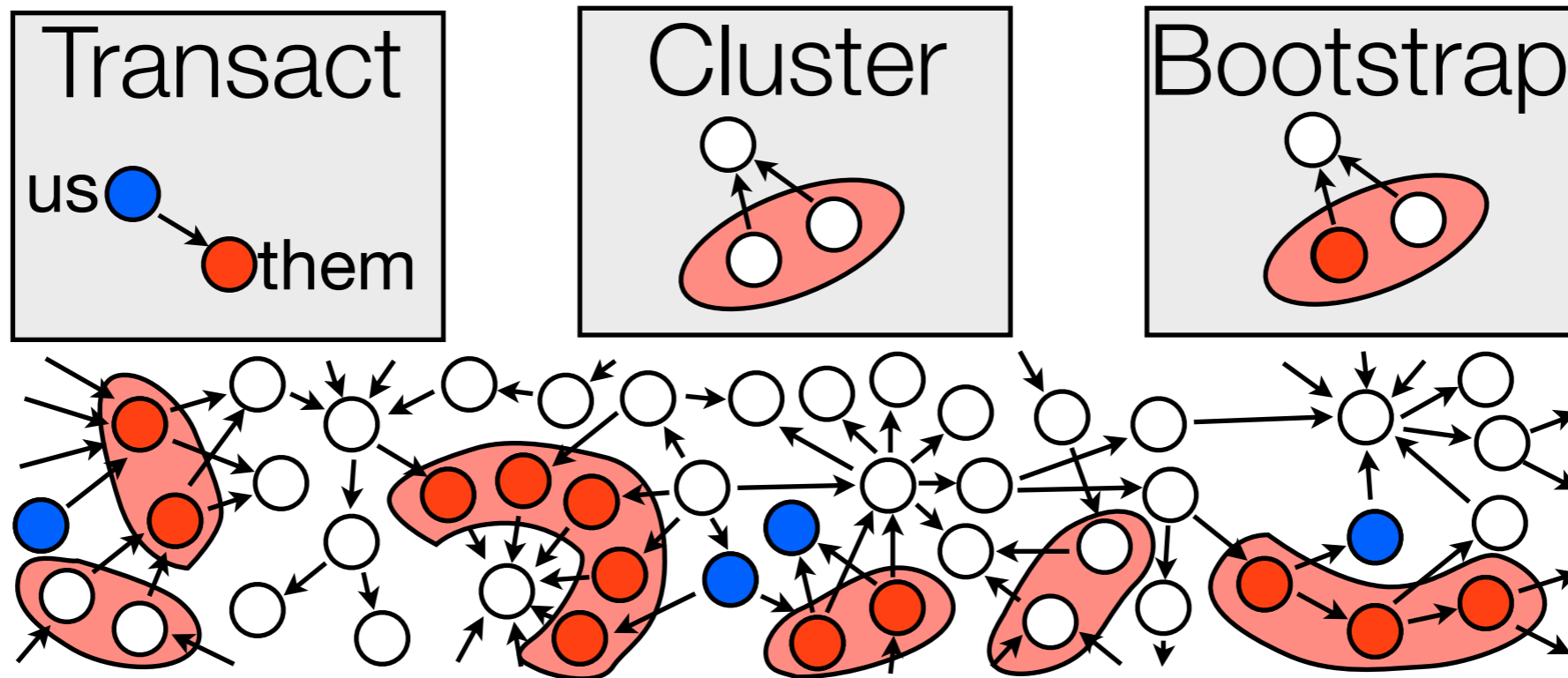
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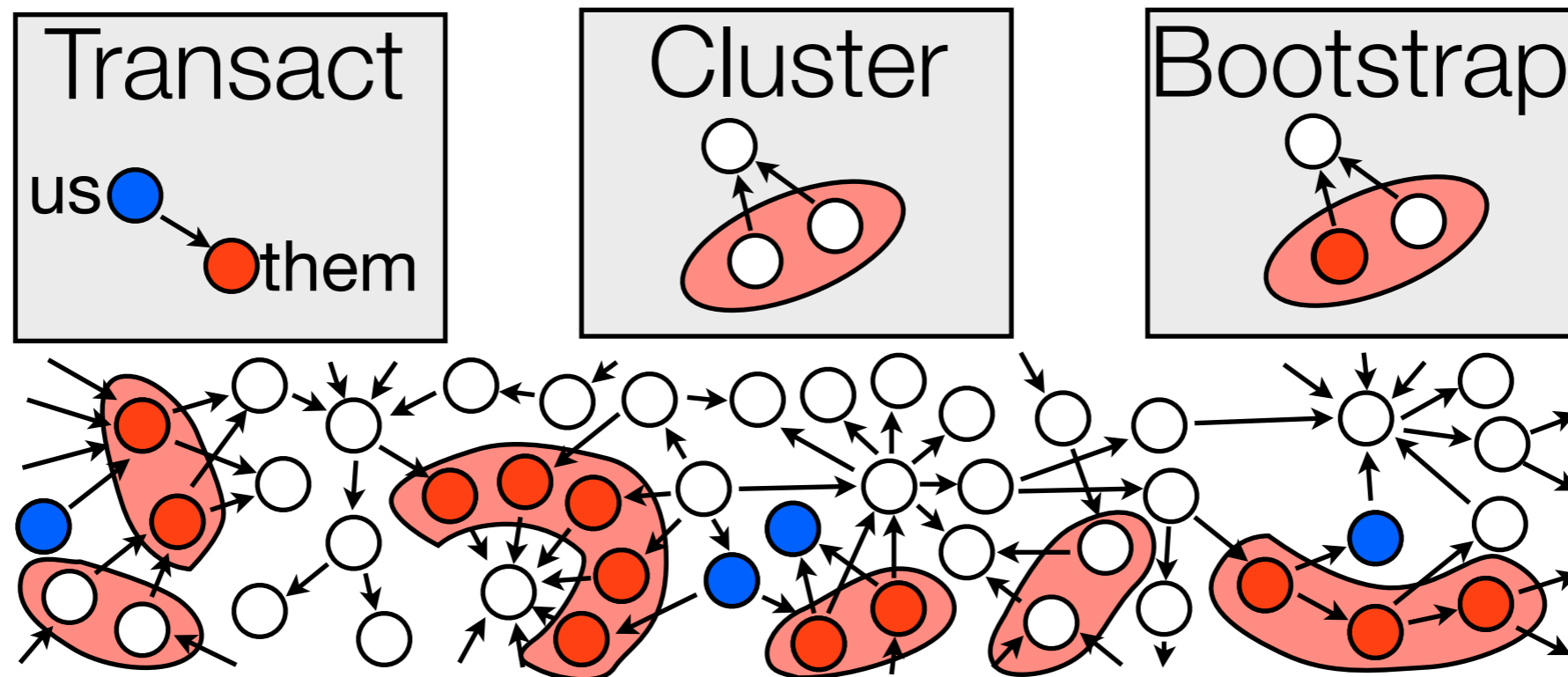
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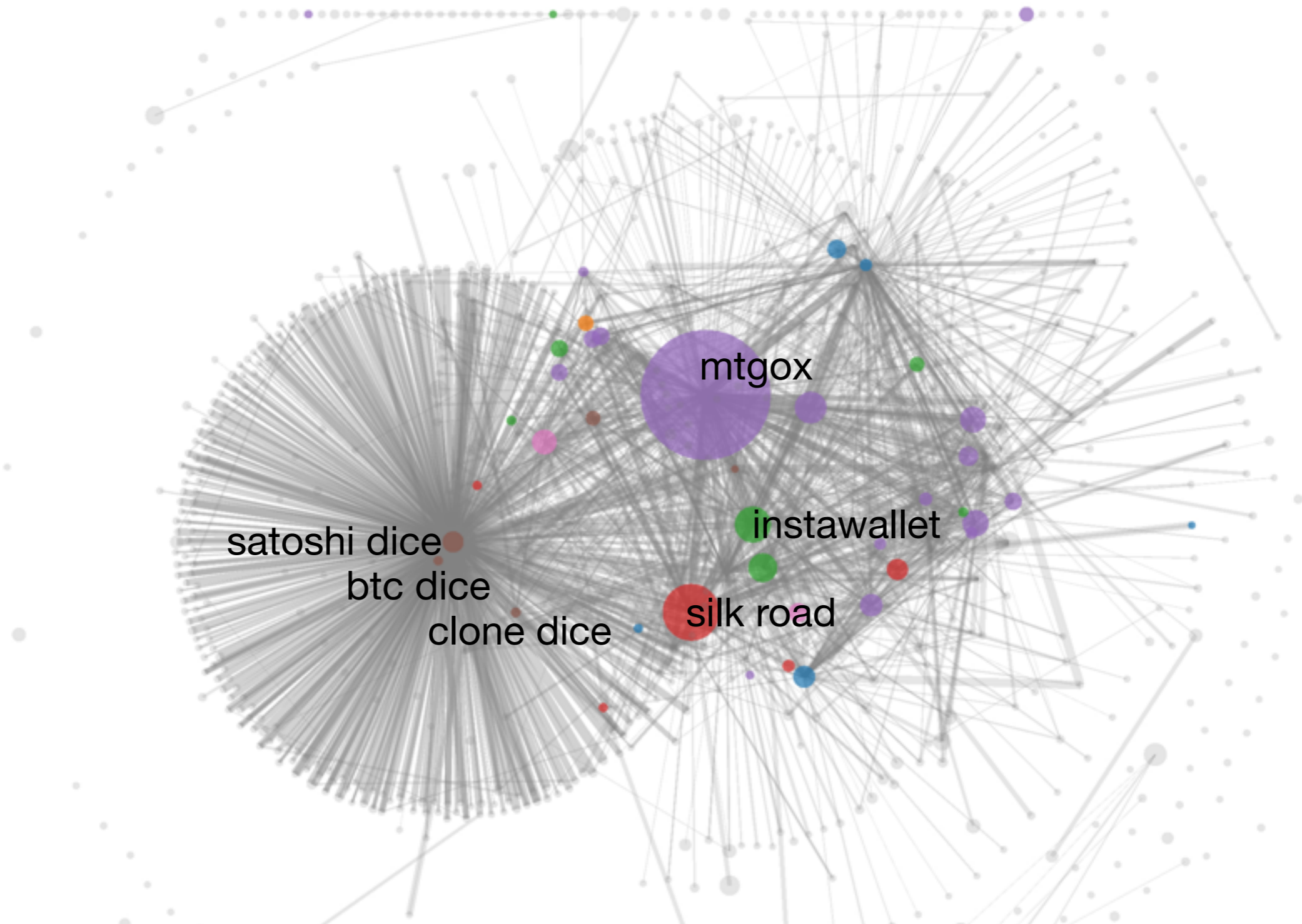


Interacted with **31** MtGox addresses, tagged **518,723!**

Participated in **344** transactions and tagged **1.3M** public keys

# Clustering using Heuristic 2

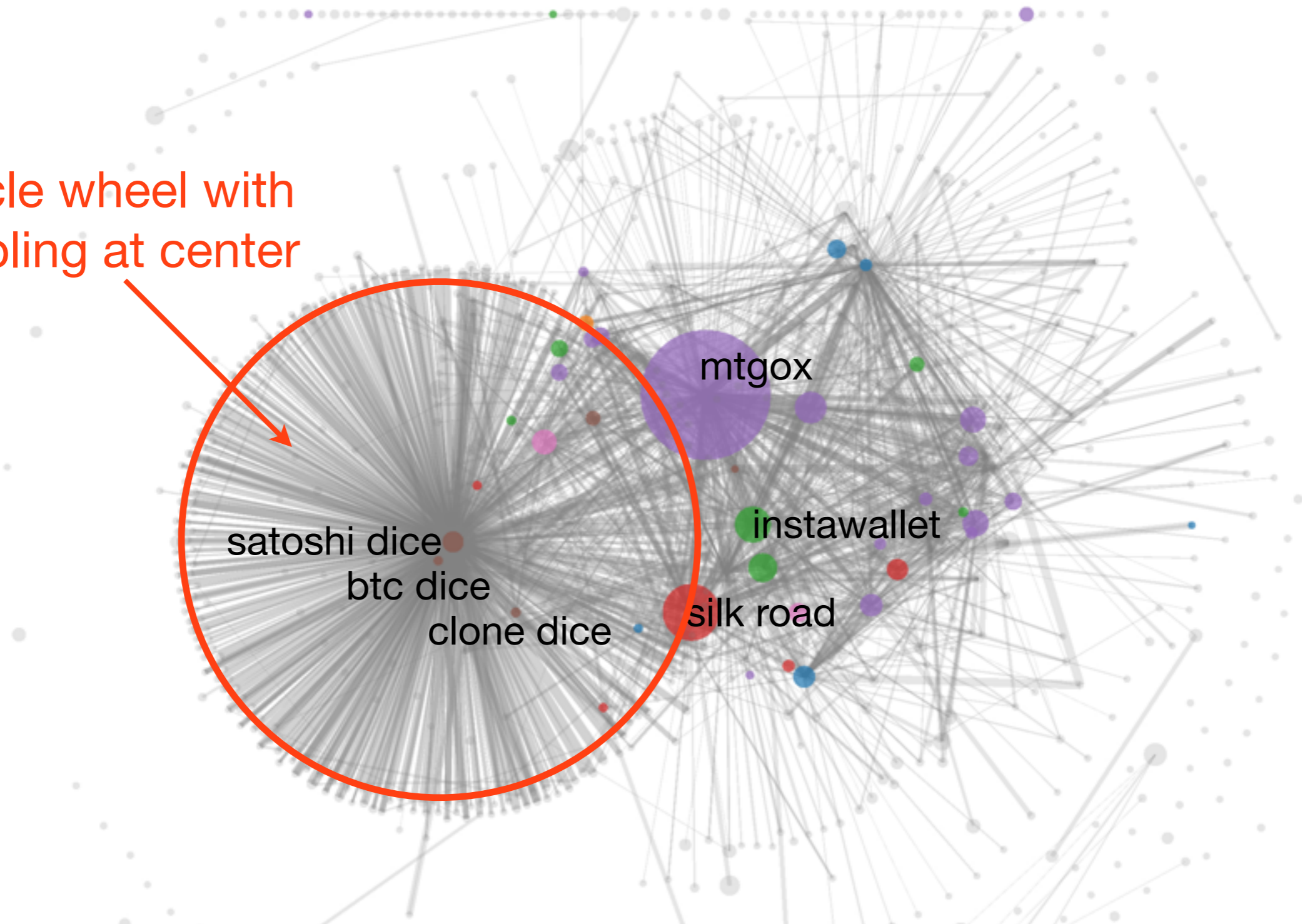
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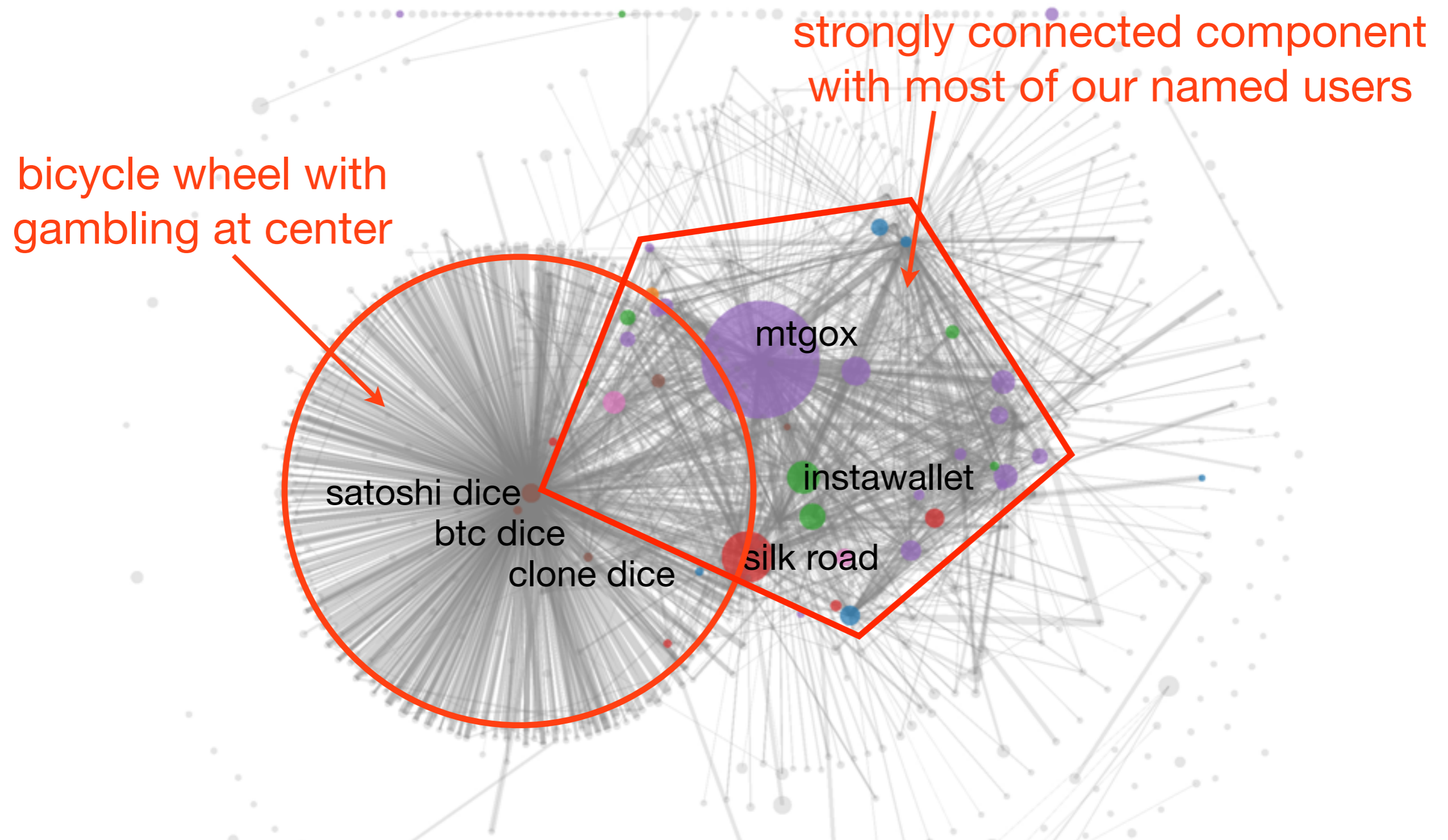
# Clustering using Heuristic 2

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bicycle wheel with  
gambling at center



# Clustering using Heuristic 2



# Following bitcoins

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# Following bitcoins

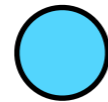
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Can see when bitcoins meaningfully **cross cluster boundaries**

# Following bitcoins

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Can see when bitcoins meaningfully **cross cluster boundaries**

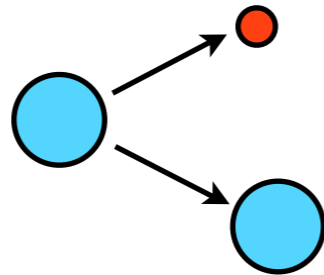




# Following bitcoins

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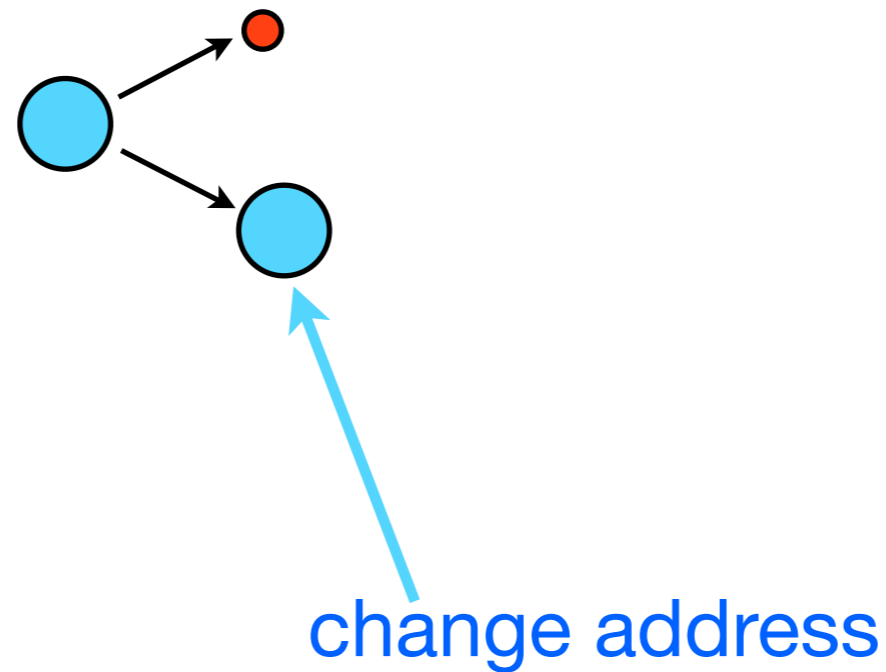
Can see when bitcoins meaningfully **cross cluster boundaries**



# Following bitcoins

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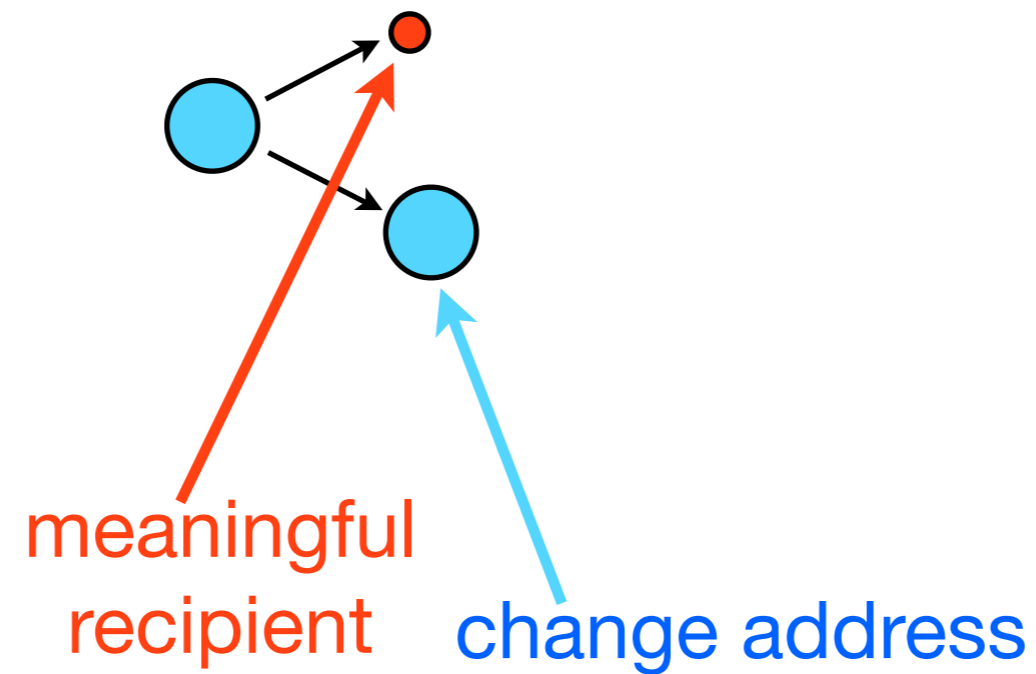
Can see when bitcoins meaningfully **cross cluster boundaries**



# Following bitcoins

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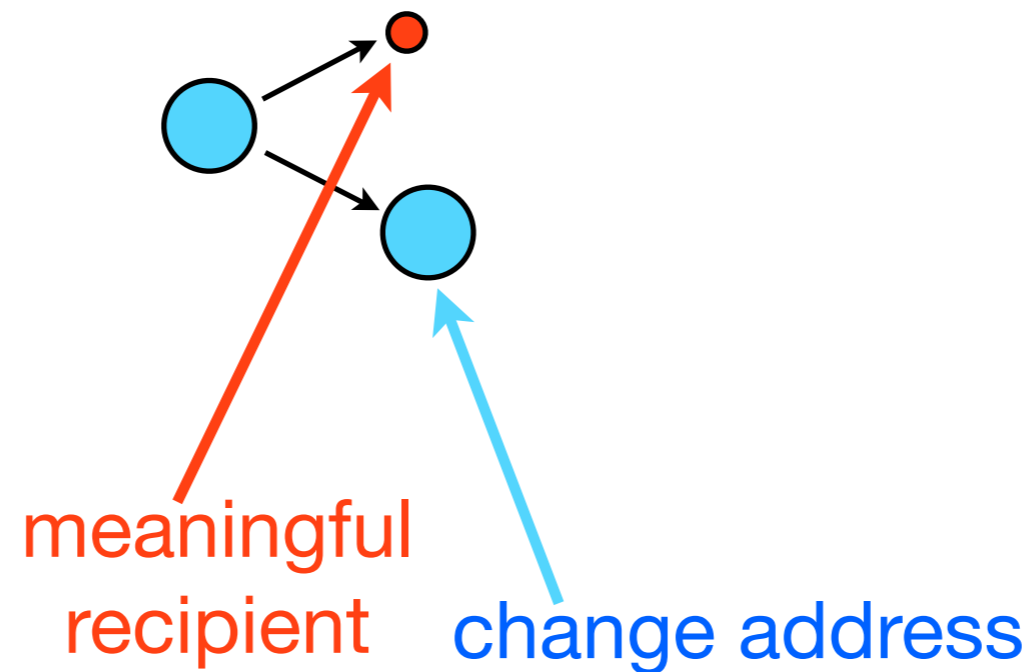
Can see when bitcoins meaningfully **cross cluster boundaries**



# Following bitcoins

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Can see when bitcoins meaningfully **cross cluster boundaries**

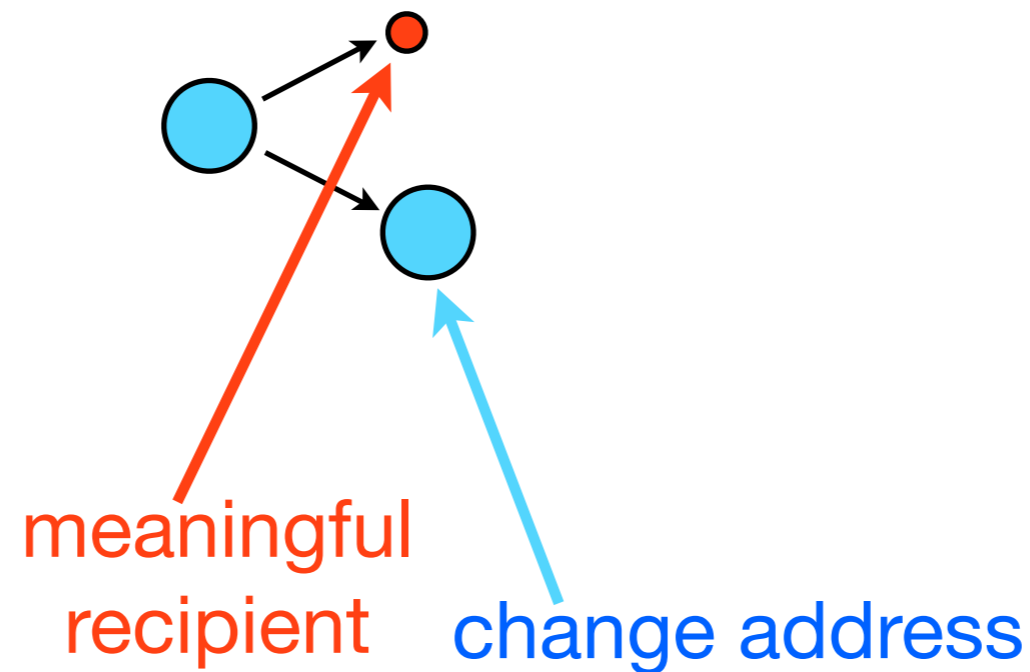


Identifying recipients **potentially de-anonymizes user**

# Following bitcoins

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Can see when bitcoins meaningfully **cross cluster boundaries**



Identifying recipients **potentially de-anonymizes user**

**Hypothesis: if you subpoena exchanges, you can identify users**

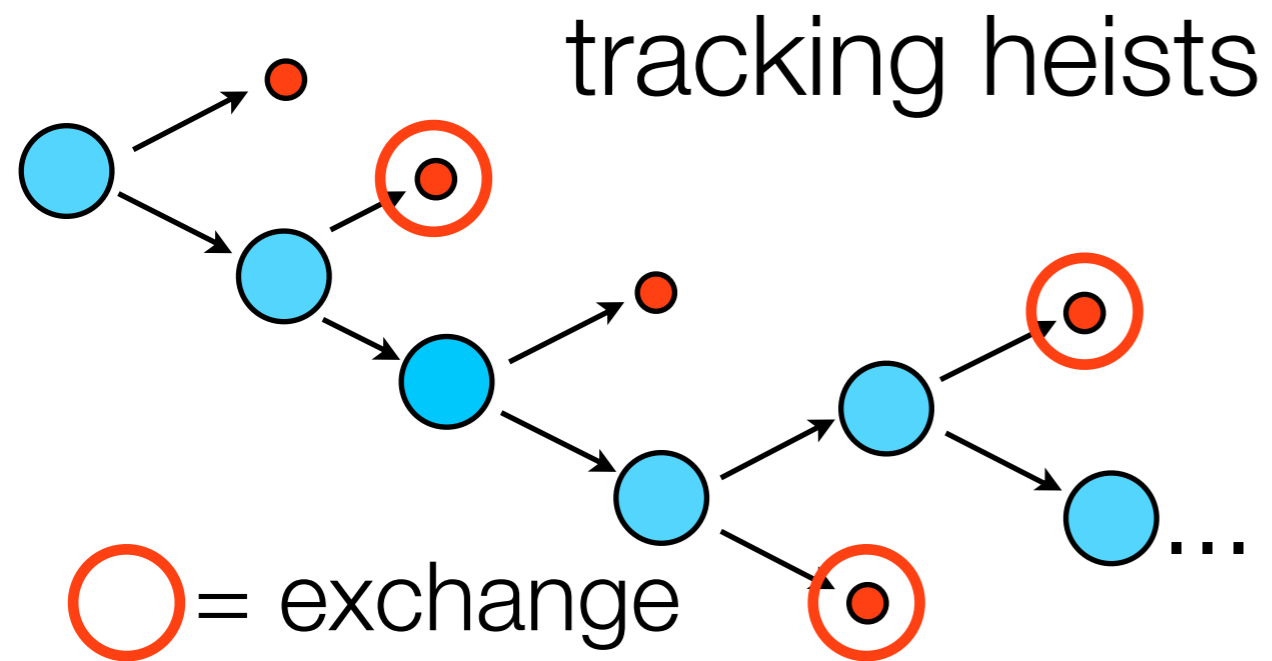
# Tracking technique

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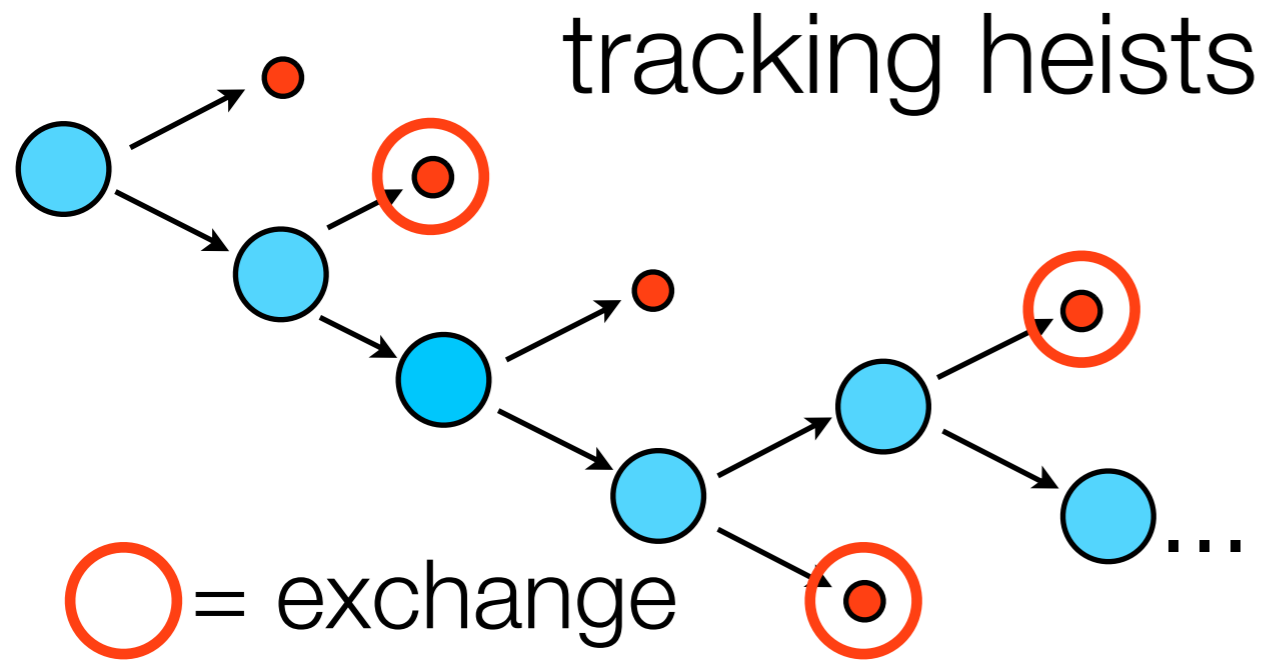


# Tracking technique

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# Tracking technique



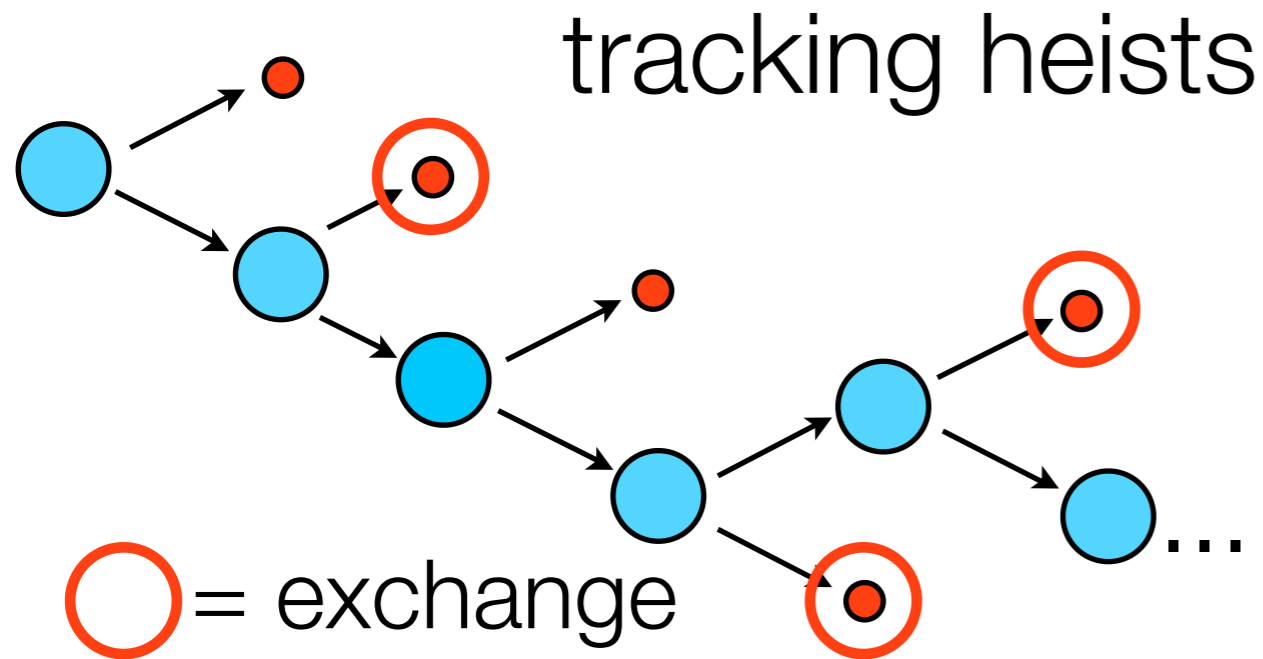
[HDM+ NDSS'14]



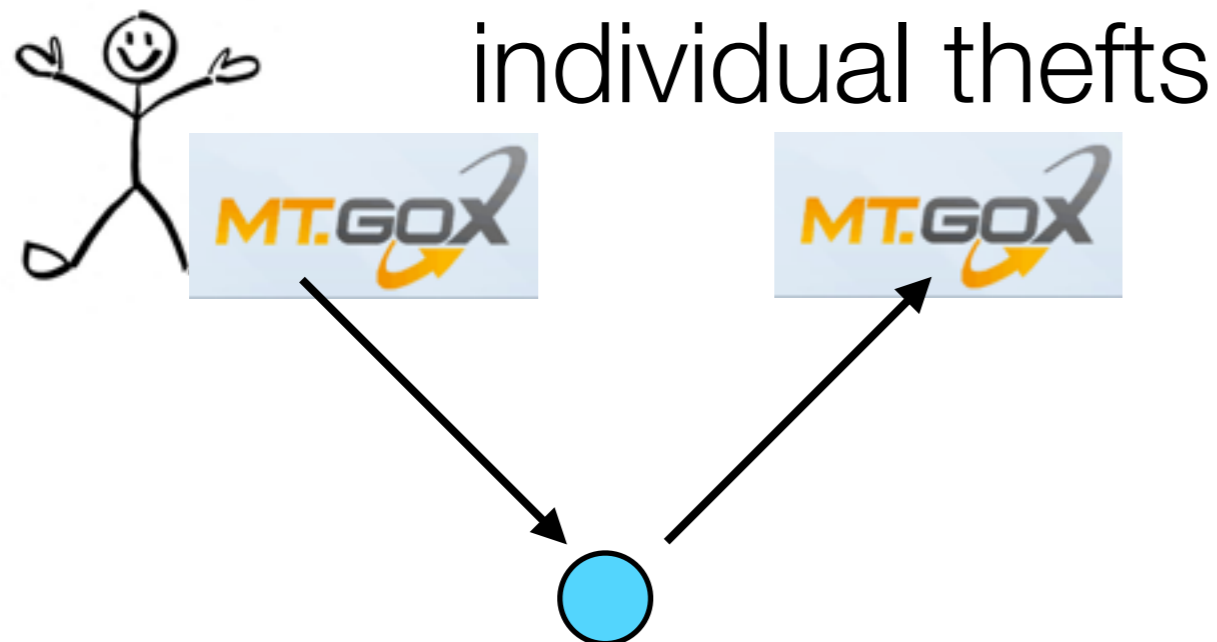
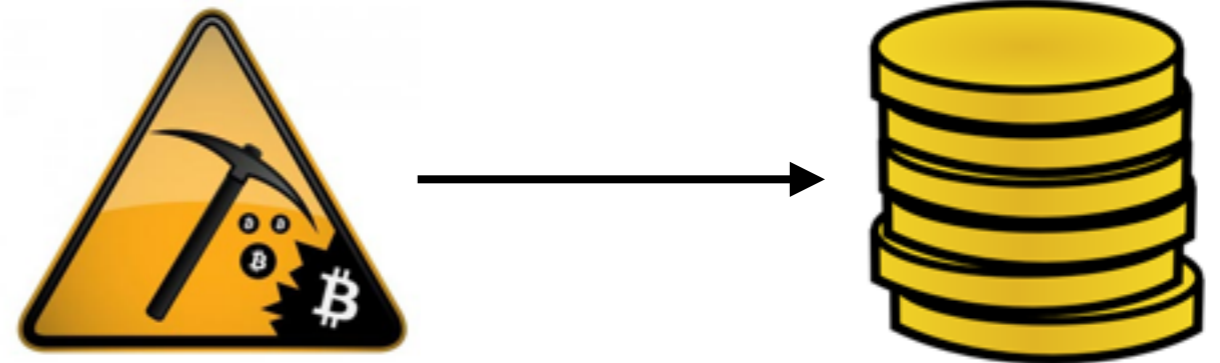




# Tracking technique



[HDM+ NDSS'14]



service interaction

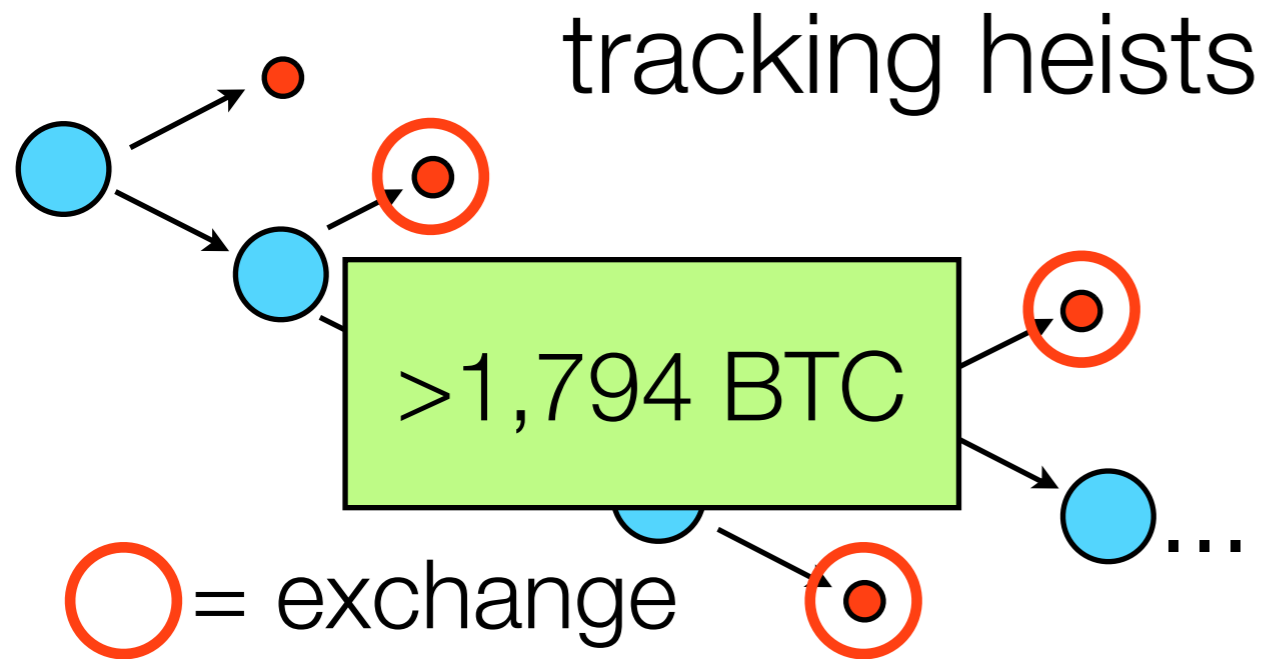


**Andy Greenberg**, Forbes Staff  
Covering the worlds of data security, privacy and hacker culture.  
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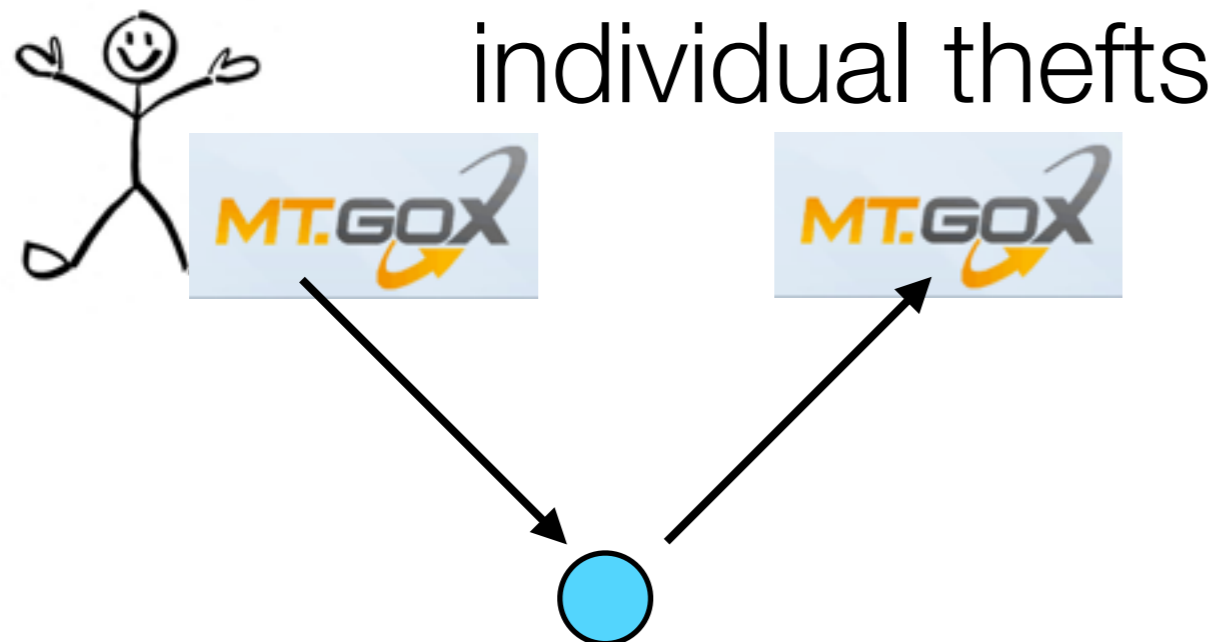
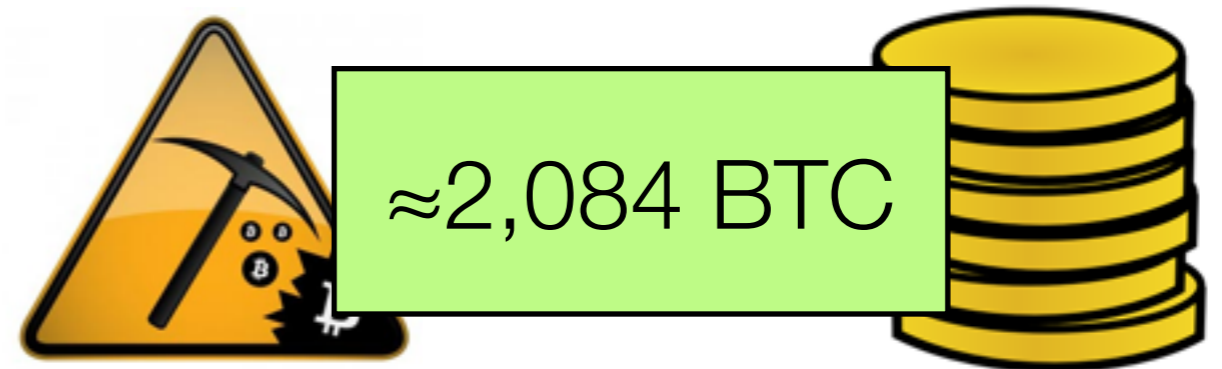
SECURITY | 9/05/2013 @ 10:36AM | 131,694 views

**Follow The Bitcoins: How We Got Busted Buying Drugs On Silk Road's Black Market**

# Tracking technique



[HDM+ NDSS'14]



service interaction



Andy Greenberg, Forbes Staff

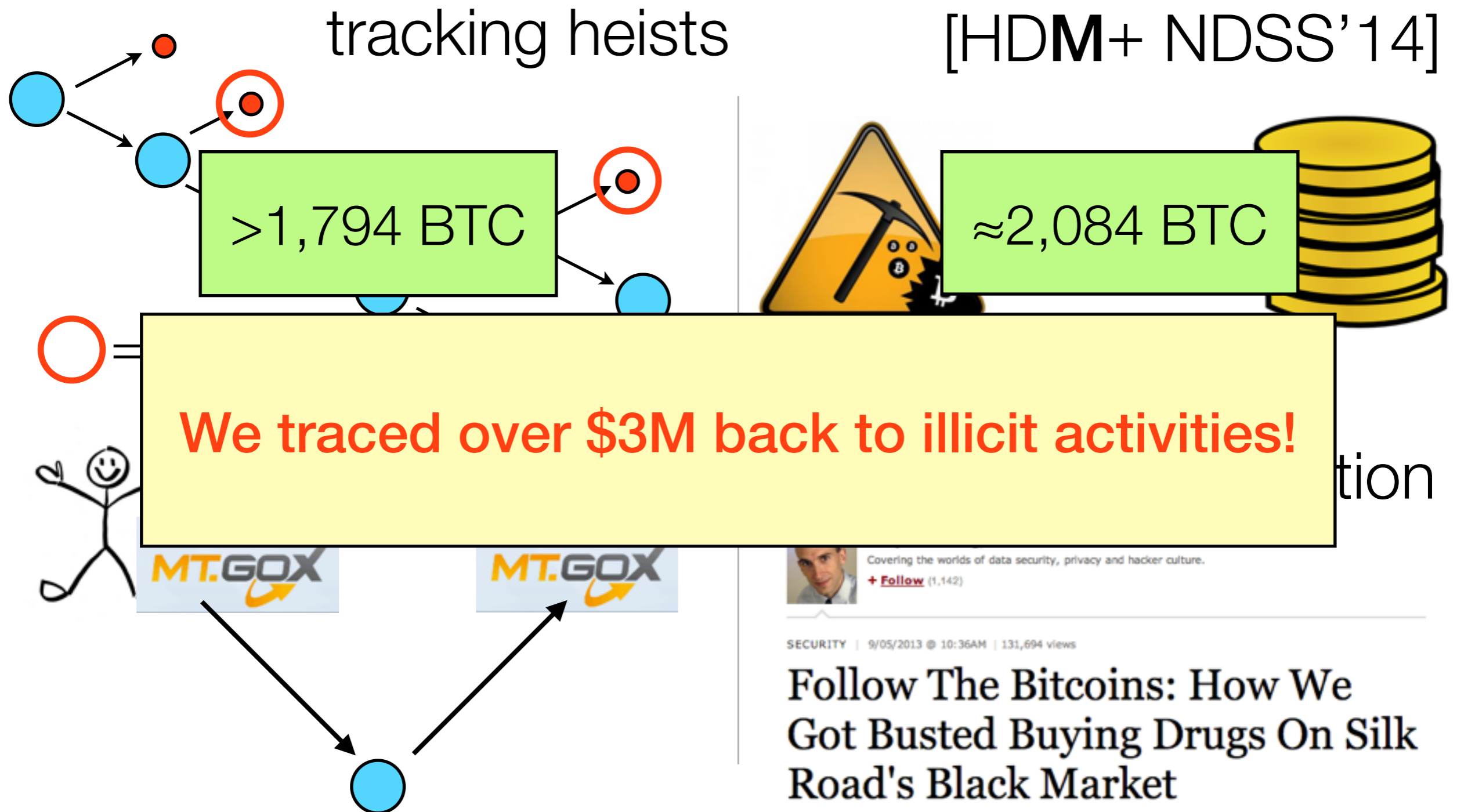
Covering the worlds of data security, privacy and hacker culture.

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Follow The Bitcoins: How We Got Busted Buying Drugs On Silk Road's Black Market

# Tracking technique



# Takeaway

**How much anonymity does Bitcoin really provide?**

# Takeaway

**How much anonymity does Bitcoin really provide?**

Our analysis provides a real-world way to **track flows of bitcoins**



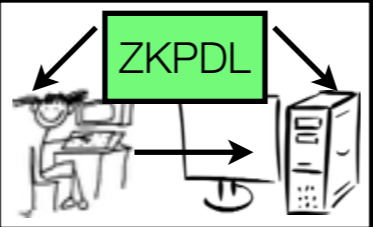

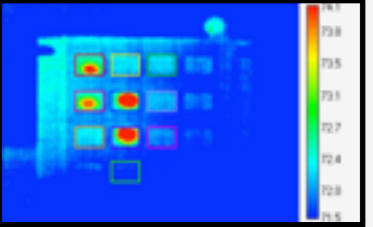
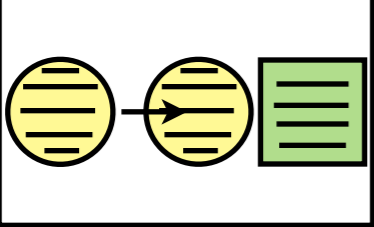
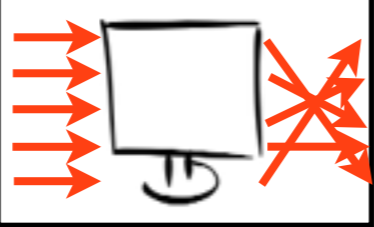


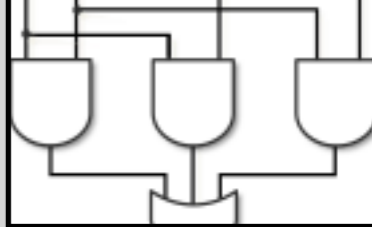
# Takeaway


**How much anonymity does Bitcoin really provide?**

Our analysis provides a real-world way to **track flows of bitcoins**


Seems **hard to launder** significant quantities of money

# My research

 [MSF10,LM13]	 [BMT14]	 [MEKHL10]	 [MMCS11]	 [MMS11]
 [CM14]	 [CKLM12,13a,13b]	 [CMZ13]	 [MP+13,HDM+14]	 [OMSK13]



RKA



Bitcoin



# Acknowledgements



RKA



Bitcoin

# Acknowledgements

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Thanks! Any questions?