

BAMS

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52 1946

A 110

106. H. W. Becker: Combinatory interpretations of Bell's numbers.

These are evolved by iterated matrix multiplication of the table of Stirling's numbers, second kind (E. T. Bell, Amer. J. Math. vol. 61 (1939) p. 89; Ann. of Math. vol. 39 (1938) p. 539). They enumerate: (1) the number of distributions of  $n$  individuals into crews (or circuits), with  $m$  levels of hierarchy (or insulation, or jumpers) in the organization chart; (2) the number of rhyme schemes, or logical relatives (C. S. Peirce, Amer. J. Math. vol. 3 (1880) p. 48) with  $m$  plexes of nuance possible to each letter. (Specialized, these yield compositions and partitions of numbers under  $m$  modes of addition, as normal, weak, strong, and so on.) The readily formulated breakdowns are formulated according to (1) number of crews, or, equivalently, (2) number of different letters, and to (1) size of first crew, or, equivalently, (2) number of  $a$ 's. The above may further be interpreted as a generalization of the substitution cycles and described polygons of Touchard (Acta Math. vol. 70 (1939) p. 249): in which the cycles are separated by up to  $m$  types of parenthesis; or the polygons are bounded by lines of up to  $m$  different colors simultaneously. (Received March 21, 1946.)

107. H. W. Becker: The general theory of rhyme.

Prosodic rhyme schemes are called sequations, abstractly, of umbra @. They classify according to range (number of different letters), terminal (last letter), singletons (rhymed letters, more generally any partition of letters), and quantum (number of letters, more generally any composition of letters). Generalizations are the multipolar, multinomial, multinary, multiplex, and multilinear sequations, having respectively  $m$  types of accent, alphabet, partial identity, nuance of nuance, and parallelism. Specialized patrices (expansions of a matrix, with given path restrictions) are those in which: each letter rhymes  $s$  times or more, or less; some letter, or none, occurs  $s$ -ply; no rhyme repeats within  $s$  adjacencies; the differences of successive letters are restricted; given letters are forbidden, or fixed, in certain positions; all numbers in the partition, or range, are odd, or even; there are no nonconsecutive rhymes (these are isomorphic with compositions); the previous is further specialized, to be isomorphic with partitions. In permuted sequations, the debuts of the different letters are in non-alphabetic order: enumerated by differences of zero, integer powers, and the polynomials  $(@M+X)^n$ . These polynomials kernel the lexicon theorems, by which the sequances are well-ordered. All are generated by variations of  $\exp t@ = \exp (e^t - 1)$ . (Received March 21, 1946.)

A 110

108. ~~A. T. Brauer: On a theorem of M. Bauer.~~

In generalization of a theorem of M. Bauer (J. Reine Angew. Math. vol. 131 (1906) pp. 265-267) the following theorem is proved. Let  $f(x)$  be a polynomial with rational coefficients which has at least one real root. Let  $G(k)$  be the group of the residue classes relatively prime to  $k$ , and  $H$  a subgroup which does not contain the class of numbers congruent to  $-1 \pmod{k}$ . Then  $f(x)$  contains infinitely many prime divisors which do not belong to the classes of  $H$ . It follows for instance that each polynomial contains an infinite number of prime divisors which are quadratic residues for a given prime of form  $4n+3$ . (Received March 20, 1946.)

109. ~~A. T. Brauer and Gertrude Ehrlich: On the irreducibility of certain polynomials.~~

Pólya has proved the following theorem (Jber. Deutschen Math. Verein. vol. 28 (1919) pp. 31-40): If for  $n$  integral values of  $x$ , the integral polynomial  $P(x)$  of degree